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ADVANCED THRUST VECTOR CONTROL PRELIMINARY DESIGN COMPUTER PROGRAM

Volume I Program Description Book 1 Requirements

THIOKOL / WASATCH DIVISION

A DIVISION OF THIOKOL CHEMICAL CORPORATION

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AIR FORCE ROCKET PROPULSION LABORATORY
EDWARDS AIR FORCE BASE, CALIFORNIA

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FOREWORD

The ASC/TMC Preliminary Design Computer Program for air and surface launched missiles was developed under Contract F04611-71-C-0013 by the Thiokol Chemical Corporation, Wasatch Division, Brigham City, Utah. The program was started on 1 October 1970 and completed on 1 September 1972. The Air Force Project Monitor was Lt Louis Fox, MKCD.

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13. ABSTRACT

UNCLASSIFIED ABSTRACT

Summary
This final report documents work accomplished under contract F04611-71-C-0013. The program discussion describes the intent and capabilities of the computer program which was developed to (1) evaluate preliminary duty cycles for missile systems, (2) develop specifications for the control system being employed, (3) perform preliminary design analysis on any of the control options, and (4) predict the performance capability of a vehicle utilizing the control system characteristics obtained from the program. The seven potential control inputs are liquid injection thrust vector control, hot gas thrust vector control, gimbal ring, ball and socket, flexible seal, jet tabs, and aerodynamic surfaces. The program has the capability to determine the thrust magnitude required to fly any one of the six types of trajectories where thrust vector and thrust magnitude control is required. The nozzle design capability includes two types of fixed nozzles and five types of movable nozzles. The program also incorporates design capability for pintle nozzle single chamber thrust magnitude control with or without thrust vector control. Two material options are available for case design, metal and filament wound glass. A three dimensional six degrees of freedom trajectory routine is available in the program.

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SECTION I

PROGRAM SUMMARY

The preliminary design and evaluation of a thrust vector control (TVC) system previously required the expenditure of considerable effort and time over a period of months.

To alleviate this situation, the Rocket Propulsion Laboratory, Edwards Air Force Base, California, funded the first TVC design program, under Contract AF 04(611)-9720, which was completed by Thiokol in 1964. Subsequent changes in state-of-the-art and a need to expand this capability led to the program entitled "Advanced Thrust Vector Control Preliminary Design Program" developed under Contract AF 04(611)-11647. The program resulting from this contract is described in the "Final Report, Advanced Thrust Vector Control Preliminary Design Computer Program," January 1968, designated Technical Report AFRPL-TR-67-318. Subsequent further changes in the state-of-the-art and the need to expand the TVC design capability to provide advanced steering and thrust magnitude control (ASC/TMC) led to the program described in this report. This additional capability was accomplished through additions and modifications to the previously developed Advanced TVC Preliminary Design Computer Program. The major additions to this program are:

1. Capability to determine the thrust magnitude required to fly any one of six types of trajectories where thrust vector and thrust magnitude control is required; and
2. Design capability for a pintle nozzle single chamber thrust magnitude control concept with or without TVC.

Additionally, data permanently stored within the computer program have been improved and equations have been updated for use in the current sub-routines for the design and performance prediction functions. Changes have been made to improve basic accuracy and to extend the range applicability of the design models to include nozzle designs with throat diameters ranging from 0.5 to 100 inches. Included in the models updated are the nozzle, torque and actuation subroutines.

The program also has been modified to improve its efficiency through allowing more flexibility in performing multiple runs, minimizing program input requirements, and improving capability for debugging program input through the use of computer print flags.

A three-dimensional, six degrees of freedom trajectory routine is available in this computer program. Included is the capability to simulate a linear control system using either input or internally calculated control system gains. An associated optimization procedure for flight path shaping is included. The complete discussion of the trajectory routine is contained in subsequent sections of this book. The nozzle design capability provided in this computer program represents comprehensive design calculations for two types of fixed nozzles and five types of movable nozzles: submerged fixed; external fixed; subsonic splitline, hinged, integral, submerged inlet supersonic splitline; and external inlet supersonic splitline. The exit cone design can be either conical or contoured. The output from the nozzle subroutine includes nozzle dimensional characteristics, nozzle performance parameters, and nozzle mass properties information.

Additionally, a pintle nozzle subroutine has been added which is capable of designing a movable pintle for nozzle throat area control. This subroutine has been so designed and integrated that a pintle can be incorporated in any of the nozzle types in which this feature is practical. These types are the subsonic splitline, external fixed hinged, integral and external entry supersonic splitline.

The pintle nozzle subroutine generally applies to the nozzle designs

incorporating an external inlet (convergent cone), rather than for those with submerged inlets. In addition, provision has been made to design a pintle for use with integral nozzles which have gimbal ring or flexible seal TVC.

The incorporation of a pintle does not affect the incorporation of TVC in any of these designs. The program includes an election of the preferred material. For throats less than 10 in. in diameter, tungsten is the preferred material. Solid tungsten pintles are designed for throat diameters less than 2 in. in diameter, while tungsten shell pintles are designed for throat diameters between 2 and 10 inches. Ablatives are preferred for pintles larger than 10 in. in diameter. The full range of insulation and structural materials is included in the nozzle routine for the remaining pintle components. Thermal sizing is accomplished with the insulation design section; structural sizing is part of the pintle subroutine. Provision for area balancing of the pintles is incorporated. The pintle will be supported by insulated struts with the number to vary from two to six.

The pintle will be hydraulically actuated by a single, double-acting actuator for small sized and an optional annular actuator for the larger pintles. Fluid is supplied and returned through the passages in the struts. The actuation auxiliary power unit is sized in the actuation and roll control subroutine.

The computer program includes capability for simulation of a non-programmed thrust profile. Thrust control systems simulated are either a perfect system (i.e., achieved thrust equals commanded thrust), or a pintle controller network. The pintle controller commands the time rate change of throat area from a control law consisting of a chamber pressure error with time rate change feedback. Thrust control modes incorporated include: specific velocity-time profile, axial acceleration proportional to line of sight rates, constant Mach number, thrust proportional to commanded turning rates, minimum velocity

during a commanded turn, and dynamic pressure constraints.

The pintle nozzle TMC portion of the program defines performance, structure, insulation, actuation, and system components for both fixed and movable nozzles.

The thrust control system logic used in the trajectory simulation is broken into two separate parts: (1) the command thrust logic, and (2) the controllable motor thrust dynamics. The command thrust logic, or thrust control law chosen, will provide the needed thrust command for the motor to enable the missile system to achieve the desired trajectory condition. The criteria for evaluating the commanded thrust is established by flight performance parameters such as specified velocity history, stipulated Mach number, commanded turning rates, minimum velocity or constrained dynamic pressure.

This final report is organized into three basic volumes:

- I Program Description
- II User's Manual
- III Test Cases

Volume I contains a summary of equations used in formulating the mathematical models used in the program. This volume contains two major books: Book 1 - Requirements, and Book 2 - Hardware. The trajectory documentation is included as a separate section in Book 1, as are the aerodynamic coefficients and the roll control requirements. Book 2 of Volume I includes a complete description of the hardware and component design routines and theory.

In Volume II - User's Manual, instructions for use of the program are given; however, the input portion of the trajectory program write-up is also needed for reference by the user.

Sample test cases are contained in Volume III. The description of each

test case is given, along with a listing of the computer input card deck and a reproduction of the complete computer output.

References to the source of the material used in developing this program are included in the particular sections to which they apply.

SECTION II

AERODYNAMIC COEFFICIENTS

The subroutines contained in this section provide the capability of determining the forces and moments generated on a missile by the flow of air over the external surface of an airborne vehicle. The approach used was to separate the forces and moments into two groups: those produced on the missile body (payload, motors, interstages, etc.), and those produced on the lifting surfaces (canards, fins).

The forces are represented by the nondimensional lift coefficient, C_{Nz} for bodies, $C_{L\alpha}$ and $C_{L\delta}$ for canards and fins, and the drag coefficients, C_A for bodies, and C_{D0} and C_{DL} for canards and fins. The moments are determined from the forces and the point of application, referred to as centers of pressure. The coefficients are calculated at the Mach numbers listed in Table 1.

Included in the subroutine generated for lifting surfaces is the capability of calculating a weight estimate of the surfaces and the location of their longitudinal and lateral center-of-gravity.

A. BODY AXIAL FORCE COEFFICIENT

This subsection presents the method used for calculating the aerodynamic axial force coefficient of a body of revolution in axial flow which is composed of cones, cone-frustums, and cylindrical sections.

The total aerodynamic axial force of a body is composed of three separate components: forebody pressure forces, viscous forces (skin friction), and the base pressure forces. The axial force coefficient for each of these forces must be calculated separately.

TABLE 1
STORED MACH NUMBER TABLES

| <u>First Stage Mach No.</u> | <u>Upper Stage Mach No.</u> |
|---------------------------------|---------------------------------|
| 0.00 | 1.25 |
| 0.50 | 1.50 |
| 0.75 | 2.00 |
| 0.95 | 2.60 |
| 1.00 | 3.00 |
| 1.25 | 4.00 |
| 1.50 | 5.00 |
| 2.00 | 6.00 |
| 2.60 | 8.00 |
| 3.00 | 10.00 |
| 4.00 | |
| 5.00 | |
| 6.00 | |
| 8.00 | |
| 10.00 | |

1. FOREBODY PRESSURE FORCES

$$C_{AFB} = C_{P_{FB}} \frac{D_2^2 - D_1^2}{D_{ref}^2} \quad (1)$$

$$\begin{aligned} C_{P_{FB}} &= C_{P_1} + C_{P_2} \\ &= 2.1 \sin^2 \sigma + \frac{\sin \sigma}{2 \sqrt{M^2 - 1}} \end{aligned} \quad (2)$$

The forebody axial force coefficient is calculated separately for each section of the body, which is either a cone or cone frustum. Where the first section of a body is a blunted cone and the equivalent nose radius is less than 20 percent of the cone base radius, the section can be considered as a pointed cone. The axial force coefficient, C_{AFB} , is calculated for $M = 3.0$; the value at $M = 3.0$ is multiplied by the factor K_{FB} shown in Table 2. Thus,

$$(C_{AFB})_M = 2.0 = (K_{FB})_M = 2.0 \quad (C_{AFB})_M = 3.0 \quad (3)$$

and so on for values of $M < 3.0$.

The pressure coefficient $C_{P_{FB}}$ is calculated using Equation 2.

2. VISCOUS FORCES (SKIN FRICTION)

$$C_{AF} = C_F \frac{A_{wet}}{S_{ref}} \quad (4)$$

The axial force coefficient due to the viscous effects of the fluid is a function of Reynold's No., Mach No., and the surface area in contact with the fluid. Typical values of Reynold's No. per foot vs Mach No. are provided in Table 3 for a small ballistic missile, a larger ballistic missile, a large booster type vehicle, and a small air launched missile. To determine the flat plate coefficient, C_F , Reynold's No. vs Mach No. must be calculated in the following manner. Using Table 3, R_N/ft is determined

TABLE 2

SUBSONIC AND TRANSONIC FOREBODY
PRESSURE DRAG COEFFICIENT (K_{FB})

| <u>Mach No.</u> | <u>K_{FB}</u> |
|-----------------|----------------------------|
| 0.00 | 0.36 |
| 0.50 | 0.36 |
| 0.75 | 0.53 |
| 0.95 | 1.00 |
| 1.00 | 1.24 |
| 1.25 | 1.71 |
| 1.50 | 1.58 |
| 2.00 | 1.31 |
| 2.60 | 1.09 |
| 3.00 | 1.00 |
| 3.00 | 1.00 |
| 3.00 | 1.00 |
| 3.00 | 1.00 |
| 3.00 | 1.00 |

TABLE 3

VARIATION OF REYNOLD'S NUMBER PER FOOT
VS MACH NUMBER

| Mach No. | $(R_N/\text{ft}) 10^{-6}^*$ | | | |
|-------------|-----------------------------|------|------|--------|
| | (1) | (2) | (3) | (4) |
| 0.00 | 3.70 | 3.30 | 3.55 | 1.976 |
| 0.50 | 3.70 | 3.30 | 3.55 | 1.976 |
| 0.75 | 5.25 | 4.62 | 4.68 | 2.964 |
| 0.95 | 6.25 | 5.55 | 5.45 | 3.754 |
| 1.00 | 6.50 | 5.77 | 5.55 | 3.952 |
| 1.25 | 7.47 | 6.57 | 6.21 | 4.940 |
| 1.50 | 8.22 | 7.13 | 6.75 | 5.928 |
| 2.00 | 9.02 | 7.87 | 7.40 | 7.904 |
| 2.60 | 9.20 | 8.21 | 7.50 | 10.275 |
| 3.00 | 8.90 | 8.15 | 7.04 | 11.856 |
| 4.00 | 7.00 | 6.70 | 4.52 | 15.808 |
| 5.00 | 4.75 | 4.85 | 2.62 | 19.760 |
| 6.00 | 3.10 | 2.40 | 1.44 | 23.712 |
| 8.00 | 1.05 | 1.18 | 0.48 | 31.616 |
| 10.00 | 0.45 | 0.42 | 0.36 | 39.520 |

- * (1) Small ballistic missile
 (2) Large ballistic missile
 (3) Large booster vehicle
 (4) Small air launched missile

at a particular Mach number. Then $R_N = R_{11}/ft \times L$, where L is the length of the missile in feet from the nose to the end of the aft skirt. Knowing R_N and Mach No., the appropriate value of C_F can be calculated using Eq 5.

$$C_F = \left[\frac{0.445}{(\log_{10} R_N)^{2.58}} \right] \left[(1 + 0.162 M^2)^{-0.58} \right] \quad (5)$$

The parameter A_{wet} is the total surface area of the missile excluding the base area. Total wetted area is the sum of the wetted area of the parts; therefore,

$$A_{wet} = A_{wet\ cone} + A_{wet\ cone-frustums} + A_{wet\ cylinders} \quad (6)$$

C_{AF} then can be calculated using Eq 4.

3. BASE PRESSURE FORCES

$$C_{AB} = -C_{PB} \frac{A_{base}}{S_{ref}} \quad (7)$$

Base pressure coefficient, C_{PB} , vs Mach No. is given in Table 4. The effective base area, A_{base} , is considered equal to one-half the difference between the base area of the missile and the total nozzle exit area. Using Eq 7, C_{AB} then is calculated.

4. TOTAL AXIAL FORCE COEFFICIENT

Total axial force coefficient is as shown in Eq 8.

$$C_A = C_{AFB} + C_{AF} + C_{AB} \quad (8)$$

5. NOMENCLATURE

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|--|--------------|
| D_2 | Largest diameter of a frustum of a cone | in. |
| D_1 | Smallest diameter of a frustum of a cone | in. |

TABLE 4

BASE PRESSURE COEFFICIENT (C_{PB})

| First Stage | | Upper Stages | |
|-------------|----------------------------|--------------|----------------------------|
| <u>M</u> | <u>C_{PB}</u> | <u>M</u> | <u>C_{PB}</u> |
| 0.00 | -0.800 | 1.25 | -0.289 |
| 0.50 | -0.483 | 1.50 | -0.206 |
| 0.75 | -0.417 | 2.00 | -0.152 |
| 0.95 | -0.486 | 2.60 | -0.116 |
| 1.00 | -0.516 | 3.00 | -0.098 |
| 1.25 | -0.289 | 4.00 | -0.067 |
| 1.50 | -0.206 | 5.00 | -0.047 |
| 2.00 | -0.152 | 6.00 | -0.032 |
| 2.60 | -0.116 | 8.00 | -0.013 |
| 3.00 | -0.098 | 10.00 | -0.000 |
| 4.00 | -0.067 | | |
| 5.00 | -0.047 | | |
| 6.00 | -0.032 | | |
| 8.00 | -0.013 | | |
| 10.00 | -0.000 | | |

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|--|--------------|
| σ | Semivertex angle of a cone or frustum of a cone | deg |
| K_{PB} | Subsonic and transonic forebody pressure drag factor | dim. |
| C_{AFB} | Forebody axial force coefficient due to pressure | dim. |
| C_{PFB} | Forebody pressure coefficient $\left(C_p = \frac{p - p_a}{q}\right)$ | dim. |
| p | Pressure on local surface | lb/sq ft |
| p_a | Ambient pressure | lb/sq ft |
| q | Dynamic pressure | lb/sq ft |
| D_{ref} | Reference diameter (usually taken as diameter of largest motor) | ft |
| C_{AF} | Axial force coefficient due to viscous forces | dim. |
| R_N | Reynold's No. $\left(R_N = \frac{\rho V L}{\mu} = \frac{V L}{\nu}\right)$ | dim. |
| ρ | Density of air | slug/cu ft |
| V | Velocity | ft/sec |
| L | Characteristic length (length of missile) | ft |
| μ | Viscosity of air | slug/ft sec |
| ν | Kinematic viscosity of air, ρ/μ | sq ft/sec |
| C_F | Flat plate skin friction coefficient | dim. |
| A_{wet} | Missile wetted area (surface area in contact with the air) | sq ft |
| S_{ref} | Reference area $\left(\frac{\pi D_{ref}^2}{4}\right)$ | sq ft |
| C_{AB} | Axial force coefficient due to base pressure | dim. |
| C_{PB} | Base pressure coefficient $\left(C_{PB} = \frac{p_B - p_a}{q}\right)$ | dim. |
| p_B | Base pressure | lb/sq ft |
| A_{base} | Effective base area of missile ($A_{base} = \frac{1}{4}$ (cross-sectional area of motor base minus nozzle exit area)) | sq ft |

B. BODY SUBSONIC-TRANSONIC NORMAL FORCE COEF

This subroutine is used to calculate the initial slope of the normal force coefficient vs angle of attack and the longitudinal position of the normal force coefficient center of pressure over the subsonic-transonic range of Mach numbers. The method used is applicable to bodies of revolution which are composed of conical sections (cones and cone frustums) and cylinders, such as are encountered with most ballistic missile configurations. One restraint must be applied to conical sections: the slope of these sections must be forward facing (no boat-tail sections) at zero angle of attack.

This procedure for determining C_{N_α} and x_{cp} for the subsonic-transonic Mach No. range is limited to the Mach No. range of $M = 0$ to $M = 2.0$.

1. NORMAL FORCE COEFFICIENT SLOPE

The initial slope of the curve of normal force coefficient, C_N , versus angle of attack, α , is defined in this procedure by the following equation.

$$C_{N\alpha} = \left(\frac{dC_N}{d\alpha} \right)_{\alpha=0^\circ} = K_N \left[\frac{A_B}{S} \sin 2\alpha \cos \alpha/2 + \eta C_{dc} A_P/S \sin^2 \alpha \right] \quad (1)$$

where $\alpha = 1^\circ$.

$$\text{Therefore; } C_{N\alpha} = K_N [.0349 A_B/S + .00031 \eta C_{dc} A_P/S] \quad (2)$$

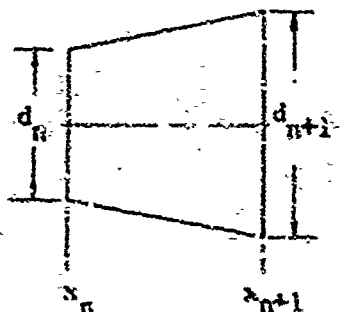
$$= .0349 K_N A_B/S + .00031 K_N C_{dc} \eta A_P/S \quad (2a)$$

$$= K_1 A_B/S + K_2 \eta A_P/S \quad (2b)$$

The factors K_1 and K_2 are functions of Mach number only and are provided in Figures 1 and 2. The factors S_{ref} , A_B , and A_P , and η are functions of body geometry and are defined below.

| | |
|-----------|---|
| S_{REF} | Cross-sectional area of the first stage motor cylindrical section ($S = \frac{\pi}{4} d_{cyl}^2$) and is the reference area on which C_N is based. (ft ²) |
| A_B | Cross-sectional area of the largest cylindrical section if there is no conical frustum on the aft end of the vehicle. If there is a conical frustum on the aft end of the vehicle, A_B is equal to the cross-sectional area of the conical frustum at the point of its largest diameter. (ft ²) |
| A_P | Planform area of the total vehicle which is the lateral projected area of the body. As the vehicle will be composed of cones, conical frustums, and cylinders, the areas of these sections are as follows: (ft ²) |

Cones and Conical Frustums



$$\Delta A_P = \left(\frac{d_n + d_{n+1}}{2} \right) (x_{n+1} - x_n) \quad (3)$$

NOTE: For a cone $d_n = 0$

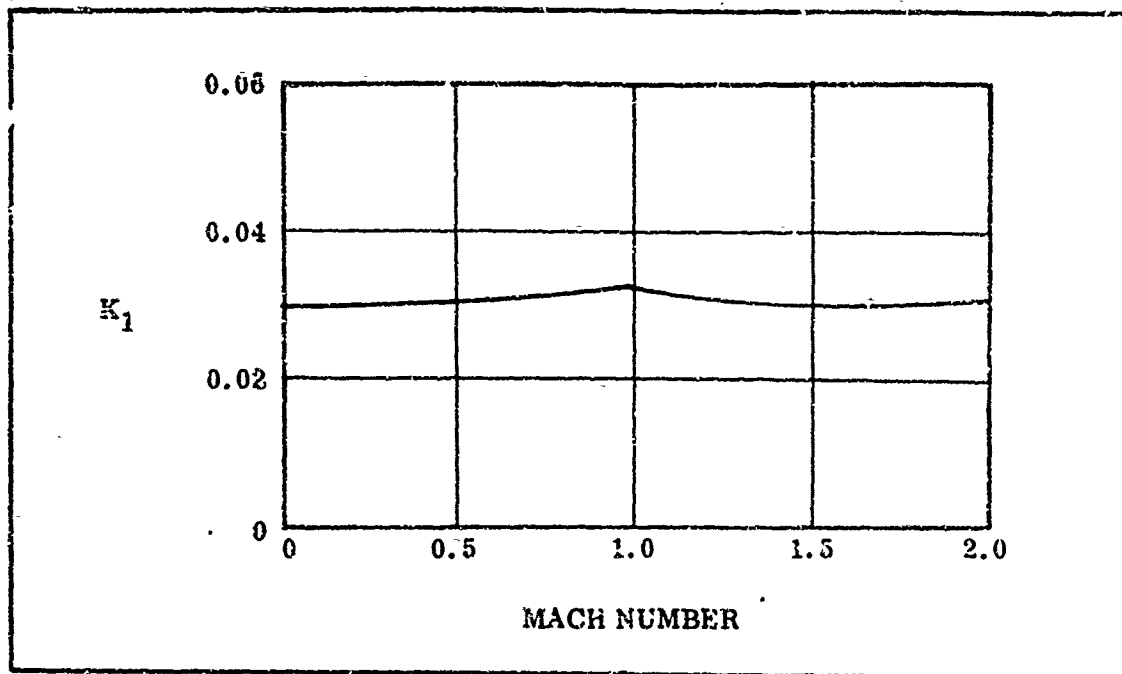


Figure 1. Subsonic-Transonic Normal Force Parameter K_1

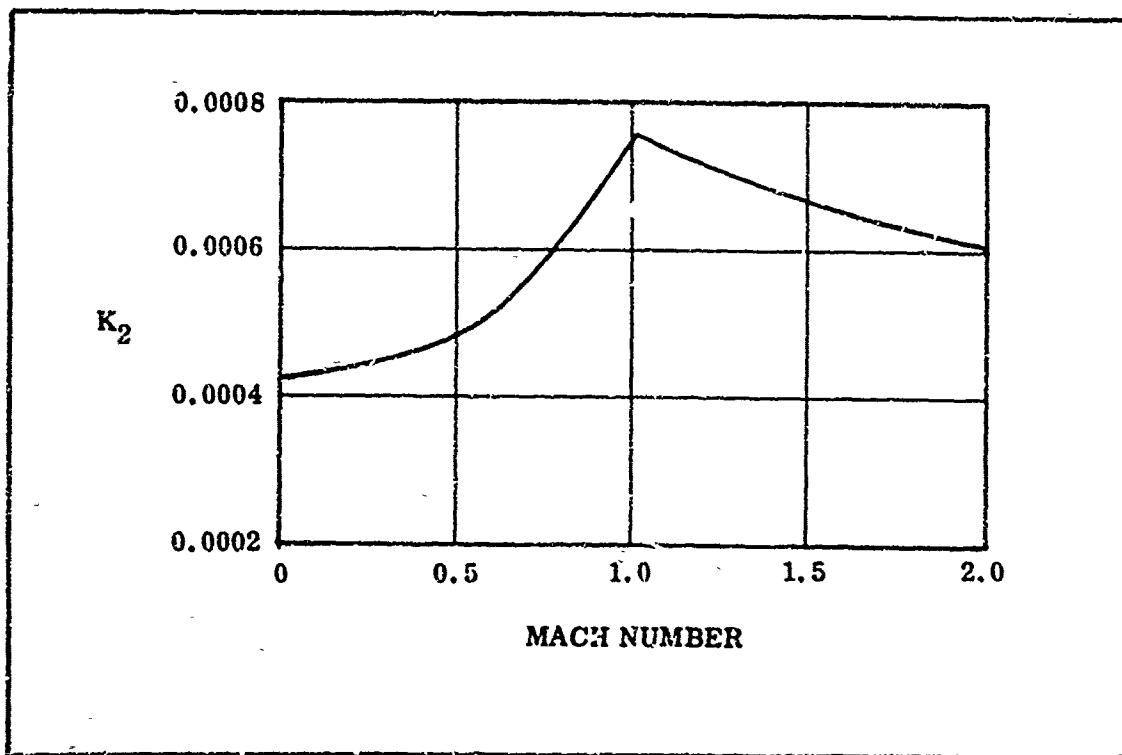
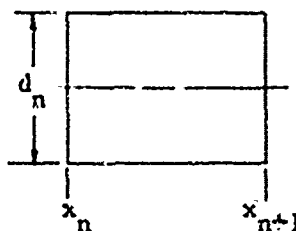


Figure 2. Subsonic-Transonic Normal Force Parameter K_2

Cylinder



$$\Delta A_P = d_n (x_{n+1} - x_n) \quad (4)$$

Therefore:

$$A_P = \Sigma \Delta A_{P_{\text{cones}}} + \Sigma \Delta A_{P_{\text{conical frustum}}} + \Sigma \Delta A_{P_{\text{cylinder}}}$$

L/d Total body fineness ratio where L is the length of the body, and d is the diameter of the largest cylindrical section. (nondimensional)

η Factor which is a function of total body fineness ratio. (Figure 3) (nondimensional)

K_1, K_2 Constants which are a function of Mach number. (Figures 1 and 2) (nondimensional)

2. NORMAL FORCE CENTER OF PRESSURE

The normal force center of pressure, x_{cp} , as defined in this procedure, is the location of a point, measured from the nose reference station of the vehicle, at which the total normal force acting on the body could be placed to produce the same moment about the body nose reference station as would the distributed normal force.

The following equation is used to calculate this parameter:

$$x_{cp} = x_1 - \frac{K_x}{C_{N\alpha}} \left\{ .4188 \left[\frac{Q - A_B L}{S_{ref}} \right] - .00366 x_c \eta C_{d_c} A_P / S_{ref} \right\} \quad (5)$$

$$= x_1 - \frac{1}{C_{N\alpha}} \left\{ .4188 K_x \left[\frac{Q - A_B L}{S_{ref}} \right] - .00366 K_x C_{d_c} x_c \eta A_P / S_{ref} \right\} \quad (5a)$$

$$= x_1 - \frac{1}{C_{N\alpha}} \left\{ K_3 \left[\frac{Q - A_B L}{S_{ref}} \right] - K_4 x_c \eta A_P / S_{ref} \right\} \quad (\text{inches}) \quad (5b)$$

The parameters A_B , S_{ref} , η , L , A_P , and $C_{N\alpha}$ are the same as defined for the purpose of calculating the slope of the normal force coefficient, $C_{N\alpha}$. The factors K_3 and K_4 are a function of Mach number and are provided in Figures 4 and 5, while Q and x_c are functions of body geometry and are defined as follows:

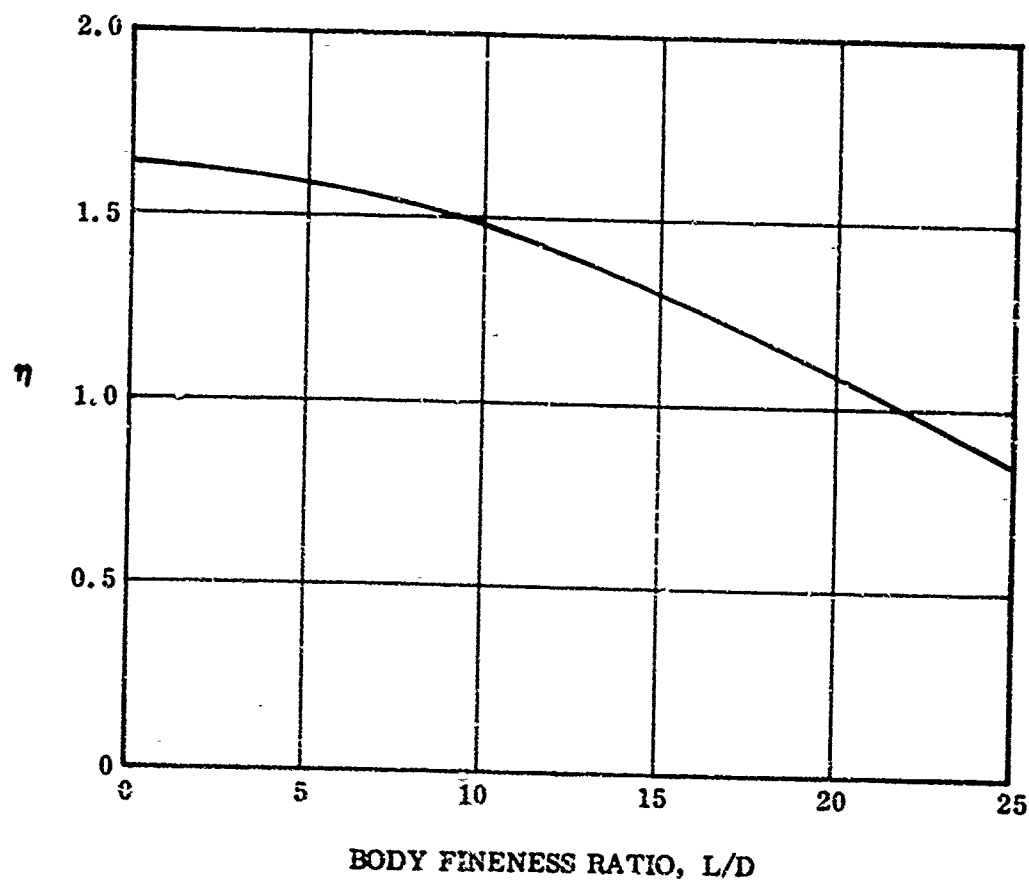


Figure 3. Subsonic-Transonic Normal Force Parameter η

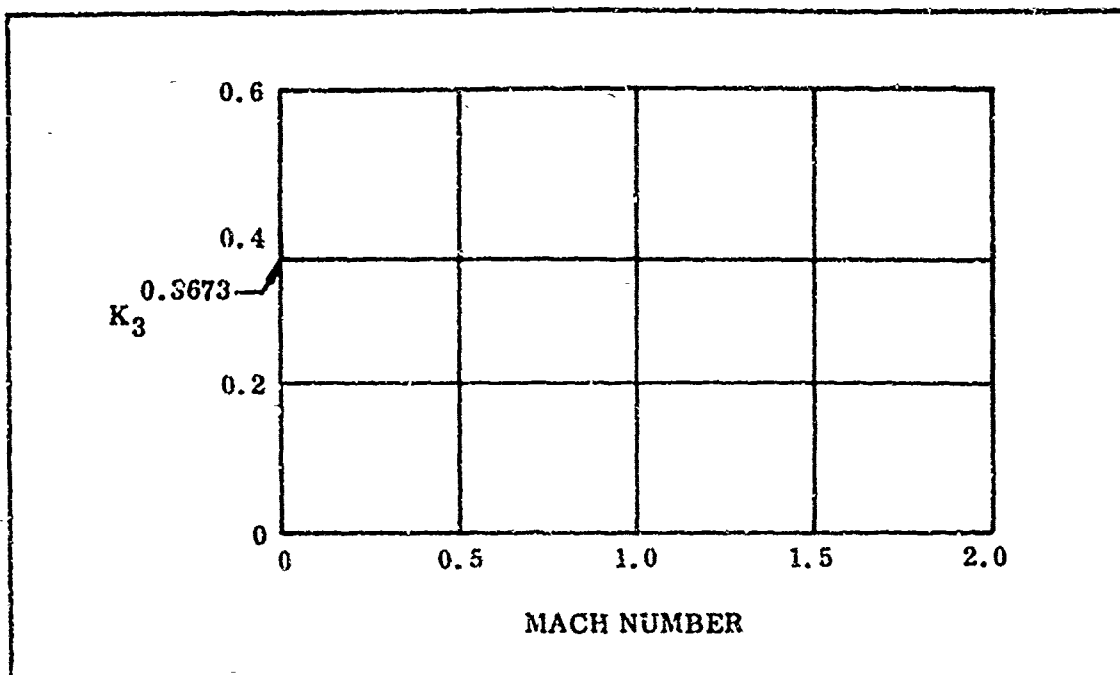


Figure 4. Subsonic-Transonic Center of Pressure Parameter K_3

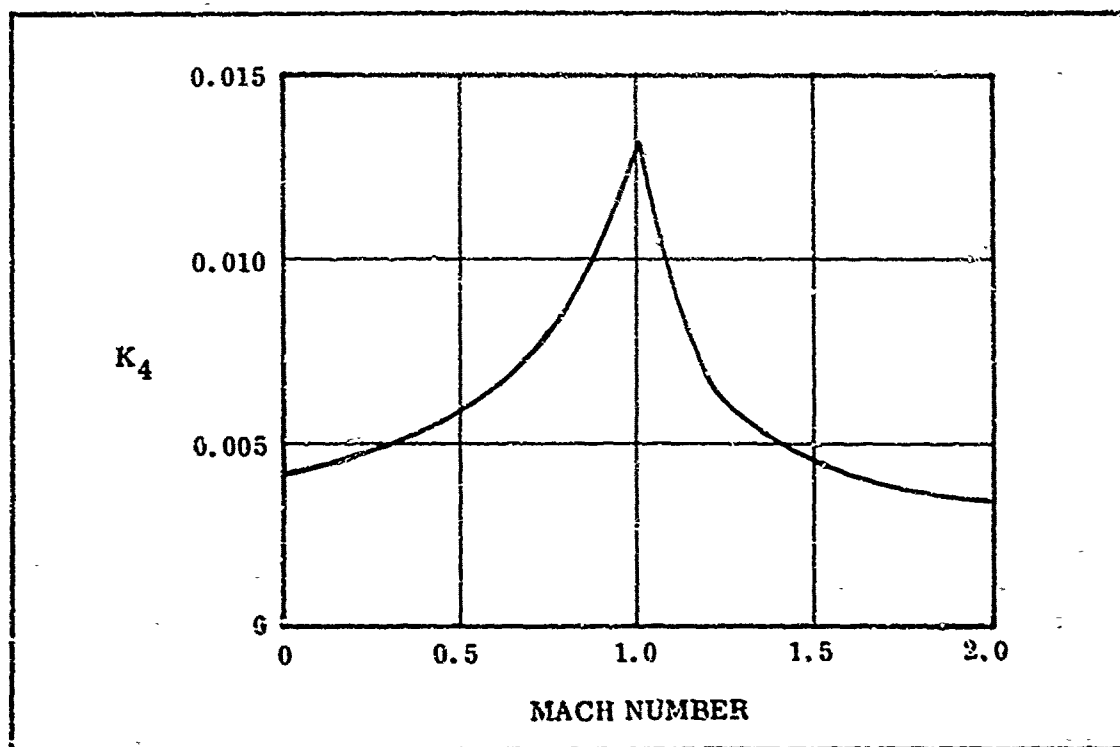
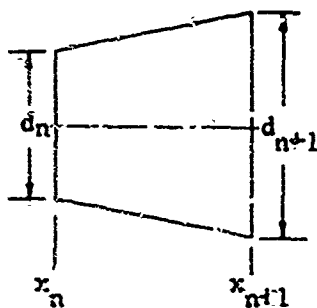


Figure 5. Subsonic-Transonic Center of Pressure Parameter K_4

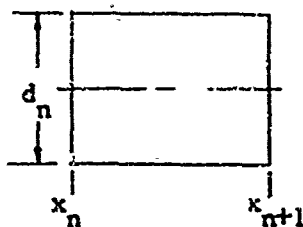
Centroid of Cones and Frustums



$$\bar{x} = x_n + (x_{n+1} - x_n) \left[\frac{3(d_n/2) + 2[(d_{n+1}/2) - (d_n/2)]}{6(d_n/2) + 3[(d_{n+1}/2) - (d_n/2)]} \right] \quad (6)$$

NOTE: For a cone $d_n = 0$

Centroid of Cylinder

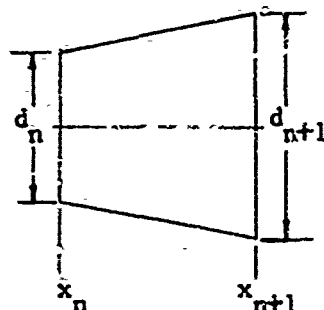


$$\bar{x} = x_n + \left(\frac{x_{n+1} - x_n}{2} \right) \quad (7)$$

Q

Body volume of the total vehicle (Figure 6). The equations to be used to calculate the volumes of the cones, conical frustums, and cylinders are as follows: (ft³)

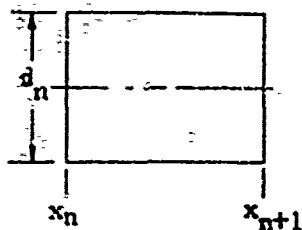
Cones and Conical Frustums



$$\Delta Q = \pi \left(\frac{x_{n+1} - x_n}{3} \right) \left[\left(\frac{d_n}{2} \right)^2 + \left(\frac{d_n}{2} \right) \left(\frac{d_{n+1}}{2} \right) + \left(\frac{d_{n+1}}{2} \right)^2 \right] \quad (8)$$

NOTE: For A cone $d_n = 0$

Cylinder



$$\Delta Q = \pi \left(\frac{d_{n+1}}{2} \right)^2 (x_{n+1} - x_n) \quad (9)$$

Therefore

$$Q = \Sigma \Delta Q_{\text{cones}} + \Sigma \Delta Q_{\text{conical frustum}} + \Sigma \Delta Q_{\text{cylinder}}$$

L

Length of vehicle (ft)

x_c

Centroid of the total planform area measured from the body nose along the body longitudinal axis. (ft)

$$x_c = \frac{\Sigma \text{Moment of Area}}{\Sigma \text{Area}} = \frac{\Sigma \Delta A \bar{x}}{\Sigma \Delta A} - x_1 \quad (10)$$

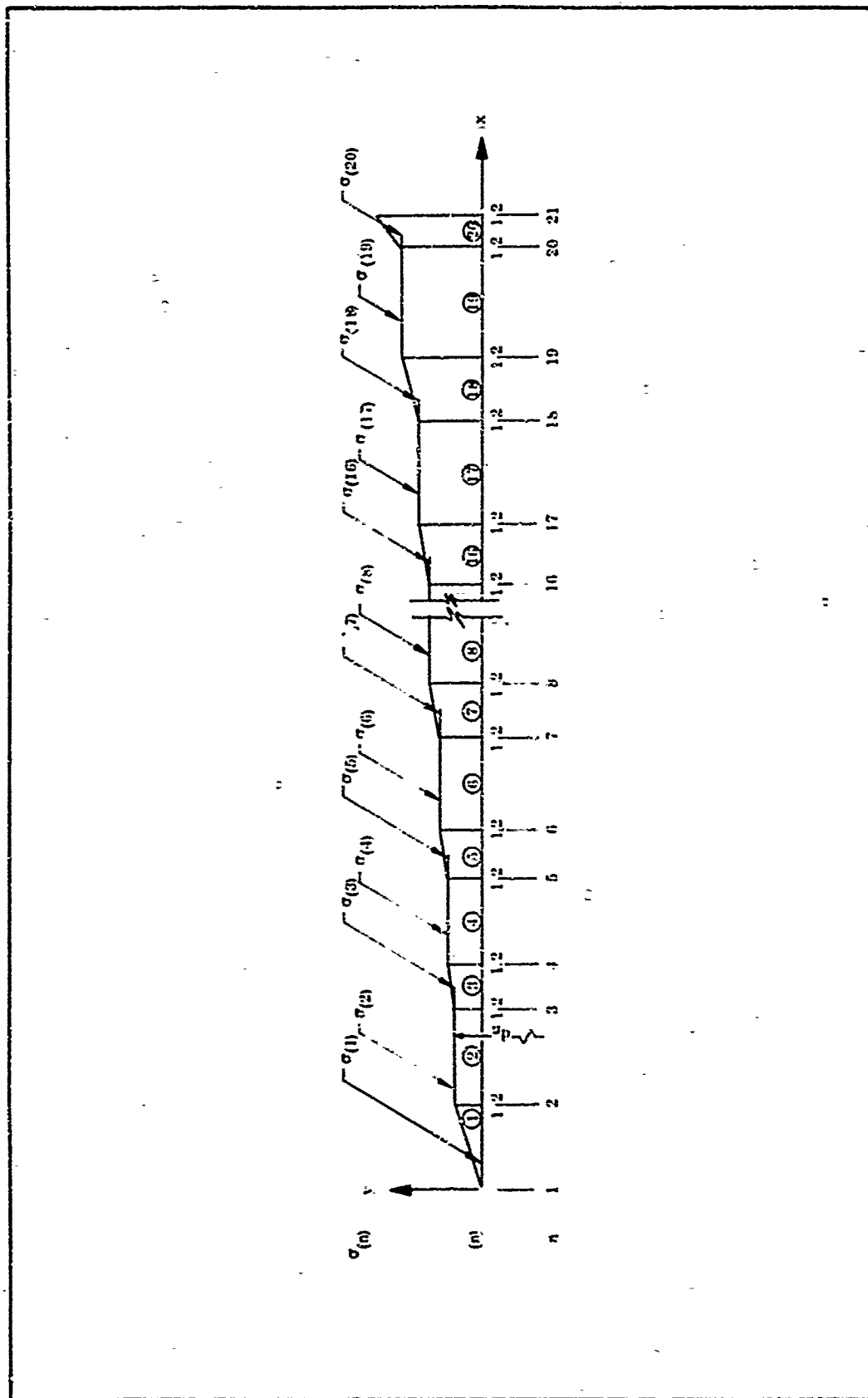


Figure 6. Body Description

C. BODY SUPERSONIC NORMAL FORCE COEFFICIENT

The method described herein has been generated for the purpose of calculating the slope of the normal force coefficient, $C_{N\alpha}$, the normal force center of pressure, x_{cp} , and the normal force loading distribution, $dC_{N\alpha}/dx$, for a pointed nose body of revolution near zero angle of attack in supersonic air flow. The Mach number range for this method is considered to be from 2.60 to 10. This method is based on second-order shock expansion theory as presented in reference 1* and an extension of the method derived in reference 2*.

Though the current approach was intended to produce a means of calculating values of the above parameters for a body of revolution composed of conical and cylindrical sections, bodies with curved profiles can be accommodated by approximating curved sections with straight line sections.

1. NORMAL FORCE COEFFICIENT SLOPE, $C_{N\alpha}$

Beginning with the standard definition for the normal force coefficient, C_N , we have

$$C_N = \frac{N}{q S_{ref}} \quad (1)$$

$$= \frac{N}{\frac{\gamma}{2} P_\infty M_\infty^2 S_{ref}} \quad (1a)$$

$$= \frac{2}{\frac{\gamma}{2} P_\infty M_\infty^2 S_{ref}} \int_0^l \int_0^\pi P r \cos \varphi d\varphi dx \quad (1b)$$

$$= \frac{4}{\gamma P_\infty M_\infty^2 S_{ref}} \int_0^l \int_0^\pi P r \cos \varphi d\varphi dx \quad (1c)$$

As the slope of the normal force coefficient is desired, the equation for C_N is differentiated with respect to angle of attack, α . Thus

$$C_{N\alpha} = \frac{dC_N}{d\alpha} = \frac{4}{\gamma P_\infty M_\infty^2 S_{ref}} \int_0^l \int_0^\pi \frac{dP}{d\alpha} r \cos \varphi d\varphi dx \quad (2)$$

*These references are listed in Table 5.

TABLE 5

REFERENCES

1. Syvertson, C. A. and Dennis, D. H.: A Second-Order Shock-Expansion Method Applicable to Bodies of Revolution Near Zero Lift. NACA TR-1328.
2. Capioux, R.: An Extension of Second-Order Shock-Expansion Theory. LMSD 48381, Lockheed Aircraft Corporation.
3. Blick, E. F.: "Similarity Rule Estimation Methods for [&]Cones," AIAA Journal. Volume 1, Number 10, 2,415-2,416, 1963.
4. Linnell, R. D. and Bailey, J. Z.: "Similarity-Rule Estimation Methods for Cones and Parabolic Noses," Journal Aeronautical Sciences. 23, 796-797 (1956).
5. Sims, J. L.: Tables for Supersonic Flow Around Right Circular Cones at Small Angle of Attack. NASA SP-3007.

Now defining Λ as the non-dimensional loading on a chin disk, the equation for Λ is

$$\Lambda = \frac{2}{\gamma P_{\infty} M_{\infty}^2 \pi} \int_0^{\pi} \frac{dP}{d\alpha} \cos \varphi d\varphi \quad (3)$$

and the equation for $C_{N\alpha}$, after substitution, becomes

$$C_{N\alpha} = \frac{2\pi}{A_B} \int_0^l \Lambda r dx \quad (4)$$

where $A_B = \pi r_i^2$ and r_i is the radius at the base of the body section for which $C_{N\alpha}$ is being calculated.

The basic problem at this point is to define the loading parameter, Λ , for each section of the body. As shown by equation (3), to define Λ it is necessary to define $\frac{dP}{d\alpha}$. In reference i, the pressure at any point on the body is defined as

$$P = P_c - (P_c - P_2) e^{-\eta} \quad (5)$$

$$= (1 - e^{-\eta}) P_c + e^{-\eta} P_2 \quad (5a)$$

Differentiating with respect to angle of attack, α , gives

$$\frac{dP}{d\alpha} = (1 - e^{-\eta}) \frac{dP_c}{d\alpha} + e^{-\eta} \left[\frac{dP_2}{d\alpha} \right] \quad (6)$$

where

$$\eta = \left(\frac{\partial P_2}{\partial s} \right) \frac{x - x_2}{(P_c - P_2) \cos \sigma_2} \quad (7)$$

Referring to equations (3) and (6), we can define Λ as

$$\Lambda = \Lambda_a + \Lambda_b \quad (8)$$

where

$$\Lambda_a = \frac{2}{\gamma P_\infty M_\infty^2 \pi} \int_0^\pi (1 - e^{-\eta}) \frac{dP_c}{d\alpha} \cos \varphi d\varphi \quad (9)$$

$$= (1 - e^{-\eta}) \tan \sigma C_{N\alpha_{TC}} \quad (9a)$$

and

$$\Lambda_b = \frac{2}{\gamma P_\infty M_\infty^2 \pi} \int_0^\pi e^{-\eta} \frac{dP_2}{d\alpha} \cos \varphi d\varphi \quad (10)$$

$$= e^{-\eta} \Gamma \quad (10a)$$

where

$$\Gamma = \frac{2}{\gamma P_\infty M_\infty^2 \pi} \int_0^\pi \frac{dP_2}{d\alpha} \cos \varphi d\varphi \quad (11)$$

Thus

$$\Lambda = (1 - e^{-\eta}) \tan \sigma C_{N\alpha_{TC}} + e^{-\eta} \Gamma \quad (12)$$

with

$$\Lambda = \Lambda_a + \Lambda_b \quad (8)$$

then

$$C_{N\alpha} = C_{N\alpha_a} + C_{N\alpha_b} \quad (13)$$

and the value of $C_{N\alpha}$ for each body section can be calculated in two increments:

$$C_{N\alpha_a} = \frac{2\pi}{A_B} \int_0^l (1 - e^{-\eta}) \tan \sigma C_{N\alpha_{TC}} r dx \quad (14)$$

and

$$C_{N\alpha_b} = \frac{2\pi}{A_B} \int_0^l e^{-\eta} \Gamma r dx \quad (15)$$

Two parameters now remain to be defined, $(\partial P / \partial S)_2$ in equation (7) and $dP_2/d\alpha$ in equation (11). Each must be defined separately for convex corners and concave corners.

A convex corner, as used herein, is defined as a corner for which the section downstream of the corner has an angle σ which is smaller than the angle σ of the section upstream of the corner. It follows then that a concave corner is one where the angle σ of the downstream section is larger than the angle σ of the upstream section.

The definitions of $(\partial P / \partial S)_2$, which are contained in reference 1, for convex and concave corners will be used in this method. They are, with substitution of symbols:

Convex Corner

$$\left(\frac{\partial P}{\partial S}\right)_2 = \frac{b_2}{r} \left(\frac{\Omega_1}{\Omega_2} \sin \sigma_1 - \sin \sigma_2 \right) + \frac{b_2}{b_1} \frac{\Omega_1}{\Omega_2} \left(\frac{\partial P}{\partial S}\right)_1 \quad (16)$$

where

$$b = \frac{\gamma P M^2}{2(M^2 - 1)} \quad (17)$$

$$\Omega = \frac{1}{M} \left[\frac{1 + \left(\frac{\gamma - 1}{2} \right) M^2}{\frac{\gamma + 1}{2}} \right]^{\frac{\gamma + 1}{2(\gamma - 1)}} \quad (18)$$

$$\left(\frac{\partial P}{\partial S} \right)_1 = \left(\frac{\partial P}{\partial S} \right)_3 = \left(\frac{P_c - P_2}{P_c - P_1} \right) \left(\frac{\partial P}{\partial S} \right)_2 \quad (19)$$

$$= e^{-\eta_3} \left(\frac{\partial P}{\partial S} \right)_2 \quad (19a)$$

Concave Corner

$$\begin{aligned} \left(\frac{\partial P}{\partial S} \right)_2 &= \frac{\tan(\epsilon + \sigma_1 - \sigma_2)}{\tan(\epsilon + \sigma_1 - \sigma_2) + \tan \mu_2} \left\{ \frac{2b_2}{r} \left[\frac{\sin \epsilon \sin \sigma_1}{\sin(\epsilon + \sigma_1 - \sigma_2)} - \sin \sigma_2 \right] \right. \\ &\quad \left. + \left(\frac{\partial P}{\partial S} \right)_1 \left[\frac{b_2}{b_1} \frac{\sin \epsilon}{\sin(\epsilon + \sigma_1 - \sigma_2)} + \left(\frac{P_2}{P_1} - F \right) \frac{\cos \epsilon \tan \mu_2}{\sin(\epsilon + \sigma_1 - \sigma_2)} \right] \right\} \end{aligned} \quad (20)$$

where

$$\mu = \sin^{-1} \left(\frac{1}{M} \right) \quad (21)$$

$$b = \frac{\gamma P M^2}{2(M^2 - 1)} \quad (22)$$

$$\left(\frac{\partial P}{\partial S} \right)_1 = \left(\frac{\partial P}{\partial S} \right)_3 = \left(\frac{P_c - P_2}{P_c - P_1} \right) \left(\frac{\partial P}{\partial S} \right)_2 \quad (23)$$

$$= e^{-\eta_3} \left(\frac{\partial P}{\partial S} \right)_2 \quad (23a)$$

$$F \approx \left(\frac{4}{\gamma + 1} \right) \left(1 + \frac{\gamma - 1}{2} M_1^2 \right) (\sin \epsilon) ; \quad (24)$$

where

$$\xi = \frac{[(\gamma + 1) \tan(\sigma_2 - \sigma_1) \cos \epsilon - \sin \epsilon] M_1^2 \sin^2 \epsilon + \sin \epsilon}{1 + [1 - 2 \sin^2 \epsilon + 2 \tan(\sigma_2 - \sigma_1) \sin \epsilon \cos \epsilon] M_1^2 \sin^2 \epsilon} \quad (25)$$

To define $dP_2/d\alpha$, the definitions as found in reference 2 for both convex and concave corners are used with only slight changes in nomenclature.

Convex Corner

$$\frac{dP_2}{d\alpha} = \left(\frac{dP_1}{d\alpha} \right)_A + \left(\frac{dP_{t1}}{d\alpha} \right)_B \quad (26)$$

where

$$A = \left(\frac{\partial M_1 / \partial P_1}{\partial M_2 / \partial P_2} \right) \left(\frac{\partial E / \partial M_1}{\partial E / \partial M_2} \right) \quad (27)$$

$$B = \left(\frac{\partial M_1 / \partial P_{t1}}{\partial M_2 / \partial P_2} \right) \left(\frac{\partial E / \partial M_1}{\partial E / \partial M_2} \right) - \left(\frac{\partial M_2 / \partial P_{t2}}{\partial M_2 / \partial P_2} \right)$$

Concave Corner

$$\frac{dP_2}{d\alpha} = \left(\frac{dP_1}{d\alpha} \right)_C + \left(\frac{dP_{t1}}{d\alpha} \right)_D \quad (29)$$

$$\frac{dP_{t2}}{d\alpha} = \left(\frac{dP_{t1}}{d\alpha} \right)_G + \left(\frac{dP_1}{d\alpha} \right)_H \quad (30)$$

where

$$C = \frac{\partial P_2}{\partial P_1} + \left(\frac{\partial P_2}{\partial M_1} \right) \left(\frac{\partial M_1}{\partial P_1} \right) - \left(\frac{\partial P_2}{\partial \epsilon} \right) \left(\frac{\partial M_1}{\partial P_1} \right) \left(\frac{\partial \theta}{\partial M_1} / \frac{\partial \theta}{\partial \epsilon} \right) \quad (31)$$

$$D = \left(\frac{\partial P_2}{\partial M_1} \right) \left(\frac{\partial M_1}{\partial P_{t1}} \right) - \left(\frac{\partial P_2}{\partial \epsilon} \right) \left(\frac{\partial \theta}{\partial M_1} \right) \left(\frac{\partial M_1}{\partial P_{t1}} / \frac{\partial \theta}{\partial \epsilon} \right) \quad (32)$$

$$G = \left(\frac{\partial P_{t2}}{\partial P_{t1}} \right) + \left(\frac{\partial P_{t2}}{\partial M_1} \right) \left(\frac{\partial M_1}{\partial P_{t1}} \right) - \left(\frac{\partial P_{t2}}{\partial \epsilon} \right) \left(\frac{\partial \theta}{\partial M_1} \right) \left(\frac{\partial M_1}{\partial P_{t1}} / \frac{\partial \theta}{\partial \epsilon} \right) \quad (33)$$

$$H = \left(\frac{\partial P_{t2}}{\partial M_1} \right) \left(\frac{\partial M_1}{\partial P_1} \right) \left(\frac{\partial P_{t2}}{\partial \epsilon} \right) \left(\frac{\partial \theta}{\partial M_1} \right) \left(\frac{\partial M_1}{\partial P_1} / \frac{\partial \theta}{\partial \epsilon} \right) \quad (34)$$

At this point it is desirable to recapitulate in such a manner as to consider the equations previously given as being the general equations of this method and the equations that follow will be those to be used for numerical calculations. This requires modifying the subscript nomenclature to make possible calculations for a multi-sectioned body.

Rewriting equations (4), (5), (7), (9), (10), (11), (12), (13), (14) and (15) gives

$$C_{N\alpha(n)} = \frac{2\pi}{A_{B(n)}} \int_0^l \Lambda_{(n)} r_{(n)} dx \quad (35)$$

where

$$r_{(n)} = r_n + (x - x_n) \tan \sigma_{(n)} \quad (36)$$

$$P_{(n)} = (1 - e^{-\eta(n)}) P_{c(n)} + e^{-\eta(n)} P_{n2} \quad (37)$$

$$\eta_{(n)} = \frac{\partial P_{n2}}{\partial S} \frac{x - x_n}{(P_{c(n)} - P_{n2}) \cos \sigma_{(n)}} \quad (38)$$

$$\Lambda_{a(n)} = (1 - e^{-\eta(n)}) \tan \sigma_{(n)} C_{N\alpha_{TC}(n)} \quad (39)$$

$$\Lambda_{b(n)} = e^{-\eta(n)} \Gamma_{(n)} \quad (40)$$

$$\Gamma_{(n)} = \frac{2}{\gamma P_{n1} M_{n1}^2 \pi} \int_0^\pi \left(\frac{dP_{n2}}{d\alpha} \right) \cos \varphi d\varphi \quad (41)$$

$$A_{(n)} = (1 - e^{-\eta(n)}) \tan \sigma_{(n)} C_{N\alpha_{TC(n)}} + e^{-\eta(n)} \Gamma_{(n)} \quad (42)$$

$$C_{N\alpha_{(n)}} = C_{N\alpha_{a(n)}} + C_{N\alpha_{b(n)}} \quad (43)$$

$$C_{N\alpha_{a(n)}} = \frac{2\pi}{A_{B(n)}} \int_0^l (1 - e^{-\eta(n)}) \tan \sigma_{(n)} C_{N\alpha_{TC(n)}} r_{(n)} dx \quad (44)$$

$$C_{N\alpha_{b(n)}} = \frac{2\pi}{A_{B(n)}} \int_0^l e^{-\eta(n)} \Gamma_{(n)} r_{(n)} dx \quad (45)$$

The terms $\left(\frac{\partial P_{n2}}{\partial S}\right)$ in equation (38) and $\left(\frac{dP_{n2}}{d\alpha}\right)$ in equation (41), as noted previously, must be defined separately for a convex corner and a concave corner and are as follows;

Convex Corner

Using the definition for $\left(\frac{\partial P}{\partial S}\right)_2$ given in equations (16) through (19) and applying subscripts results in the following:

$$\frac{\partial P_{n2}}{\partial S} = \frac{b_{n2}}{r_n} \left(\frac{\Omega_{n1}}{\Omega_{n2}} \sin \sigma_{(n-1)} - \sin \sigma_{(n)} \right) + \frac{b_{n2}}{b_{n1}} \frac{\Omega_{n1}}{\Omega_{n2}} \left(\frac{\partial P}{\partial S} \right)_{n1} \quad (46)$$

where

$$b_{n2} = \frac{\gamma P_{n2} M_{n2}^2}{2(M_{n2}^2 - 1)} \quad (47)$$

$$b_{n1} = \frac{\gamma P_{n1} M_{n1}^2}{2(M_{n1}^2 - 1)} \quad (48)$$

$$\frac{b_{n2}}{b_{n1}} = \left(\frac{p_{n2}}{p_{n1}} \right) \left(\frac{M_{n2}^2}{M_{n1}^2} \right) \left(\frac{M_{n1}^2 - 1}{M_{n2}^2 - 1} \right) \quad (49)$$

$$\Omega_{n1} = \frac{1}{M_{n1}} \left[\frac{1 + \frac{\gamma-1}{2} M_{n1}^2}{\frac{\gamma+1}{2}} \right]^{\frac{\gamma+1}{2(\gamma-1)}} \quad (50)$$

$$\Omega_{n2} = \frac{1}{M_{n2}} \left[\frac{1 + \frac{\gamma-1}{2} M_{n2}^2}{\frac{\gamma+1}{2}} \right]^{\frac{\gamma+1}{2(\gamma-1)}} \quad (51)$$

$$\frac{\Omega_{n1}}{\Omega_{n2}} = \left(\frac{M_{n2}}{M_{n1}} \right) \left[\frac{1 + \frac{\gamma-1}{2} M_{n1}^2}{1 + \frac{\gamma-1}{2} M_{n2}^2} \right]^{\frac{\gamma+1}{2(\gamma-1)}} \quad (52)$$

$$\left(\frac{\partial p}{\partial s} \right)_{n1} = e^{-\eta_{(n-1)}} \left(\frac{\partial p}{\partial s} \right)_{(n-1)2} \quad (53)$$

where $\left(\frac{\partial p}{\partial s} \right)_{(n-1)2}$ is defined in calculations for body section (n-1)

Concave Corner

Using the definition for $\left(\frac{\partial p}{\partial s} \right)_2$ given in equations (20), (21), (22), and (23) and applying subscripts produces:

$$\begin{aligned} \left(\frac{\partial p}{\partial s} \right)_{n2} = & \frac{\tan[\epsilon_{(n)} + \sigma_{(n-1)} - \sigma_{(n)}]}{\tan[\epsilon_{(n)} + \sigma_{(n-1)} - \sigma_{(n)}] + \tan \mu_{n2}} \left[\frac{.7 p_{n2} M_{n2}^2}{r_n (M_{n2}^2 - 1)} \left(\frac{\sin \epsilon_{(n)} \sin \sigma_{(n-1)}}{\sin[\epsilon_{(n)} + \sigma_{(n-1)} - \sigma_{(n)}]} - \sin \sigma_{(n)} \right) \right. \\ & + \left(\frac{\partial p}{\partial s} \right)_{n1} \left(\frac{p_{n2} M_{n2}^2 (M_{n1}^2 - 1)}{p_{n1} M_{n1}^2 (M_{n2}^2 - 1)} \frac{\sin \epsilon_{(n)}}{\sin[\epsilon_{(n)} + \sigma_{(n-1)} - \sigma_{(n)}]} \right. \\ & \left. \left. + \left[\frac{p_{n2}}{p_{n1}} - F \right] \frac{\cos \epsilon_{(n)} \tan \mu_{n2}}{\sin[\epsilon_{(n)} + \sigma_{(n-1)} - \sigma_{(n)}]} \right) \right] \quad (54) \end{aligned}$$

where

$$F = \left(\frac{4}{\gamma + 1} \right) \left(1 + \frac{\gamma - 1}{2} M_{n1}^2 \right) (\sin \epsilon_{(n)})^2 \zeta \quad (55)$$

and

$$\zeta = \frac{((\gamma + 1) \tan[\sigma_{(n)} - \sigma_{(n-1)}] \cos \epsilon_{(n)} - \sin \epsilon_{(n)})^2 M_{n1}^2 \sin^2 \epsilon_{(n)} + \sin \epsilon_{(n)}}{1 + \left(1 - 2 \sin^2 \epsilon_{(n)} + 2 \tan[\sigma_{(n)} - \sigma_{(n-1)}] \sin \epsilon_{(n)} \cos \epsilon_{(n)} \right) M_{n1}^2 \sin^2 \epsilon_{(n)}} \quad (55a)$$

Using the definitions for $dP_2/d\alpha$, equation (26) for convex corners and equations (29) and (30) for concave corners, and applying subscripts provides the following:

Convex Corner

$$\left(\frac{dP_2}{d\alpha} \right)_n = \left(\frac{dP_1}{d\alpha} \right)_n A_n + \left(\frac{dP_{t1}}{d\alpha} \right)_n B_n \quad (56)$$

Concave Corner

$$\left(\frac{dP_2}{d\alpha} \right)_n = \left(\frac{dP_1}{d\alpha} \right)_n C_n + \left(\frac{dP_{t1}}{d\alpha} \right)_n D_n \quad (57)$$

$$\left(\frac{dP_{t2}}{d\alpha} \right) = \left(\frac{dP_{t1}}{d\alpha} \right) G + \left(\frac{dP_1}{d\alpha} \right) H \quad (58)$$

The subscript n has been omitted on equation (58) because the pressures are a function of the body sections which have preceded body section (n) . Consider equation (57) and note that $\left(\frac{dP_2}{d\alpha} \right)_n$ is a function of $\left(\frac{dP_{t1}}{d\alpha} \right)_n$ which is a function of $\left(\frac{dP_{t2}}{d\alpha} \right)_{n-1}$ which in turn is a function of $\left(\frac{dP_{t1}}{d\alpha} \right)_{n-1}$ and so forth upstream until $\left(\frac{dP_{t1}}{d\alpha} \right) = 0$. Thus there is established a recurrence formula which, in the process of defining $\left(\frac{dP_2}{d\alpha} \right)$, also defines the parameter ζ .

Definitions of parameters A, B, C, D, G and H are provided in equations (59) through (37).

The recurrence formulas providing for the evaluation of Γ for convex corners are shown in Table 6 and those for concave corners in Table 7.

TABLE 6

EQUATIONS FOR Γ FOR A CONVEX CORNER

| Equation No. | No. of Concave Corners Preceding | $\Gamma_{(n)}$ |
|--------------|----------------------------------|--|
| (1) | nose cone | $A_n \tan \sigma_{(n-1)} C_{No} TC_{(n-1)}$ |
| (2) | preceded by convex corners only | $A_n \Lambda_{n1}$ |
| (3) | 1 | Eq (2) + $B_n H_K \Lambda_{K1}$ |
| (4) | 2 | Eq (3) + $B_n (G_K H_L \Lambda_{L1})$ |
| (5) | 3 | Eq (4) + $B_n (G_K G_L H_M \Lambda_{M1})$ |
| (6) | 4 | Eq (5) + $B_n (G_K G_L G_M H_N \Lambda_{N1})$ |
| (7) | 5 | Eq (6) + $B_n (G_K G_L G_M G_N H_O \Lambda_{O1})$ |
| (8) | 6 | Eq (7) + $B_n (G_K G_L G_M G_N G_O H_P \Lambda_{P1})$ |
| (9) | 7 | Eq (8) + $B_n (G_K G_L G_M G_N G_O G_P H_Q \Lambda_{Q1})$ |
| (10) | 8 | Eq (9) + $B_n (G_K G_L G_M G_N G_O G_P G_Q H_R \Lambda_{R1})$ |
| (11) | 9 | Eq (10) + $B_n (G_K G_L G_M G_N G_O G_P G_Q G_R H_S \Lambda_{S1})$ |
| (12) | 10 | Eq (11) + $B_n (G_K G_L G_M G_N G_O G_P G_Q G_R G_S H_T \Lambda_{T1})$ |

$$\Lambda_{\text{convex corner}} = \Lambda_{(n)} = (1 - e^{-\eta(n)}) \tan \sigma_{(n)} C_{No} TC_{(n)} + e^{-\eta(n)} \Gamma_{(n)}$$

TABLE 7

EQUATIONS FOR Γ FOR A CONCAVE CORNER

| Equation No. | No. of Concave Corners Preceding | $\Gamma_{(n)}$ |
|--------------|----------------------------------|---|
| (1) | nose cone | $C_n \Lambda_{n1}$ |
| (2) | 0 | $C_n \Lambda_{n1}$ (assumes only nose cone plus convex corners precede) |
| (3) | 1 | $C_n \Lambda_{n1} + D_n (H_K \Lambda_{K1})$ |
| (4) | 2 | Eq (3) + $D_n (G_K H_L \Lambda_{L1})$ |
| (5) | 3 | Eq (4) + $D_n (G_K G_L H_M \Lambda_{M1})$ |
| (6) | 4 | Eq (5) + $D_n (G_K G_L G_M H_N \Lambda_{N1})$ |
| (7) | 5 | Eq (6) + $D_n (G_K G_L G_M G_N H_O \Lambda_{O1})$ |
| (8) | 6 | Eq (7) + $D_n (G_K G_L G_M G_N G_O H_P \Lambda_{P1})$ |
| (9) | 7 | Eq (8) + $D_n (G_K G_L G_M G_N G_O G_P H_Q \Lambda_{Q1})$ |
| (10) | 8 | Eq (9) + $D_n (G_K G_L G_M G_N G_O G_P G_Q H_R \Lambda_{R1})$ |
| (11) | 9 | Eq (10) + $D_n (G_K G_L G_M G_N G_O G_P G_Q G_R H_S \Lambda_{S1})$ |
| (12) | 10 | Eq (11) + $D_n (G_K G_L G_M G_N G_O G_P G_Q G_R G_S H_T \Lambda_{T1})$ |

$$\Lambda_{\text{concave corner}} = \Lambda_{(n)} = (1 - e^{-\eta(n)}) \tan \sigma_{(n)} C_{n\alpha_{TC(n)}} + e^{-\eta(n)} \Gamma_{(n)}$$

TABLE 7 (Cont)

Where the Subscripts* Are

| | | | | | | | | |
|---|--|---|---|---|---|---|---|-----|
| n | Upstream corner of body section being analyzed | | | | | | | |
| K | Upstream corner of nearest concave body section upstream of body section (n) | | | | | | | |
| L | Upstream corner of nearest concave body section upstream of body section (K) | | | | | | | |
| M | Same as L except upstream of body section (L) | | | | | | | |
| N | " | " | " | " | " | " | " | (M) |
| O | " | " | " | " | " | " | " | (N) |
| P | " | " | " | " | " | " | " | (O) |
| Q | " | " | " | " | " | " | " | (P) |
| R | " | " | " | " | " | " | " | (Q) |
| S | " | " | " | " | " | " | " | (R) |
| T | " | " | " | " | " | " | " | (S) |

1 When used with a letter subscript (Example K1); refers to conditions on upstream side of corner.

*These subscripts are applicable to both Tables 6 and 7.

$$A = \left(\frac{\partial M_{n1} / \partial P_{n1}}{\partial M_{n2} / \partial P_{n2}} \right) \left(\frac{\partial E / \partial M_{n1}}{\partial E / \partial M_{n2}} \right) \quad (59)$$

$$B = \left(\frac{\partial M_{n1} / \partial P_{t n1}}{\partial M_{n2} / \partial P_{n2}} \right) \left(\frac{\partial E / \partial M_{n1}}{\partial E / \partial M_{n2}} \right) - \left(\frac{\partial M_{n2} / \partial P_{t n2}}{\partial M_{n2} / \partial P_{n2}} \right) \quad (60)$$

$$C = \frac{\partial P_{n2}}{\partial P_{n1}} + \left(\frac{\partial P_{n2}}{\partial M_{n1}} \right) \left(\frac{\partial M_{n1}}{\partial P_{n1}} \right) - \left(\frac{\partial P_{n2}}{\partial \epsilon_{(n)}} \right) \left(\frac{\partial M_{n1}}{\partial P_{n1}} \right) \left(\frac{\partial \theta_n}{\partial M_{n1}} / \frac{\partial \theta_n}{\partial \epsilon_{(n)}} \right) \quad (61)$$

$$D = \left(\frac{\partial P_{n2}}{\partial M_{n1}} \right) \left(\frac{\partial M_{n1}}{\partial P_{t n1}} \right) - \left(\frac{\partial P_{n2}}{\partial \epsilon_{(n)}} \right) \left(\frac{\partial \theta_n}{\partial M_{n1}} \right) \left(\frac{\partial M_{n1}}{\partial P_{t n1}} / \frac{\partial \theta_n}{\partial \epsilon_{(n)}} \right) \quad (62)$$

$$G = \left(\frac{\partial P_{t n2}}{\partial P_{t n1}} \right) + \left(\frac{\partial P_{t n2}}{\partial M_{n1}} \right) \left(\frac{\partial M_{n1}}{\partial P_{t n1}} \right) - \left(\frac{\partial P_{t n2}}{\partial \epsilon_{(n)}} \right) \left(\frac{\partial \theta_n}{\partial M_{n1}} \right) \left(\frac{\partial M_{n1}}{\partial P_{t n1}} / \frac{\partial \theta_n}{\partial \epsilon_{(n)}} \right) \quad (63)$$

$$H = \left(\frac{\partial P_{t n2}}{\partial M_{n1}} \right) \left(\frac{\partial M_{n1}}{\partial P_{n1}} \right) - \left(\frac{\partial P_{t n2}}{\partial \epsilon_{(n)}} \right) \left(\frac{\partial \theta_n}{\partial M_{n1}} \right) \left(\frac{\partial M_{n1}}{\partial P_{n1}} / \frac{\partial \theta_n}{\partial \epsilon_{(n)}} \right) \quad (64)$$

$$E = \left\{ \cos^{-1} \frac{1}{M} + \frac{1}{2} \left(\frac{\gamma + 1}{\gamma - 1} \right)^{\frac{1}{2}} \cos^{-1} \left(1 - \frac{\gamma + 1}{1 + \frac{\gamma - 1}{2} M^2} \right) \right\} \quad (65)$$

$$\frac{\partial M_{n1}}{\partial P_{n1}} = - \frac{1}{\gamma M_{n1} P_{n1}} \left(\frac{P_{t n1}}{P_{n1}} \right)^{\frac{\gamma - 1}{\gamma}} \quad (66)$$

$$\frac{\partial M_{n2}}{\partial P_{n2}} = - \frac{1}{\gamma M_{n2} P_{n2}} \left(\frac{P_{t n2}}{P_{n2}} \right)^{\frac{\gamma - 1}{\gamma}} \quad (67)$$

$$\frac{\partial \Gamma}{\partial M_{n1}} = \frac{1}{M_{n1} (M_{n1}^2 - 1)^{\frac{1}{2}}} - \frac{1}{2} (\gamma + 1)^{\frac{1}{2}} (\gamma - 1)^{\frac{1}{2}} \left\{ \frac{\left(\frac{M_{n1}}{1 + \frac{\gamma - 1}{2} M_{n1}^2} \right)^2}{1 - \left(1 - \frac{\gamma + 1}{1 + \frac{\gamma - 1}{2} M_{n1}^2} \right)^2} \right\}^{\frac{1}{2}} \quad (68)$$

$$\frac{\partial E}{\partial M_{n2}} = \frac{1}{M_{n2}(M_{n2}^2 - 1)^{\frac{1}{2}}} - \frac{1}{2}(\gamma + 1)^{\frac{1}{2}} (\gamma - 1)^{\frac{1}{2}} \left\{ \frac{\left(1 + \frac{\gamma - 1}{2} M_{n2}^2\right)^2}{\left[1 - \left(1 - \frac{\gamma + 1}{1 + \frac{\gamma - 1}{2} M_{n2}^2}\right)^2\right]^{\frac{1}{2}}} \right\} \quad (69)$$

$$\frac{\partial M_{n1}}{\partial P_{t n1}} = \frac{1}{\gamma P_{n1} M_{n1}} \left(\frac{P_{t n1}}{P_{n1}} \right)^{-\frac{1}{\gamma}} \quad (70)$$

$$\frac{\partial M_{n2}}{\partial P_{t n2}} = \frac{1}{\gamma P_{n2} M_{n2}} \left(\frac{P_{t n2}}{P_{n2}} \right)^{-\frac{1}{\gamma}} \quad (71)$$

$$\frac{\partial P_{n2}}{\partial P_{n1}} = \frac{2 \gamma M_{n1}^2 \sin^2 \epsilon_{(n)} - (\gamma - 1)}{\gamma + 1} \quad (72)$$

$$\frac{\partial P_{n2}}{\partial M_{n1}} = P_{n1} \left(\frac{4 \gamma}{\gamma + 1} \right) M_{n1} \sin^2 \epsilon_{(n)} \quad (73)$$

$$\frac{\partial P_{n2}}{\partial \epsilon_{(n)}} = \frac{4 \gamma P_{n1}}{\gamma + 1} M_{n1}^2 \sin \epsilon_{(n)} \cos \epsilon_{(n)} \quad (74)$$

$$\begin{aligned} \frac{\partial \theta_n}{\partial \epsilon_{(n)}} = & \frac{\{2 + M_{n1}^2 (\gamma + 1 - 2 \sin^2 \epsilon_{(n)})\} [4 M_{n1}^2 \cos^2 \epsilon_{(n)} - 2 M_{n1}^2 + \frac{2}{\sin^2 \epsilon_{(n)}}]}{[2 + M_{n1}^2 (\gamma + 1 - 2 \sin^2 \epsilon_{(n)})]^2 + [2 M_{n1}^2 \sin \epsilon_{(n)} \cos \epsilon_{(n)} - 2 \cot \epsilon_{(n)}]^2} \\ & + \frac{[2 M_{n1}^2 \sin \epsilon_{(n)} \cos \epsilon_{(n)} - 2 \cot \epsilon_{(n)}] [4 M_{n1}^2 \sin \epsilon_{(n)} \cos \epsilon_{(n)}]}{[2 + M_{n1}^2 (\gamma + 1 - 2 \sin^2 \epsilon_{(n)})]^2 + [2 M_{n1}^2 \sin \epsilon_{(n)} \cos \epsilon_{(n)} - 2 \cot \epsilon_{(n)}]^2} \end{aligned} \quad (75)$$

$$\frac{\partial \delta_n}{\partial M_{n1}} = \frac{(\gamma - 1) M_{n1} \cot \epsilon_{(n)}}{[1 - M_{n1}^2 (\sin^2 \epsilon_{(n)} - \frac{\gamma + 1}{2})]^2 + [M_{n1}^2 \sin \epsilon_{(n)} \cos \epsilon_{(n)} - \cot \epsilon_{(n)}]^2} \quad (76)$$

$$\frac{\partial p_{t_{n2}}}{\partial p_{t_{n1}}} = \left[\left(\frac{\gamma + 1}{2\gamma} \right) \left[\frac{1}{M_{n1}^2 \sin^2 \epsilon_{(n)} - \left(\frac{\gamma - 1}{2\gamma} \right)} \right] \left[\left(\frac{\gamma + 1}{2} \right) \left(\frac{2 M_{n1}^2 \sin^2 \epsilon_{(n)}}{2 + (\gamma - 1) M_{n1}^2 \sin^2 \epsilon_{(n)}} \right) \right]^\gamma \right]^{\frac{1}{\gamma - 1}} \quad (77)$$

$$\begin{aligned} \frac{\partial p_{t_{n2}}}{\partial M_{n1}} = & \frac{\partial p_{t_{n1}}}{\partial M_{n1}} \left(\frac{\rho_{n2}}{\rho_{n1}} \right)^{\frac{\gamma}{\gamma - 1}} \left(\frac{p_{n1}}{p_{n2}} \right)^{\frac{1}{\gamma - 1}} + p_{t_{n1}} \left[\left(\frac{p_{n1}}{p_{n2}} \right)^{\frac{1}{\gamma - 1}} \frac{\partial (\rho_{n2}/\rho_{n1})}{\partial M_{n1}} \right]^{\frac{\gamma}{\gamma - 1}} \\ & + \left(\frac{\rho_{n2}}{\rho_{n1}} \right)^{\frac{\gamma}{\gamma - 1}} \frac{\partial (p_{n1}/p_{n2})}{\partial M_{n1}} \left(\frac{p_{n1}}{p_{n2}} \right)^{\frac{1}{\gamma - 1}} \end{aligned} \quad (78)$$

$$\frac{\partial p_{t_{n2}}}{\partial \epsilon_{(n)}} = p_{t_{n2}} \left[\left(\frac{p_{n1}}{p_{n2}} \right)^{\frac{1}{\gamma - 1}} \frac{\partial (\rho_{n2}/\rho_{n1})}{\partial \epsilon_{(n)}} \right]^{\frac{\gamma}{\gamma - 1}} + \left(\frac{\rho_{n2}}{\rho_{n1}} \right)^{\frac{\gamma}{\gamma - 1}} \frac{\partial (p_{n1}/p_{n2})}{\partial \epsilon_{(n)}} \left(\frac{p_{n1}}{p_{n2}} \right)^{\frac{1}{\gamma - 1}} \quad (79)$$

$$\frac{\partial (p_{n1}/p_{n2})}{\partial M_{n1}} \left(\frac{\rho_{n2}}{\rho_{n1}} \right)^{\frac{1}{\gamma - 1}} = \left(\frac{-1}{\gamma - 1} \right) \left[\frac{\gamma + 1}{2\gamma X_{n1} - (\gamma - 1)} \right]^{\frac{2 - \gamma}{\gamma - 1}} \left\{ \frac{(\gamma + 1) [4\gamma X_{n1}/M_{n1}]}{[2\gamma X_{n1} - (\gamma - 1)]^2} \right\} \quad (80)$$

$$\frac{\partial (\rho_{n2}/\rho_{n1})}{\partial M_{n1}} \left(\frac{p_{n1}}{p_{n2}} \right)^{\frac{\gamma}{\gamma - 1}} = \frac{\gamma}{\gamma - 1} \left[\frac{(\gamma + 1) X_{n1}}{(\gamma - 1) X_{n1} + 2} \right]^{\frac{1}{\gamma - 1}} \left\{ \frac{4(\gamma + 1) X_{n1}/M_{n1}}{[(\gamma - 1) X_{n1} + 2]^2} \right\} \quad (81)$$

$$\frac{\partial \left(\frac{P_{n1}}{P_{n2}} \right)^{\frac{1}{\gamma-1}}}{\partial \epsilon_{(n)}} = - (4 \gamma) \left(\frac{\gamma+1}{\gamma-1} \right) \left(\frac{P_{n1}}{P_{n2}} \right)^{\frac{2-\gamma}{\gamma-1}} \left\{ \frac{X_{n1} \cot \epsilon_{(n)}}{[2 \gamma X_{n1} - (\gamma-1)]^2} \right\} \quad (82)$$

$$\frac{\partial \left(\frac{\rho_{n2}}{\rho_{n1}} \right)^{\frac{\gamma}{\gamma-1}}}{\partial \epsilon_{(n)}} = (4 \gamma) \left(\frac{\gamma+1}{\gamma-1} \right) \left(\frac{\rho_{n2}}{\rho_{n1}} \right)^{\frac{1}{\gamma-1}} \left\{ \frac{X_{n1} \cot \epsilon_{(n)}}{[1(\gamma-1) X_{n1} + 2]^2} \right\} \quad (83)$$

$$\frac{P_{n1}}{P_{n2}} = \frac{\gamma+1}{2 \gamma M_{n1}^2 \sin^2 \epsilon_{(n)} - (\gamma-1)} \quad (84)$$

$$\frac{\rho_{n2}}{\rho_{n1}} = \frac{(\gamma+1) M_{n1}^2 \sin^2 \epsilon_{(n)}}{(\gamma-1) M_{n1}^2 \sin^2 \epsilon_{(n)} + 2} \quad (85)$$

$$X_{n1} = M_{n1}^2 \sin^2 \epsilon_{(n)} \quad (86)$$

$$\frac{\partial P_{n1}}{\partial M_{n1}} = \gamma P_{n1} M_{n1} \left(1 + \frac{\gamma-1}{2} M_{n1}^2 \right)^{\frac{1}{\gamma-1}} \quad (87)$$

Referring now to equations (5) and (12), it is seen that values of the pressure on a cone, P_c , and the slope of the normal force coefficient for a cone, $C_{N_{TC}}$, are required. Both of these parameters are a function of Mach number and, therefore, the surface Mach number on a cone is also required. Values of these parameters can be determined from several sources, but to simplify the procedure for machine calculation, equations will be used to calculate the pressure and Mach number on the cone surface. Values from reference 5 will be used for values of $C_{N_{TC}}$ and these are contained in Table 8.

The Mach number, as derived from reference 3, is

$$M_n = \frac{M_{n1} \cos \sigma_{(n)} \left(1 - \frac{\sin \sigma_{(n)}}{M_{n1}}\right)^{\frac{1}{2}}}{\left[1.0 + 0.35(M_{n1} \sin \sigma_{(n)})^{1.5}\right]^{\frac{1}{2}}} \quad (88)$$

$$\text{for } 0 \leq M_{n1} \sin \sigma_{(n)} \leq 1.0$$

and

$$M_{n2} = \frac{M_{n1} \cos \sigma_{(n)} \left(1 - \frac{\sin \sigma_{(n)}}{M_{n1}}\right)^{\frac{1}{2}}}{\left\{ \left[1 + \exp \left(-1 - 1.52 M_{n1} \sin \sigma_{(n)}\right)\right] \left[1 + \left(\frac{M_{n1} \sin \sigma_{(n)}}{2}\right)^2\right] \right\}^{\frac{1}{2}}} \quad (89)$$

$$\text{for } M_{n1} \sin \sigma_{(n)} \geq 1.0$$

The pressure on a cone, P_c , is calculated from the equation for pressure coefficient in references 3 and 4, which is in current nomenclature,

TABLE 8
Values of $C_{M_{TC}}$ per Degree

| M_{n2} | $\sigma(n)$ | 0° | 2.5° | 5.0° | 7.5° | 10.0° | 12.5° | 15.0° | 17.5° | 20.0° | 22.5° | 25.0° | 27.5° | 30.0° | 35.0° |
|----------|-------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|-------|
| 1.5 | .03490 | .03450 | .03374 | .03284 | .03190 | .03095 | .02999 | .02902 | .02802 | .02698 | .02592 | .02499 | .02400 | .02260 | |
| 1.75 | .03490 | .03443 | .03361 | .03270 | .03180 | .03094 | .03009 | .02922 | .02831 | .02734 | .02631 | .02522 | .02417 | .02176 | |
| 2.0 | .03490 | .03436 | .03347 | .03256 | .03173 | .03096 | .03021 | .02942 | .02857 | .02764 | .02664 | .02556 | .02441 | .02200 | |
| 2.25 | .03490 | .03421 | .03322 | .03237 | .03169 | .03110 | .03049 | .02981 | .02903 | .02816 | .02717 | .02609 | .02493 | .02240 | |
| 3.0 | .03490 | .03405 | .03301 | .03227 | .03176 | .03131 | .03079 | .03017 | .02942 | .02855 | .02757 | .02648 | .02530 | .02272 | |
| 3.5 | .03490 | .03390 | .03285 | .03226 | .03190 | .03154 | .03107 | .03047 | .02973 | .02886 | .02786 | .02676 | .02556 | .02298 | |
| 4.0 | .03490 | .03375 | .03274 | .03231 | .03207 | .03178 | .03132 | .03073 | .02998 | .02910 | .02809 | .02697 | .02575 | .02317 | |
| 4.5 | .03490 | .03362 | .03268 | .03240 | .03224 | .03197 | .03154 | .03094 | .03018 | .02929 | .02826 | .02712 | .02589 | .02329 | |
| 5.0 | .03490 | .03349 | .03266 | .03251 | .03241 | .03216 | .03173 | .03112 | .03035 | .02943 | .02839 | .02725 | .02600 | .02335 | |
| 6.0 | .03490 | .03327 | .03270 | .03276 | .03272 | .03248 | .03203 | .03139 | .03059 | .02965 | .02859 | .02741 | .02615 | .02344 | |
| 7.0 | .03490 | .03311 | .03282 | .03300 | .03299 | .03273 | .03225 | .03158 | .03076 | .02980 | .02871 | .02752 | .02625 | .02351 | |
| 8.0 | .03490 | .03299 | .03297 | .03322 | .03320 | .03292 | .03241 | .03172 | .03088 | .02990 | .02880 | .02760 | .02631 | .02356 | |
| 10.0 | .03490 | .03290 | .03329 | .03359 | .03353 | .03319 | .03264 | .03191 | .03103 | .03002 | .02891 | .02769 | .02639 | .02360 | |
| 12.0 | .03490 | .03294 | .03358 | .03387 | .03376 | .03337 | .03278 | .03202 | .03112 | .03010 | .02897 | .02774 | .02643 | .02363 | |
| 14.0 | .03490 | .03306 | .03383 | .03407 | .03391 | .03349 | .03287 | .03209 | .03117 | .03013 | .02901 | .02777 | .02646 | .02368 | |
| 15.0 | .03490 | .03312 | .03394 | .03416 | .03398 | .03353 | .03290 | .03211 | .03119 | .03016 | .02902 | .02779 | .02647 | .02369 | |
| 16.0 | .03490 | .03320 | .03404 | .03422 | .03402 | .03358 | .03293 | .03212 | .03120 | .03018 | .02903 | .02780 | .02648 | .02370 | |
| 18.0 | .03490 | .03337 | .03421 | .03434 | .03410 | .03362 | .03297 | .03216 | .03122 | .03020 | .02905 | .02781 | .02649 | .02373 | |
| 20.0 | .03490 | .03351 | .03436 | .03445 | .03417 | .03367 | .03300 | .03219 | .03125 | .03021 | .02906 | .02782 | .02650 | .02373 | |
| 25.0 | .03490 | .03382 | .03462 | .03462 | .03429 | .03375 | .03301 | .03223 | .03126 | .03028 | .02909 | .02786 | .02652 | .02374 | |
| 30.0 | .03490 | .03413 | .03483 | .03473 | .03434 | .03377 | .03303 | .03230 | .03129 | .03035 | .02912 | .02789 | .02654 | .02374 | |

$$C_p = \frac{(4 \sin^2 \sigma_{(n)})(2.5 + 8 \sqrt{M_{n1}^2 - 1} \sin \sigma_{(n)})}{1 + 16 \sqrt{M_{n1}^2 - 1} \sin \sigma_{(n)}} \quad (90)$$

But also

$$C_p = \frac{P/P_\infty - 1}{\frac{\gamma}{2} M_\infty^2} \quad (91)$$

therefore

$$P_{c(n)} = P_{n1} \left(1 + \frac{\gamma}{2} M_{n1}^2 C_p \right) \quad (92)$$

$$= P_{n1} \left\{ 1 + \frac{\gamma}{2} M_{n1}^2 \left[\frac{(4 \sin^2 \sigma_{(n)})(2.5 + 8 \sqrt{M_{n1}^2 - 1} \sin \sigma_{(n)})}{1 + 16 \sqrt{M_{n1}^2 - 1} \sin \sigma_{(n)}} \right] \right\} \quad (92a)$$

It has been shown that this method of calculating $C_{N\alpha}$ for a vehicle calculates the incremental contribution of each body section. These incremental contributions are nondimensionalized by the dynamic pressure, q , immediately upstream of the particular body section and the cross-sectional area at the downstream end of the same body section. It is necessary to use common nondimensionalizing factors and these will be the dynamic pressure of the free stream immediately ahead of the vehicle and the cross-sectional area of the largest cylindrical section of the vehicle. These factors are identified by the symbol q_{11} for the free stream dynamic pressure and S_{ref} for the cross-sectional reference area.

Thus

$$C_{N\alpha_t} = \sum_{(1)}^{(n)} \Delta C_{N\alpha_{(n)}} = \sum_{(1)}^{(n)} (C_{N\alpha_{(n)}}) \frac{q_{n1}}{q_{11}} \frac{A_{B(n)}}{S_{ref}} \quad (93)$$

where

$$q_{n1} = \frac{\gamma}{2} P_{n1} M_{n1}^2 \quad (94)$$

$$q_{11} = \frac{\gamma}{2} P_{11} M_{11}^2 \quad (95)$$

$$A_{B(n)} = \pi r_n^2 + 1 \quad (96)$$

$$S_{ref} = \pi r_{ref}^2 \quad (97)$$

2. UNIT NORMAL FORCE LOADING DISTRIBUTION

The longitudinal loading distribution of the normal force coefficient is expressed by the parameter $dC_{N\alpha}/dx$ and is developed below.

Previously the slope of the normal force coefficient was defined as

$$C_{N\alpha} = \frac{2\pi}{A_B} \int_0^l \Lambda \cdot r dx \quad (4)$$

but it can also be defined as

$$C_{N\alpha} = \int_0^l (dC_{N\alpha}/dx) dx \quad (98)$$

therefore

$$(dC_{N\alpha}/dx) = \frac{2\pi}{A_B} \Lambda r \quad (99)$$

where, as before,

$$\Lambda = \Lambda_a + \Lambda_b \quad (8)$$

$$= (1 - e^{-\eta}) \tan \sigma C_{N_{TC}} + e^{-\eta} \Gamma \quad (12)$$

and

$$r = r_1 + x \tan \sigma \quad (100)$$

Thus

$$(dC_{N\alpha}/dx) = \frac{2\pi}{A_B} \left[(1 - e^{-\eta}) \tan \sigma C_{N_{TC}} + e^{-\eta} \Gamma \right] (r_1 + x \tan \sigma) \quad (101)$$

The distribution in the above form is referenced to the dynamic pressure immediately upstream of the subject body section and to the cross-sectional area at the downstream end of the same body section. Once again, it is necessary that the incremental values be referenced to the same value of the dynamic pressure q_{11} , and area S_{ref} . The equation for the loading distribution then becomes

$$\left(\frac{dC_{N\alpha}}{dx} \right) = \frac{2 \pi q_{n1}}{12 q_{11} S_{ref}} \left[\left(1 - e^{-\eta} \right) \tan \sigma C_{N\alpha_{TC}} + e^{-\eta} \Gamma \right] (r_1 + x \tan \sigma) \quad (102)$$

The above development for the loading distribution $dC_{N\alpha}/dx$, provides the general equation for this parameter. Adding appropriate subscripts produces the form of the equation to be used for calculating the loading distribution over each body section of a multi-sectioned vehicle. This is

$$\left(\frac{dC_{N\alpha}}{dx} \right)_{(n)} = \frac{2 \pi q_{n1}}{12 q_{11} S_{ref}} \left[\left(1 - e^{-\eta(n)} \right) \tan \sigma_{(n)} C_{N\alpha_{TC(n)}} + e^{-\eta(n)} \Gamma_{(n)} \right] (r_n + x \tan \sigma_{(n)}) \quad (103)$$

where $x = x_{n1} - x_n$

For most body sections, the loading distribution should be adequately described by values at six longitudinal body stations. These points will be at the forward end, aft end and at four intermediate locations equally spaced along the body section of the vehicle. This will apply to each body section of the vehicle.

3. NORMAL FORCE CENTER OF PRESSURE

The center of pressure, as used here, will be defined as the longitudinal location, in body station, of the centroid of the normal force loading distribution.

Using the normal definition of a moment of force and the usual sign convention

$$M_{om} = -Nx \quad (104)$$

$$= N(x_{ref} - x_{cp})$$

Now

$$N = C_{No} \alpha q S_{ref} \quad (105)$$

and

$$M_{om} = C_{mo} \alpha q S_{ref} d \quad (106)$$

Thus

$$C_{mo} \alpha q S_{ref} d = C_{No} \alpha q S_{ref} (x_{ref} - x_{cp}) \quad (107)$$

Rearranging

$$x_{cp} = \frac{C_{mo} \alpha q S_{ref} d}{C_{No} \alpha q S_{ref}} \quad (108)$$

$$= \frac{C_{mo} d}{C_{No}} - x_{ref} \quad (108a)$$

If x_{ref} is defined as zero body station, then $x_{ref} = 0$ and

$$x_{cp} = \frac{C_{mo} d}{C_{No}} \quad (109)$$

In reference 1, the definition of C_{mo} is given as

$$C_{mo} = \frac{2\pi}{A_B d} \int_0^l \Lambda r x \, dx \quad (110)$$

with

$$\Lambda = (1 - e^{-\eta}) \tan \sigma C_{No_{TC}} + e^{-\eta} \Gamma \quad (12)$$

then

$$C_{mo} = \frac{2\pi}{A_B d} \int_0^l \left[(1 - e^{-\eta}) \tan \sigma C_{No_{TC}} + e^{-\eta} \Gamma \right] r x \, dx \quad (111)$$

and

$$C_{N\alpha} = \frac{2\pi}{A_B} \int_0^l \left[(1 - e^{-\eta}) \tan \sigma C_{N\alpha_{TC}} + e^{-\eta} \Gamma \right] r dx \quad (112)$$

and the center of pressure is

$$x_{cp} = \frac{\left\{ \frac{2\pi}{A_B d} \int_0^l \left[(1 - e^{-\eta}) \tan \sigma C_{N\alpha_{TC}} + e^{-\eta} \Gamma \right] r x dx \right\} d}{\frac{2\pi}{A_B} \int_0^l \left[(1 - e^{-\eta}) \tan \sigma C_{N\alpha_{TC}} + e^{-\eta} \Gamma \right] r dx} \quad (113)$$

$$= \frac{\int_0^l \left[(1 - e^{-\eta}) \tan \sigma C_{N\alpha_{TC}} + e^{-\eta} \Gamma \right] r x dx}{\int_0^l \left[(1 - e^{-\eta}) \tan \sigma C_{N\alpha_{TC}} + e^{-\eta} \Gamma \right] r dx} \quad (113_1)$$

Equation (113) is then the general equation for the center of pressure.

The same equation with the proper subscripts added will be used for calculations and is

$$x_{cp(n)} = \frac{\int_0^l \left[\left(1 - e^{-\eta(n)} \right) \tan \sigma_{(n)} C_{N\alpha_{TC(n)}} + e^{-\eta(n)} \Gamma_{(n)} \right] r_{(n)} x_{(n)} dx}{\int_0^l \left[\left(1 - e^{-\eta(n)} \right) \tan \sigma_{(n)} C_{N\alpha_{TC(n)}} + e^{-\eta(n)} \Gamma_{(n)} \right] r_{(n)} dx} \quad (114)$$

where

$$x_{(n)} = (x - x_n) \quad (13)$$

and

$$r_{(n)} = r_n + (x - x_n) \tan \sigma_{(n)} \quad (36)$$

The above equation defines the center of pressure for one particular body section, whereas the center of pressure of the loading over the complete body is desired; therefore, equation (113) defines the summation to be used

$$x_{cp\text{total}} = \frac{\sum_{(1)}^{(n)} \int_0^l \left[(1 - e^{-\eta(n)}) \tan \sigma_{(n)} C_{N\alpha_{TC(n)}} + e^{-\eta(n)} \Gamma_{(n)} \right] r_{(n)} x_{(n)} dx}{\sum_{(1)}^{(n)} \int_0^l \left[(1 - e^{-\eta(n)}) \tan \sigma_{(n)} C_{N\alpha_{TC(n)}} + e^{-\eta(n)} \Gamma_{(n)} \right] r_{(n)} dx} \quad (115)$$

To utilize this method for determining the normal force coefficient center of pressure and loading distribution, it is first necessary to calculate the variation along the body of the static and total pressure, Mach number, pressure gradient and the loading parameter F. The following equations, (116-138), are to be used for this purpose.

$$P_{n2} = P_{n1} \left[\frac{2\gamma M_{n1}^2 \sin^2 \epsilon_{(n)} - (\gamma - 1)}{\gamma + 1} \right] \quad 116$$

$$M_{n2} = \left\{ \frac{(\gamma + 1)^2 M_{n1}^4 \sin^2 \epsilon_{(n)} - 4 (M_{n1}^2 \sin^2 \epsilon_{(n)} - 1)(\gamma M_{n1}^2 \sin^2 \epsilon_{(n)} + 1)}{[2\gamma M_{n1}^2 \sin^2 \epsilon_{(n)} - (\gamma - 1)][(\gamma - 1) M_{n1}^2 \sin^2 \epsilon_{(n)} + 2]} \right\}^{\frac{1}{2}} \quad 117$$

$$P_{t_{n2}} = P_{t_{n1}} \left[\frac{(\gamma + 1) M_{n1}^2 \sin^2 \epsilon_{(n)}}{(\gamma - 1) M_{n1}^2 \sin^2 \epsilon_{(n)} + 2} \right]^{\frac{\gamma}{\gamma-1}} \left[\frac{\gamma + 1}{2\gamma M_{n1}^2 \sin^2 \epsilon_{(n)} - (\gamma - 1)} \right]^{\frac{1}{\gamma-1}} \quad 118$$

$$M_{n1} = \left\{ \frac{2 [\cot \epsilon_{(n)} + \tan (\sigma_{(n)} - \sigma_{(n-1)})]}{\sin 2 \epsilon_{(n)} - (\gamma + \cos 2 \epsilon_{(n)}) \tan (\sigma_{(n)} - \sigma_{(n-1)})} \right\}^{\frac{1}{\gamma-1}} \quad 119$$

$$(\sigma_{(n)} - \sigma_{(n-1)}) = \tan^{-1} \left[\frac{2(M_{n1}^2 \sin^2 \epsilon_{(n)} - 1) \cot \epsilon_{(n)}}{M_{n1}^2 (\gamma + 1 - 2 \sin^2 \epsilon_{(n)}) + 2} \right] \quad 120$$

$$\cot(\sigma_{(n)} - \sigma_{(n-1)}) = \tan \epsilon_{(n)} \left[\frac{(\gamma + 1) M_{n1}^2}{2(M_{n1}^2 \sin^2 \epsilon_{(n)} - 1)} - 1 \right] \quad 121$$

$$\sigma_{(n)} - \sigma_{(n-1)} = \left[\cos^{-1} \frac{1}{M_{n2}} + \frac{1}{2} \left(\frac{\gamma + 1}{\gamma - 1} \right)^{\frac{1}{2}} \cos^{-1} \left(1 - \frac{\gamma + 1}{1 + \frac{\gamma - 1}{2} M_{n2}^2} \right) \right] \\ - \left[\cos^{-1} \frac{1}{M_{n1}} + \frac{1}{2} \left(\frac{\gamma + 1}{\gamma - 1} \right)^{\frac{1}{2}} \cos^{-1} \left(1 - \frac{\gamma + 1}{1 + \frac{\gamma - 1}{2} M_{n1}^2} \right) \right] \quad 122$$

$$M_{n1} = \left\{ \frac{2}{\gamma - 1} \left[\left(\frac{P_{t_{n1}}}{P_{n1}} \right)^{\frac{\gamma-1}{\gamma}} - 1 \right] \right\}^{\frac{1}{2}} \quad 123$$

$$M_{n2} = \left\{ \frac{2}{\gamma - 1} \left[\left(\frac{P_{t_{n2}}}{P_{n2}} \right)^{\frac{\gamma-1}{\gamma}} - 1 \right] \right\}^{\frac{1}{2}} \quad 124$$

$$P_{t_{n1}} = P_{n1} \left(1 + \frac{\gamma-1}{2} M_{n1}^2 \right)^{\frac{\gamma}{\gamma-1}} \quad 125$$

$$P_{t_{n2}} = P_{n2} \left(1 + \frac{\gamma-1}{2} M_{n2}^2 \right)^{\frac{\gamma}{\gamma-1}} \quad 126$$

$$P_{n1} = \frac{P_{t_{n1}}}{\left(1 + \frac{\gamma-1}{2} M_{n1}^2 \right)^{\frac{\gamma}{\gamma-1}}} \quad 127$$

$$P_{n2} = \frac{P_{t_{n2}}}{\left(1 + \frac{\gamma-1}{2} M_{n2}^2 \right)^{\frac{\gamma}{\gamma-1}}} \quad 128$$

$$P_{c(n)} = P_{n1} \left(1 + \frac{\gamma}{2} M_{n1}^2 C_{P_{c(n)}} \right) \quad 129$$

$$\left(\frac{\partial P}{\partial S} \right)_{n2} = \frac{b}{r_n} \left[\frac{\Omega_{n1}}{\Omega_{n2}} \sin \sigma_{(n-1)} - \sin \sigma_{(n)} \right] + \frac{b}{b_{n1}} \frac{\Omega_{n1}}{\Omega_{n2}} \left(\frac{\partial P}{\partial S} \right)_{n1} \quad 130$$

$$\eta_{(n)} = \left(\frac{\partial P}{\partial S} \right)_{n2} \frac{x - x_n}{(P_{c(n)} - P_{n2}) \cos \sigma_{(n)}} \quad 131$$

$$P_{nx} = P_{c(n)} - (P_{c(n)} - P_{n2}) e^{-\eta_{(n)} x} \quad 132$$

$$\left(\frac{\partial P}{\partial S} \right)_{(n+1)1} = \left(\frac{P_{c(n)} - P_{(n+1)1}}{P_{c(n)} - P_{n2}} \right) \left(\frac{\partial P}{\partial S} \right)_{n2} \quad 133$$

$$\begin{aligned} \left(\frac{\partial P}{\partial S} \right)_{n2} = & \frac{\tan [\epsilon_{(n)} + \sigma_{(n-1)} - \sigma_{(n)}]}{\tan [\epsilon_{(n)} + \sigma_{(n-1)} - \sigma_{(n)}] + \tan \mu_{n2}} \left[\frac{\gamma P_{n2} M_{n2}^2}{r_n (M_{n2}^2 - 1)} \left(\frac{\sin \epsilon_{(n)} \sin \sigma_{(n-1)}}{\sin [\epsilon_{(n)} + \sigma_{(n-1)} - \sigma_{(n)}]} \right. \right. \\ & \left. \left. - \sin \sigma_{(n)} \right) + \left(\frac{\partial P}{\partial S} \right)_{n1} \left(\frac{P_{n2} M_{n2}^2 (M_{n1}^2 - 1)}{P_{n1} M_{n1}^2 (M_{n2}^2 - 1)} \frac{\sin \epsilon_{(n)}}{\sin [\epsilon_{(n)} + \sigma_{(n-1)} - \sigma_{(n)}]} \right. \right. \\ & \left. \left. + \left[\frac{P_{n2}}{P_{n1}} - F \right] \frac{\cos \epsilon_{(n)} \tan \mu_{n2}}{\sin [\epsilon_{(n)} + \sigma_{(n-1)} - \sigma_{(n)}]} \right] \right] \quad 134 \end{aligned}$$

$$F = \left(\frac{4}{\gamma + 1} \right) \left(1 + \frac{\gamma - 1}{2} M_{n1}^2 \right) \sin \epsilon_{(n)} \quad \zeta \quad 135$$

where

$$\zeta = \frac{[(\gamma + 1) \tan (\sigma_{(n)} - \sigma_{(n-1)}) \cos \epsilon_{(n)} - \sin \epsilon_{(n)}] M_{n1}^2 \sin^2 \epsilon_{(n)} + \sin \epsilon_{(n)}}{1 + [1 - 2 \sin^2 \epsilon_{(n)} + 2 \tan (\sigma_{(n)} - \sigma_{(n-1)}) \sin \epsilon_{(n)} \cos \epsilon_{(n)}] M_{n1}^2 \sin^2 \epsilon_{(n)}}$$

$$0 \leq M_{n1} \sin \sigma_{(n)} \leq 1.0$$

$$M_{n2} = \frac{M_{n1} \cos \sigma_{(n)} \left(1 - \frac{\sin \sigma_{(n)}}{M_{n1}} \right)^{\frac{1}{2}}}{[1.0 + 0.35(M_{n1} \sin \sigma_{(n)})^{1.5}]^{\frac{1}{2}}} \quad 136$$

$$M_{n1} \sin \sigma_{(n)} \geq 1.0$$

$$M_{n2} = \frac{M_{n1} \cos \sigma_{(n)} \left(1 - \frac{\sin \sigma_{(n)}}{M_{n1}} \right)^{\frac{1}{2}}}{\left\{ \left[1 + \exp(-1 - 1.52 M_{n1} \sin \sigma_{(n)}) \right] \left[1 + \left(\frac{M_{n1} \sin \sigma_{(n)}}{2} \right)^2 \right] \right\}^{\frac{1}{2}}} \quad 137$$

$$C_{PC(n)} = \frac{(4 \sin^2 \sigma_{(n)}) (2.5 + 8 \sqrt{M_{n1}^2 - 1} \sin \sigma_{(n)})}{(1 + 16 \sqrt{M_{n1}^2 - 1} \sin \sigma_{(n)})} \quad 138$$

4. LIMITS ON PARAMETERS

1. $(\sigma_{(n)} - \sigma_{(n-1)})$

a. $0^\circ < (\sigma_{(n)} - \sigma_{(n-1)}) \leq 30.0^\circ$

2. M_{n1}

a. $2.6 \leq M_{n1} \leq 10.0$

3. $\left(\frac{\partial p}{\partial s}\right)_{n2}$ for a convex corner, $(\sigma_{(n)} < \sigma_{(n-1)})$

a. $\left(\frac{\partial p}{\partial s}\right)_{n2} \geq 0.0$

b. Must have same sign as the pressure difference $(P_{c(n)} - P_{n2})$

4. $\left(\frac{\partial p}{\partial s}\right)_{n2}$ for a concave corner, $(\sigma_{(n)} > \sigma_{(n-1)})$

a. $\left(\frac{\partial p}{\partial s}\right)_{n2} \leq 0.0$

b. Must have same sign as the pressure difference $(P_{c(n)} - P_{n2})$

5. $\eta_{(n)}$ for both convex and concave body sections

a. Because of 3 and 4 above, it follows that $\eta_{(n)} \geq 0.0$

5. NOMENCLATURE

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-----------------------------|---|--------------|
| A | Parameter Defined by Equation (59) | |
| A_B | Base Area of Body Section (n) | sq ft |
| b | Parameter Defined by Equation (17) | |
| B | Parameter Defined by Equation (60) | |
| C | Parameter Defined by Equation (61) | |
| $C_{M\alpha}, dC_M/d\alpha$ | Slope of Pitching Moment Coefficient | 1/deg |
| C_N | Normal Force Coefficient | dim. |
| C_P | Pressure Coefficient $(= P - P_\infty / \frac{\gamma}{2} P_\infty M_\infty^2)$ | dim. |
| $C_{N\alpha}, dC_N/d\alpha$ | Slope of Normal Force Coefficient | 1/deg |
| $C_{N\alpha TC}$ | Slope of Normal Force Coefficient for a Tangent Cone | 1/deg |
| $dC_{N\alpha}/dx$ | Longitudinal Loading Parameter | 1/deg-in. |
| d | Body Diameter | in. ft |
| D | Parameter Defined by Equation (62) | |
| e | Base of Napierian Logarithm | dim. |
| E | Parameter Defined Equation (65) | dim. |
| F | Parameter Defined by Equation (55) and (55a) | dim. |
| G | Parameter Defined by Equation (63) | dim. |
| H | Parameter Defined by Equation (64) | dim. |
| l | Upper Limit of Integration | ft |
| M | Mach Number | dim. |
| Mom | Moment | in-lb |
| N | Normal Force | lb |
| P | Pressure | psi psf |
| P_2 | Static Pressure at Downstream Side of a Corner | psi psf |
| P_c | Cone Surface Static Pressure | psi psf |

| | | |
|------------|--|-------------|
| q | Dynamic Pressure $(\frac{\gamma}{2} V^2)$ | psf |
| r | Body Radius | in. ft. |
| S | Distance Along Streamline | in. |
| S_{ref} | Reference Area (Cross-sectional Area of Largest Cylindrical Body Section) | sq ft |
| x | Longitudinal Distance Along Body (Body Station) | in. ft. |
| x_{cp} | Normal Force Center of Pressure, Body Station | in. |
| α | Angle of Attack in Fitch Plane | deg |
| γ | Ratio of Specific Heats | dim. |
| Γ | Loading Parameter Defined by Equation (11) | dim. |
| δ | Shockwave Angle Relative to Body Centerline | deg |
| ϵ | Shock Wave Angle Relative to Flow Direction Immediately Upstream of Body Corner (Two-Dimensional Flow) | deg |
| ζ | Parameter Defined by Equation (55a) | |
| η | Exponent of e | dim. |
| θ | Flow Turn Angle $(\sigma_{(n)} - \sigma_{(n-1)})$ | deg |
| Λ | Loading Parameter Defined by Equation (3) & (12) | dim. |
| μ | $\sin^{-1} \frac{1}{M}$ | dim. |
| ρ | Density | Slugs/cu ft |
| π | $Pi = 3.1416$ | dim. |
| σ | Body Surface Angle Relative to Body Centerline | deg |
| φ | Body Meridional Angle | deg |
| Ω | Parameter Defined by Equation (18) | |

6. SUBSCRIPTS

| | |
|-----|--|
| a | First Increment |
| b | Second Increment |
| B | Base |
| c | Cone Value |
| cp | Center of Pressure |
| i | i th Section or Location |
| (n) | Body Section for which Values are being Calculated |
| n | Upstream Corner of Body Section (n) |
| n1 | Upstream Side of Upstream Corner of Body Section (n) |
| n2 | Downstream Side of Upstream Corner of Body Section (n) |
| n3 | Upstream Side of Downstream Corner of Body Section (n) (Same as (n + 1)1) |
| K | Nearest Body Corner at which a Concave Corner Occurs Upstream of Body Section (n) |
| L | Nearest Body Corner at which a Concave Corner Occurs Upstream of Body Corner K |
| M | Nearest Body Corner at which a Concave Corner Occurs Upstream of Body Corner L |
| N | Nearest Body Corner at which a Concave Corner Occurs Upstream of Body Corner M |
| O | Nearest Body Corner at which a Concave Corner Occurs Upstream of Body Corner N |
| P | Nearest Body Corner at which a Concave Corner Occurs Upstream of Body Corner O |
| Q | Nearest Body Corner at which a Concave Corner Occurs Upstream of Body Corner P |
| R | Nearest Body Corner at which a Concave Corner Occurs Upstream of Body Corner Q |

| | |
|----------|--|
| S | Nearest Body Corner at which a Concave Corner Occurs Upstream of Body Corner R |
| T | Nearest Body Corner at which a Concave Corner Occurs Upstream of Body Corner S |
| t | Total |
| TC | Tangent Cone |
| ref | Reference |
| 1 | Upstream Side of Upstream Corner of Body Section |
| 2 | Downstream Side of Upstream Corner of Body Section |
| 3 | Upstream Side of Downstream Corner of Body Section |
| 11 | Body Free Stream Value |
| α | Derivative with Respect to Angle of Attack α |
| ∞ | Local Free Stream Value |

D. LIFTING SURFACES AERODYNAMIC PARAMETERS

This subroutine is designed to provide the capability of predicting the force and moment contribution of lifting surfaces to missile aerodynamics and control. The planforms of the surfaces are restricted to a basic delta planform with an unswept trailing edge and taper ratios in the range of 0.0 to 0.60 ($0.0 \leq \lambda \leq 0.60$).

The surfaces, whether they are canards or tail fins, are considered to occur in sets consisting of two pairs of surfaces in a cruciform configuration. Deflections for pitch and yaw control are possible but only by deflecting the full semi-span surface (i.e. no provisions for partial chord flaps) and each surface of a pair is deflected identically to the other (i.e. no differential deflections).

The basic aerodynamic parameters derived from this procedure are $C_{L\alpha}$, C_{D0} , C_{DL} , and x_{cp} versus Mach number for canards and fins. The force coefficients $C_{L\alpha}$, C_{D0} and C_{DL} are calculated per pair based on the exposed planform area, S_{exp} , of the particular lifting surface. As it is desired to use the values of these parameters as they apply to a missile system, equations are provided to resolve them into normal, side and axial force coefficients, C_N , C_Y , and C_A in the missile axis system and based on S_{ref} , the missile reference area.

In addition, equations are provided for determination of hinge moments produced by the lifting surfaces and a procedure for calculating an estimated weight and center of gravity of the lifting surfaces. The weight calculated is an estimate only of the weight of the exposed surfaces and does not include an estimate for attachment or actuation system weights.

1. BASIC FORCE AND MOMENT EQUATIONS

Assuming a missile system composed of an axisymmetric body with cruciform canards and cruciform fins, the following equations can be written, referenced to the missile axis system.

Static Forces

$$N = N_b + N_c + N_f \quad (\text{Pitch}) \quad (1)$$

$$Y = Y_b + Y_c + Y_f \quad (\text{Yaw}) \quad (2)$$

$$A = A_b + A_c + A_f \quad (\text{Axial}) \quad (3)$$

Where

$$N_b = C_{Nb} q S_{ref} \quad (4)$$

$$N_c = C_{Nc} q S_{ref} \quad (5)$$

$$N_f = C_{Nf} q S_{ref} \quad (6)$$

$$Y_b = C_{Yb} q S_{ref} \quad (7)$$

$$Y_c = C_{Yc} q S_{ref} \quad (8)$$

$$Y_f = C_{Yf} q S_{ref} \quad (9)$$

And

$$C_{Nb} = C_{Nob} \alpha \quad (10)$$

$$\begin{aligned} C_{Nc} &= C_{Noc} \alpha_{effc} \frac{S_c}{S_{ref}} \\ &= \frac{S_c}{S_{ref}} \left(\left[C_{Loc} (\alpha + \delta_{cp}) + C_{lc} (\alpha + \delta_{cp})^2 \right] \cos \alpha \right. \\ &\quad \left. + \left[C_{D0c} + K_{Lc} \left[C_{Loc} (\alpha + \delta_{cp}) + C_{lc} (\alpha + \delta_{cp})^2 \right]^2 \right] \sin \alpha \right) \quad (11) \end{aligned}$$

$$\begin{aligned} C_{Nf} &= C_{Nof} \alpha_{efff} \frac{S_f}{S_{ref}} \\ &= \frac{S_f}{S_{ref}} \left(\left[C_{Lof} (\alpha + \delta_{fp}) + C_{lf} (\alpha + \delta_{fp})^2 \right] \cos \alpha \right. \\ &\quad \left. + \left[C_{D0f} + K_{Lf} \left[C_{Lof} (\alpha + \delta_{fp}) + C_{lf} (\alpha + \delta_{fp})^2 \right]^2 \right] \sin \alpha \right) \quad (12) \end{aligned}$$

$$C_{Yb} = C_{Nob} \beta \quad (13)$$

$$C_{Yc} = C_{N\alpha c}^{\beta} \text{ effc } \frac{S_c}{S_{ref}}$$

$$= \frac{S_c}{S_{ref}} \left(\left[C_{L\alpha c} (\beta + \delta_{cY}) + C_{lc} (\beta + \delta_{cY})^2 \right] \cos \beta + \left\{ C_{D0c} + K_{Lc} \left[C_{L\alpha c} (\beta + \delta_{cY}) + C_{lc} (\beta + \delta_{cY})^2 \right]^2 \right\} \sin \beta \right) \quad (14)$$

$$C_{Yf} = C_{N\alpha f}^{\beta} \text{ efff } \frac{S_f}{S_{ref}} \quad (15)$$

$$= \frac{S_f}{S_{ref}} \left(\left[C_{L\alpha f} (\beta + \delta_{fY}) + C_{lf} (\beta + \delta_{fY})^2 \right] \cos \beta + \left\{ C_{D0f} + K_{Lf} \left[C_{L\alpha f} (\beta + \delta_{fY}) + C_{lf} (\beta + \delta_{fY})^2 \right]^2 \right\} \sin \beta \right) \quad (15)$$

For the Axial Force

$$A_b = C_{Ab} q S_{ref} \quad (16)$$

$$A_c = (C_{AcP} + C_{AcY}) q S_{ref} \quad (17)$$

$$A_f = (C_{AfP} + C_{AfY}) q S_{ref} \quad (18)$$

Where

$$C_{Ab} = C_{Ab} \quad (19)$$

$$C_{AcP} = \left(\left\{ C_{D0c} + K_{Lc} \left[C_{L\alpha c} (\alpha + \delta_{cP}) + C_{lc} (\alpha + \delta_{cP})^2 \right]^2 \right\} \cos \alpha - \left[C_{L\alpha c} (\alpha + \delta_{cP}) + C_{lc} (\alpha + \delta_{cP})^2 \right] \sin \alpha \right) \frac{S_c}{S_{ref}} \quad (20)$$

$$C_{AcY} = \left(\left\{ C_{DOc} + K_{Lc} \left[C_{Loe} (\beta + \delta_{cY}) + C_{lc} (\beta + \delta_{cY})^2 \right]^2 \right\} \cos \beta - \left[C_{Loe} (\beta + \delta_{cY}) + C_{lc} (\beta + \delta_{cY})^2 \right] \sin \beta \right) \frac{S_c}{S_{ref}} \quad (21)$$

$$C_{AfP} = \left(\left\{ C_{DOF} + K_{Lf} \left[C_{LoF} (\alpha + \delta_{fP}) + C_{lf} (\alpha + \delta_{fP})^2 \right]^2 \right\} \cos \alpha - \left[C_{LoF} (\alpha + \delta_{fP}) + C_{lf} (\alpha + \delta_{fP})^2 \right] \sin \alpha \right) \frac{S_f}{S_{ref}} \quad (22)$$

$$C_{AfY} = \left(\left\{ C_{DOF} + K_{Lf} \left[C_{LoF} (\beta + \delta_{fY}) + C_{lf} (\beta + \delta_{fY})^2 \right]^2 \right\} \cos \beta - \left[C_{LoF} (\beta + \delta_{fY}) + C_{lf} (\beta + \delta_{fY})^2 \right] \sin \beta \right) \frac{S_f}{S_{ref}} \quad (23)$$

Static Moments

$$Mom = M_b + M_c + M_f \quad (24)$$

Pitch Moment

$$M_y = N_b \bar{x}_b + N_c \bar{x}_c + N_f \bar{x}_f + A_b \bar{z}_b \quad (25)$$

Yaw Moment

$$M_z = Y_b \bar{x}_b + Y_c \bar{x}_c + Y_f \bar{x}_f + A_b \bar{y}_b \quad (26)$$

Roll Moment

$$M_x = -N_b \bar{y}_b - Y_b \bar{z}_b - N_c \bar{y}_c - N_f \bar{y}_c - Y_c \bar{z}_c - Y_f \bar{z}_c \quad (27)$$

$$= -N_b \bar{y}_b - Y_b \bar{z}_b - N_c \bar{y}_b - N_f \bar{y}_b - Y_c \bar{z}_b - Y_f \bar{z}_b \quad (28)$$

$$= -(N_b + N_c + N_f) \bar{y}_b - (Y_b + Y_c + Y_f) \bar{z}_b \quad (29)$$

The forces N_b , N_c , N_f , A_b , Y_b , Y_c and Y_f have been defined leaving the definition of the moment arms. These are as follows:

$$\bar{x}_b = x_{cg} - x_{cpb} \quad (30)$$

$$\bar{x}_c = x_{cg} - x_{cpc} \quad (31)$$

$$\bar{x}_f = x_{cg} - x_{cpf} \quad (32)$$

$$\bar{z}_b = z_{cg} \quad (33)$$

$$\bar{y}_b = y_{cg} \quad (34)$$

Lifting Surface Hinge Moment

The general equations for the lifting surface hinge moments and moment arms are:

$$(H.M.)_y = N\bar{x}_h - C_A\bar{z}_h \quad (35)$$

$$(H.M.)_z = Y\bar{x}_h + C_A\bar{y}_h \quad (36)$$

Where

$$\bar{x}_h = (x_H - x_{cp}) \cos \delta \quad (37)$$

$$\bar{y}_h = (x_H - x_{cp}) \sin \delta \quad (38)$$

$$\bar{z}_h = (x_H - x_{cp}) \sin \delta \quad (39)$$

Thus, for the canards

$$(H.M.)_{yc} = N_c(x_{Hc} - x_{cpc}) \cos \delta_{cp} + C_{AcP} (x_{Hc} - x_{cpc}) \sin \delta_{cp} \quad (40)$$

$$(H.M.)_{zc} = Y_c (x_{Hc} - x_{cpc}) \cos \delta_{cy} + C_{AcY} (x_{Hc} - x_{cpc}) \sin \delta_{cy} \quad (41)$$

and similarly for the fins

$$(H.M.)_{yf} = N_f (x_{Hf} - x_{cpf}) \cos \delta_{fP} + C_{AfP} (x_{Hf} - x_{cpf}) \sin \delta_{fP} \quad (42)$$

$$(H.M.)_{zf} = Y_f (x_{Hf} - x_{cpf}) \cos \delta_{fY} + C_{AfY} (x_{Hf} - x_{cpf}) \sin \delta_{fY} \quad (43)$$

2. INPUT PARAMETERS

The parameters required as input are x_{or} , c_R , ϵ_L , λ , τ , x_H , r_b and d_{ref} . Except for d_{ref} , sets of values of the other parameters must be provided for each set of lifting surfaces, canards and tail fins.

Limitations exist on the range of permissible values for some of these parameters and are defined below. Definitions of all the parameters can be found in the section on nomenclature and sketches defining the axis system; lifting surface geometry and missile geometry are provided in Figures 7 thru 10.

$$24.0^\circ \leq \epsilon_L \leq 70.0^\circ$$

$$0.0 \leq \lambda \leq 0.60$$

$$0.03 \leq \tau \leq 0.12$$

$$x_{orf} \leq x_e - c_{Rf}$$

The above are limitations on the input parameters and must be controlled at that point. Additional limitations exist relative to values of some of the parameters which are calculated. These are:

AR Limits on this parameter are defined in Figure 11 as a function of the limits imposed on ϵ_L and λ .

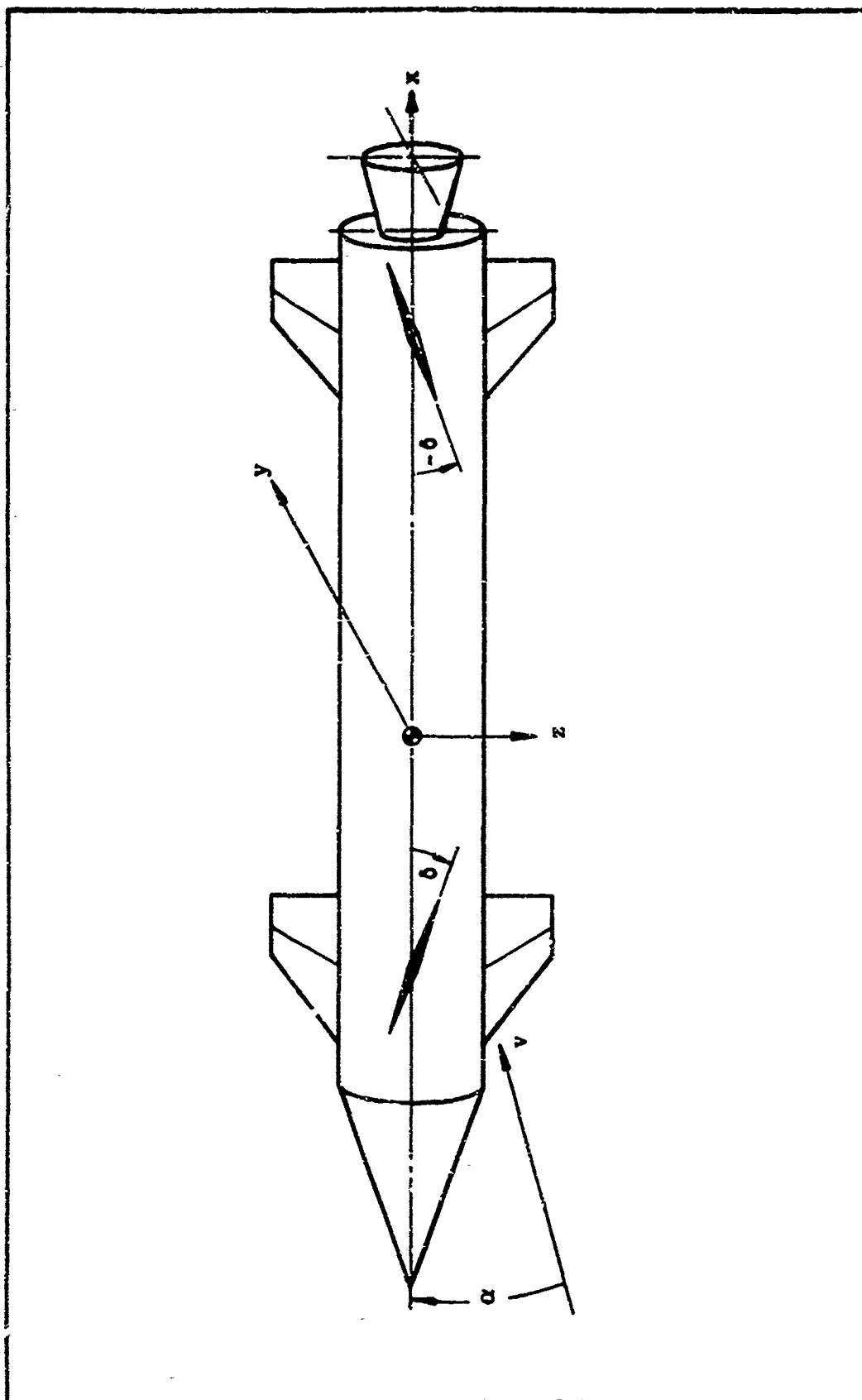
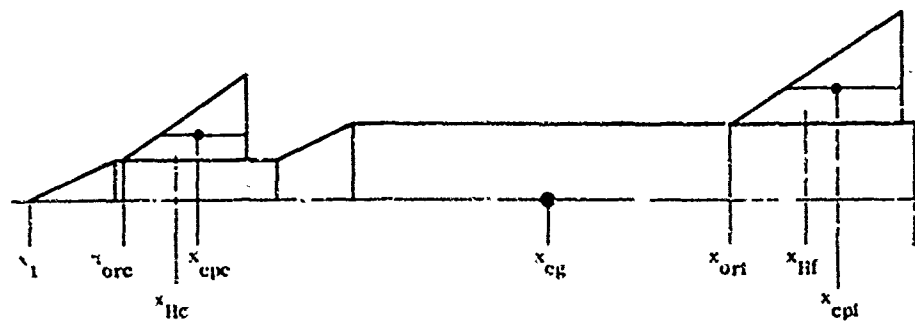
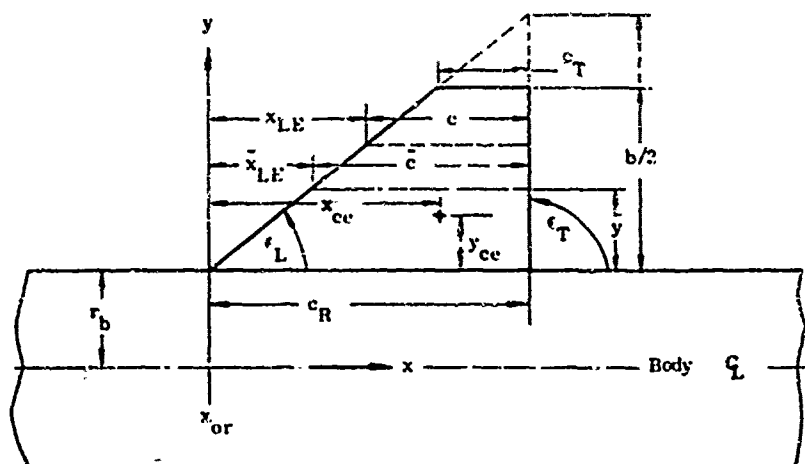


Figure 7. Missile Axis System



a. MISSILE SYSTEM



b. LIFTING SURFACE

Figure 8. Lifting Surface Geometry Parameters

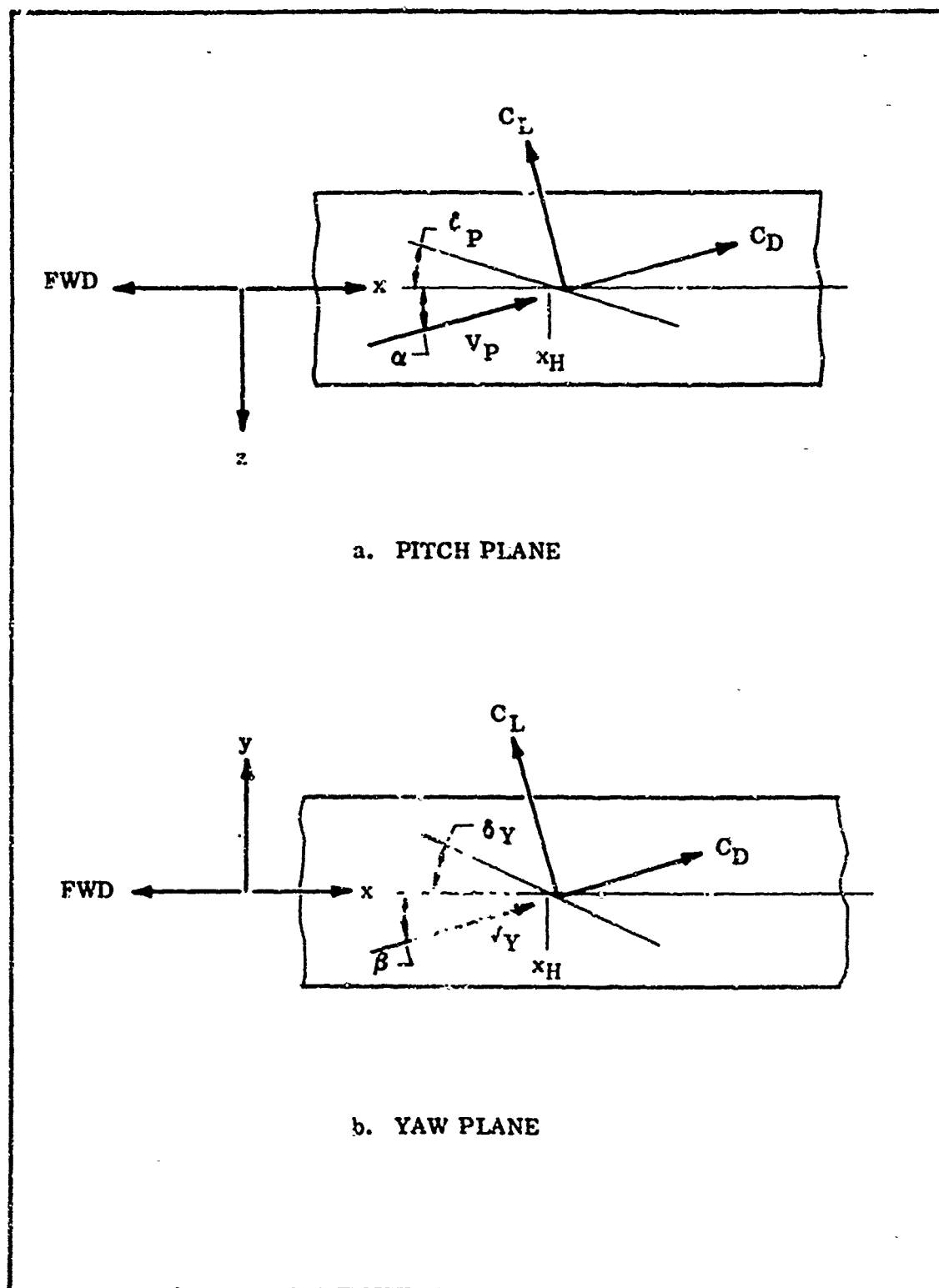


Figure 9. Lifting Surfaces Pitch, Yaw and Deflection Angles and Force Coefficients

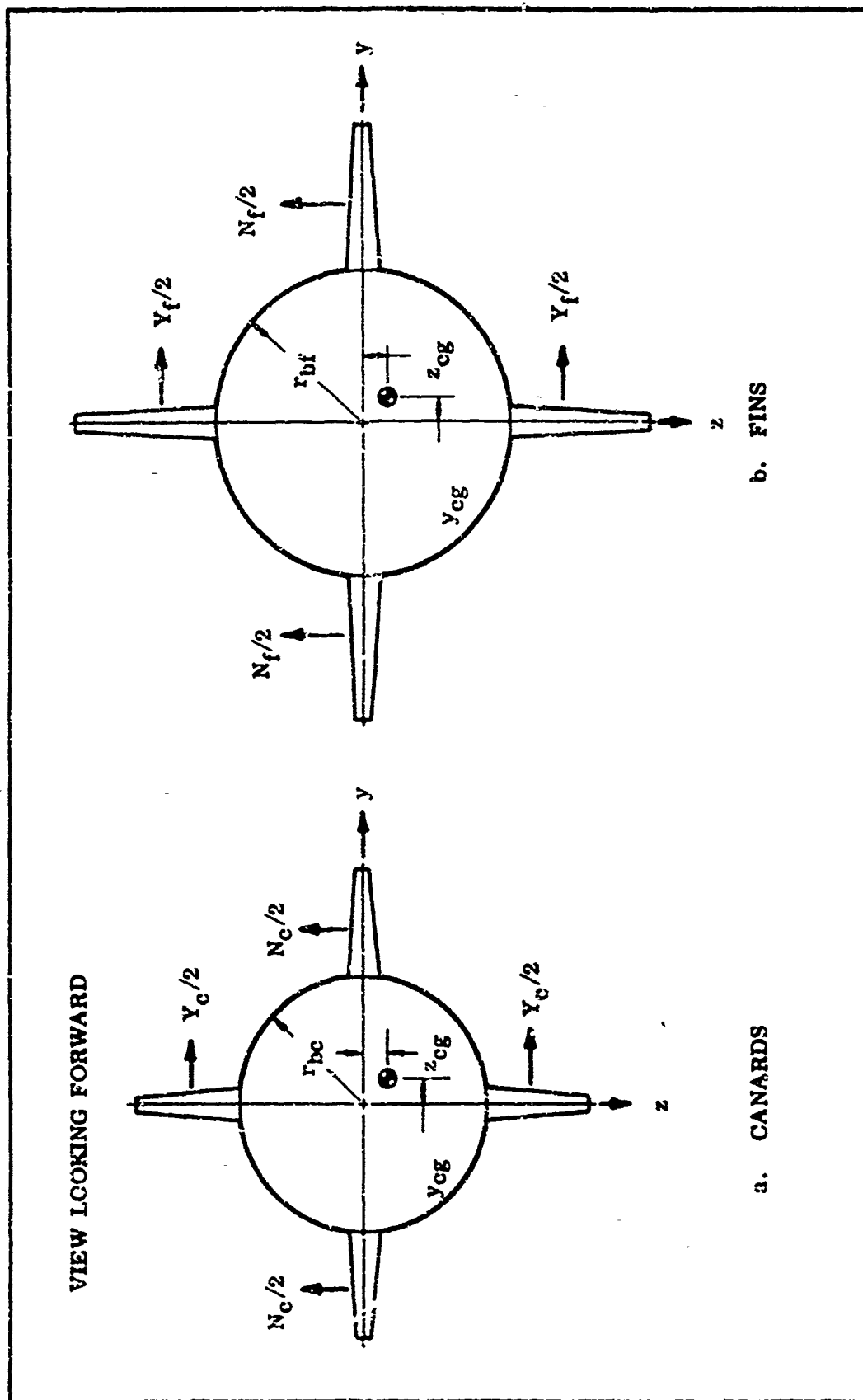


Figure 10. Cruciform Configuration

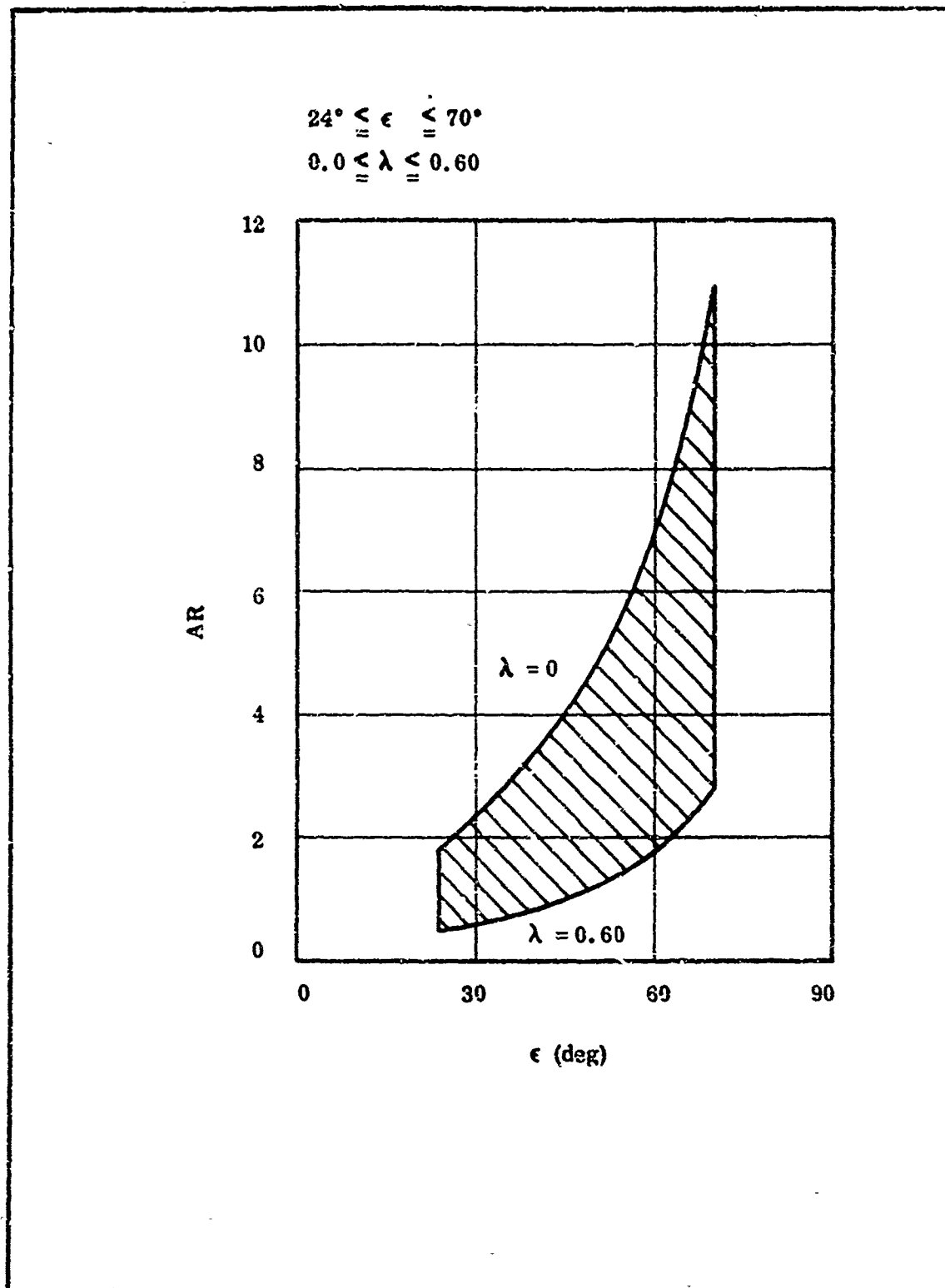


Figure 11. Range of Aspect Ratios Accommodated
for Calculation of $C_{L\alpha}$

3. DETERMINATION OF PARAMETERS

An examination of the equations which define the static forces and moments will show that values must be determined for the parameters $C_{L\alpha}$, C_1 , C_{DO} , K_L , S_{exp} and α_{cp} . Values of the parameters versus Mach number must be determined for each set of surfaces.

$C_{L\alpha}$

The linear value of lift curve slope for canards and fins is determined versus Mach number. For subsonic values of Mach number, $0 \leq M \leq 1.0$, $C_{L\alpha}$ is determined from Figure 12 as a function of $\sqrt{1-M^2} \tan \epsilon_L$ and taper ratio, λ ; and for supersonic Mach numbers, $M > 1.0$, $C_{L\alpha}$ is determined from Figure 13 and the equation shown on that figure as a function of $\sqrt{M^2-1}$ AR and taper ratio. The parameter determined in this manner is $C_{L\alpha}/AR$ per radian, and to produce $C_{L\alpha}$ per degree use the equation below:

$$C_{L\alpha} = \left(\frac{C_{L\alpha}}{AR} \right) \frac{AR}{57.3} \quad (44)$$

Data provided for the above will accommodate values of PAR up to 109.34788 which corresponds to a condition of $M = 10.0$, $AR = 10.98988$ and $\lambda = 0$.

C_1

The parameter C_1 is defined as the nonlinear lift curve factor and is obtained from Figure 14 for the appropriate aspect ratio.

C_{DO}

The drag coefficient at zero lift, C_{DO} , is composed of two components, friction drag coefficient, C_{DF} , and form or pressure drag coefficient, C_{DP} . For incompressible flow, the form drag coefficient is small enough relative to the friction drag coefficient, that the parameter C_{DO} for $M < 1.0$ is defined as follows:

$$C_{DO} = \frac{1.11 C_{DF}}{\sqrt{1-M^2}} \quad M < 1.0 \quad (45)$$

The above is limited to the case where $M < 1.0$, therefore, another definition for C_{DO} must be used for the case where $M > 1.0$, thus

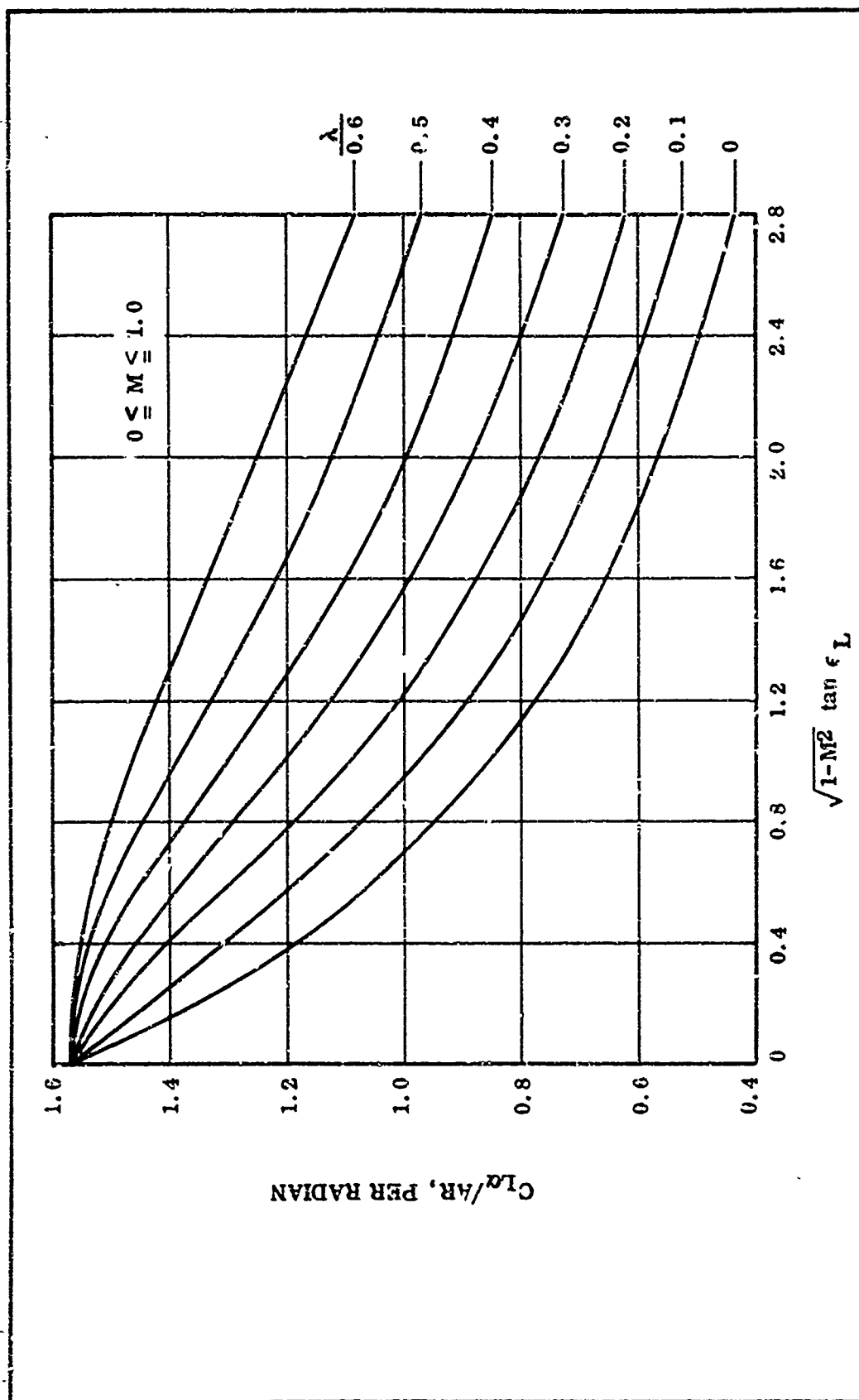


Figure 12. Subsonic Linear Lift Curve Slope

SUPERSONIC LINEAR LIFT CURVE SLOPE

For $\sqrt{M^2-1} AR > 4.0$ Use

$$(C_{L\alpha}/AR)_1 = (C_{L\alpha}/AR)_0 (\beta_0/\beta_1)$$

Where

$(C_{L\alpha}/AR)_1$ Is Value When $\sqrt{M^2-1} AR > 4.0$

$(C_{L\alpha}/AR)_0$ Is Value When $\sqrt{M^2-1} AR = 4.0$

$\beta_0 = \sqrt{M^2-1}$ When $\sqrt{M^2-1} AR = 4.0$

$\beta_1 = \sqrt{M^2-1}$ When $\sqrt{M^2-1} AR > 4.0$

$$(\sqrt{M^2-1} AR)_{max} = 102.14788$$

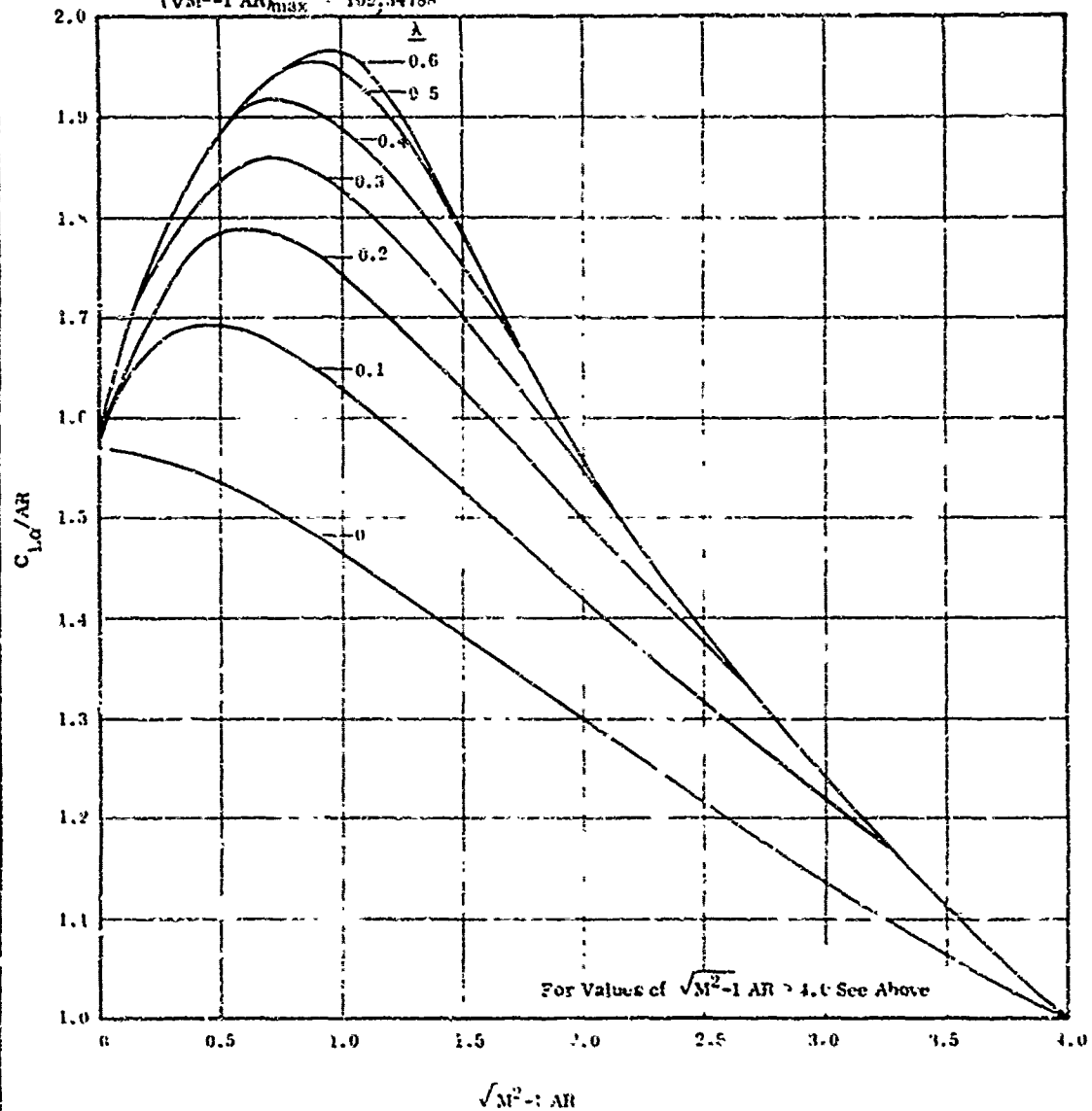


Figure 13. Supersonic Linear Lift Curve Slope

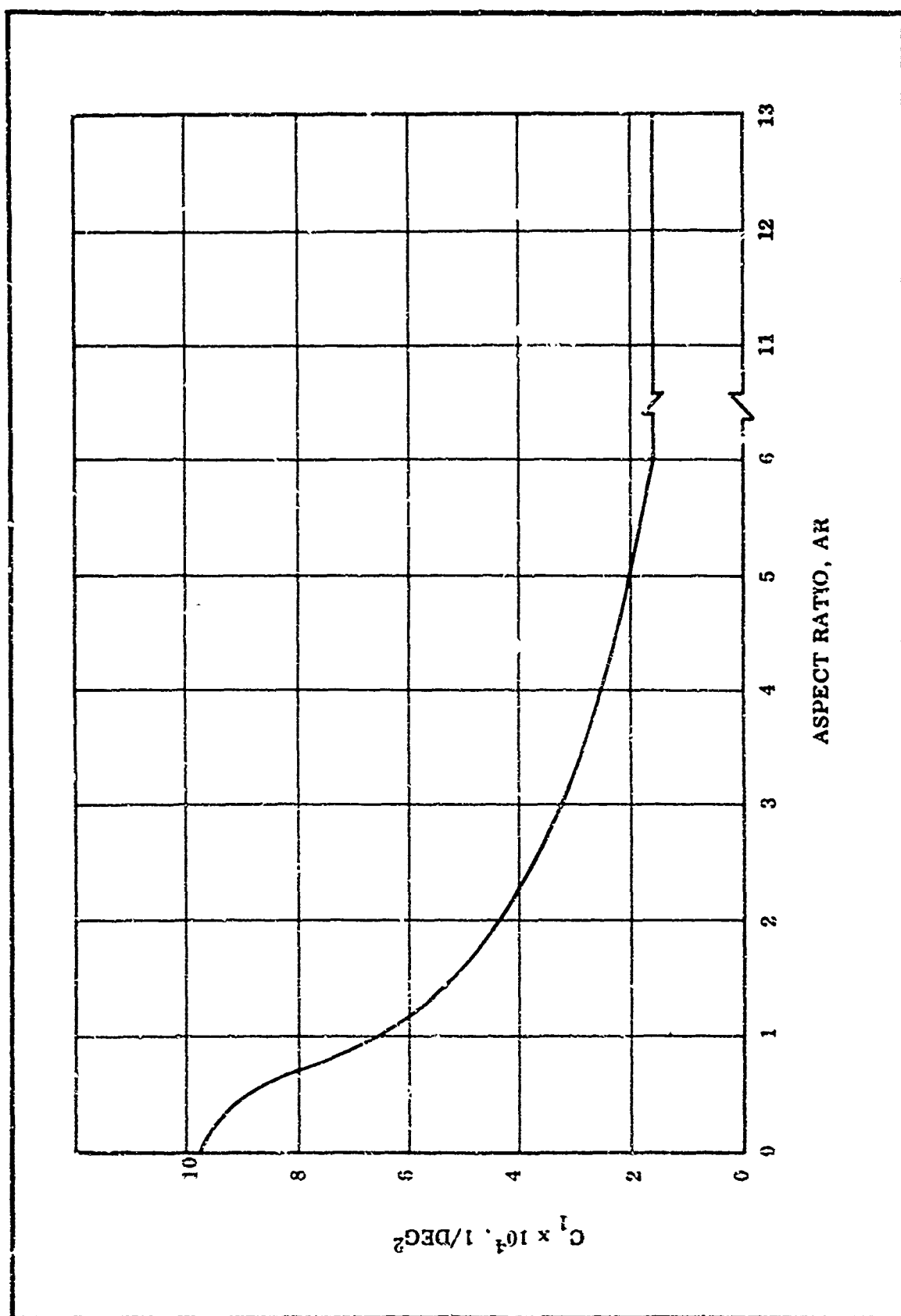


Figure 14. Nonlinear Lift Factor

$$C_{Df} = C_{DF} + C_{DP} \quad M > 1.0 \quad (46)$$

where

$$C_{DP} = F_D \tau^2 \left\{ B(10)^{CAR^i} \left[(M - 0.9) + DAR^j \right]^{EAR^k} \right\} \quad (46a)$$

with

$$\begin{aligned} B &= 0.51393 & i &= -0.79948 \\ C &= 0.35801 & j &= -1.4767 \\ D &= 1.65 & k &= -0.1765 \\ E &= -1.0613 & K_D &= 5.743 \end{aligned}$$

The friction drag coefficient C_{DF} is a function of Reynolds number and wetted area and is determined in the following manner.

- For a given Mach number and type of missile, determine R_N/FT from Table 9.
- Calculate \bar{c} in feet

$$\bar{c} = \frac{c_R}{18} \left(1 + \frac{\lambda^2}{1 + \lambda} \right) \quad (47)$$

where c_R is in inches

- Calculate R_N

$$R_N = (R_N/FT) \bar{c} \quad (48)$$

- For given M and corresponding R_N , calculate C_f from equation 49

$$C_f = \left[\frac{0.455}{(\log_{10} R_N)^{2.58}} \right] \left[(1 + 0.162 M^2)^{-0.58} \right] \quad (49)$$

or, for hand calculations, C_f may be obtained from Figure 15.

- Calculate C_{DF}

$$\begin{aligned} C_{DF} &= C_f \frac{A_{WET}}{S_{Exp}} \\ &= 2C_f \end{aligned} \quad (50)$$

TABLE 9

VARIATION OF REYNOLDS NUMBER PER FOOT VERSUS MACH NUMBER

| Mach Number | $(R_N/FT)10^{-6}$ * | | | |
|----------------|---------------------|------|------|--------|
| | (1) | (2) | (3) | (4) |
| 0.0 | 3.70 | 3.30 | 3.55 | 1.976 |
| 0.50 | 3.70 | 3.30 | 3.55 | 1.976 |
| 0.75 | 5.25 | 4.62 | 4.68 | 2.964 |
| 0.95 | 6.25 | 5.55 | 5.45 | 3.754 |
| 1.00 | 6.50 | 5.77 | 5.55 | 3.952 |
| 1.25 | 7.47 | 6.57 | 6.21 | 4.940 |
| 1.50 | 8.22 | 7.13 | 6.75 | 5.928 |
| 2.00 | 9.02 | 7.87 | 7.40 | 7.904 |
| 2.60 | 9.20 | 8.21 | 7.50 | 10.275 |
| 3.00 | 8.90 | 8.15 | 7.04 | 11.856 |
| 4.00 | 7.00 | 6.70 | 4.52 | 15.808 |
| 5.00 | 4.75 | 4.85 | 2.62 | 19.760 |
| 6.00 | 3.10 | 3.40 | 1.44 | 23.712 |
| 8.00 | 1.05 | 1.18 | 0.48 | 31.616 |
| 10.00 | 0.45 | 0.42 | 0.30 | 39.520 |

*

- (1) Small Ballistic Missile
- (2) Large Ballistic Missile
- (3) Large Booster Vehicle
- (4) Small Air Launched Missile

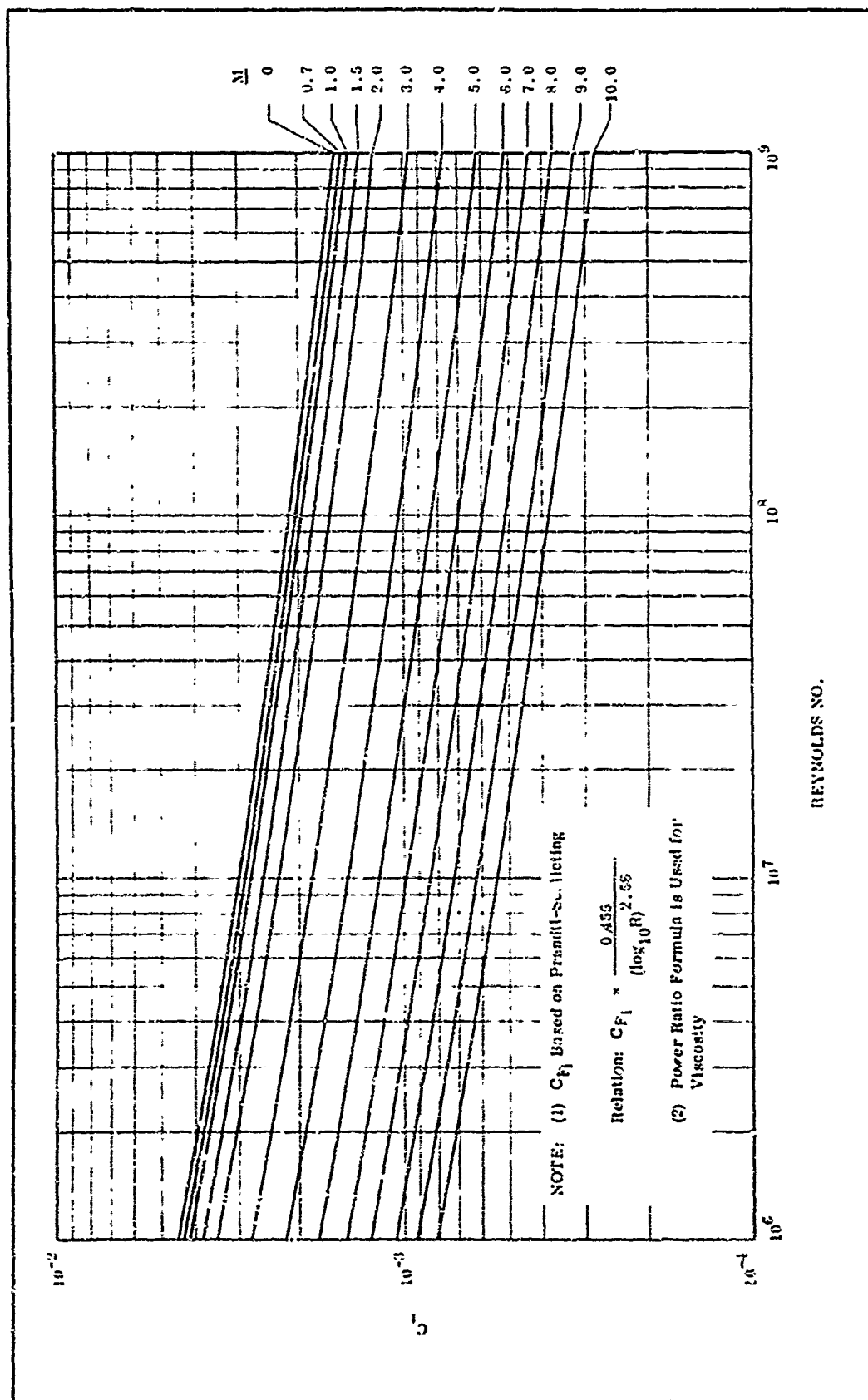


Figure 15. Turbulent Skin Friction Coefficient for Insulated Flat Plate

K_L

The drag due to lift factor, K_L , describes the shape of the drag polar as a function of C_L^2 and, combined with C_{D0} , provides the drag coefficient of the lifting surface. As used in this procedure, the following definition applies.

$$K_L = \frac{1}{C_{L\alpha}} \quad (51)$$

where $C_{L\alpha}$ is in radian units.

S_{Exp}

The exposed planform area, S_{Exp} , is defined as the planform area of the lifting surface which exists external to the body and is calculated from the equation below.

$$S_{Exp} = (1 - \lambda^2) c_R^2 \tan \epsilon_L \quad (52)$$

x_{cp}

The longitudinal location of the lifting surface center of pressure is defined in inches of missile body station and is determined from the equations below as a function of geometric location and Mach number.

$$x_{cp} = x_{or} + \bar{x}_{LE} + K_{cp} \bar{c} \quad (53)$$

where

$$\begin{aligned} \bar{x}_{LE} &= \frac{\bar{y}}{\tan \epsilon_L} \\ &= \frac{(1 + 2\lambda)(1 - \lambda) c_R}{3(1 + \lambda)} \end{aligned} \quad (54)$$

and

$$\bar{c} = \frac{2}{3} c_R \left(1 + \frac{\lambda^2}{1 + \lambda}\right)$$

and K_{cp} is determined as a function of Mach number from Figure 16.

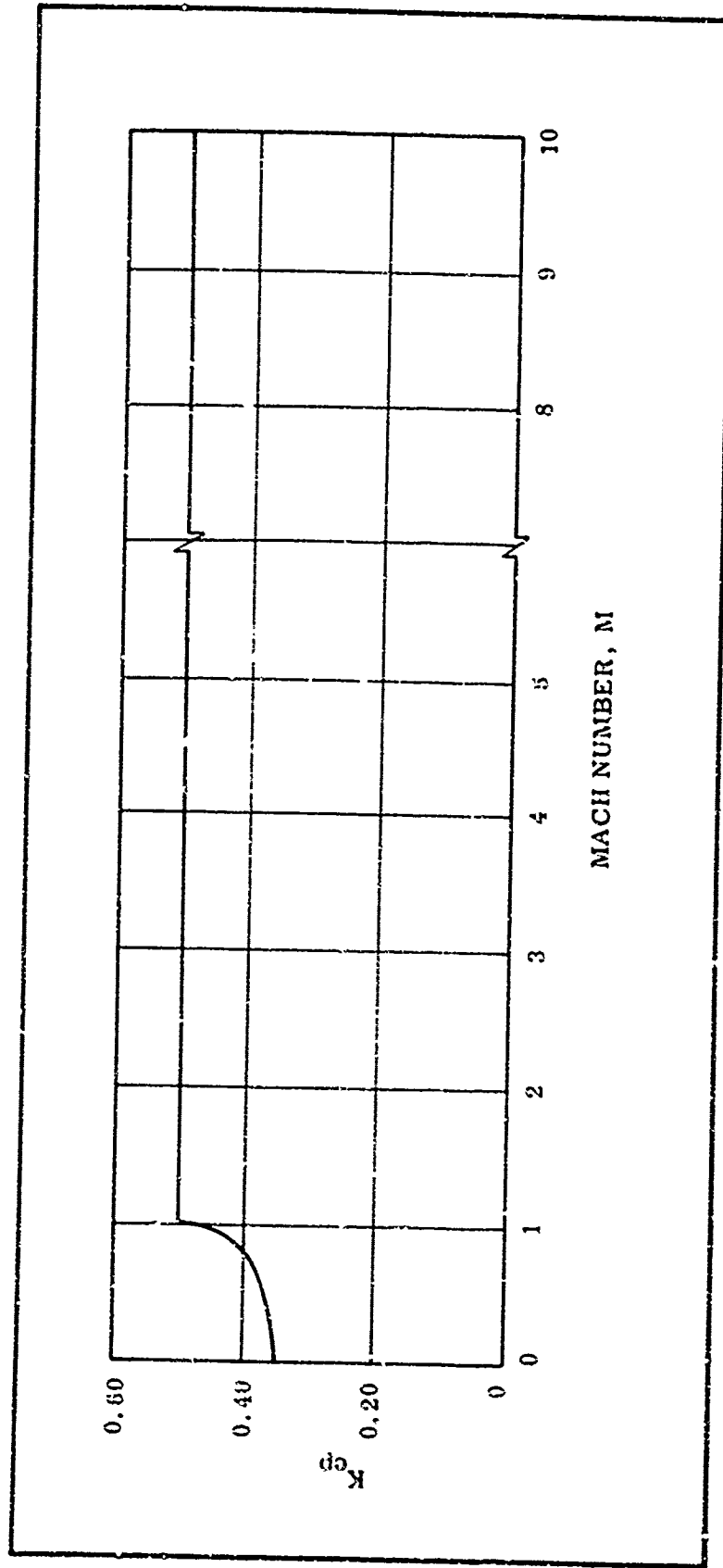


Figure 16. Center of Pressure Factor

y_{cp} and z_{cp}

The spanwise center of pressure is determined from the basic assumption that the spanwise loading distribution over the lifting surfaces is elliptical in shape at all Mach numbers. With this assumption then, the center of pressure is a constant fraction of the lifting surface semi-span, b/2, and the definition below will be used.

$$y_{cp} = r_b + 0.42441 (b/2) \quad (56)$$

and

$$z_{cp} = r_b + 0.42441 (b/2) \quad (57)$$

For application in the controls section of the trajectory subroutine, it is desired that the center of pressure and hinge line be referenced from the root chord leading edge in fraction of the root chord. This can be accomplished by using the equations below.

$$\frac{x_{cp}}{c_R} = \frac{x_{LE} + K_{cp} \bar{c}}{c_R} \quad (58)$$

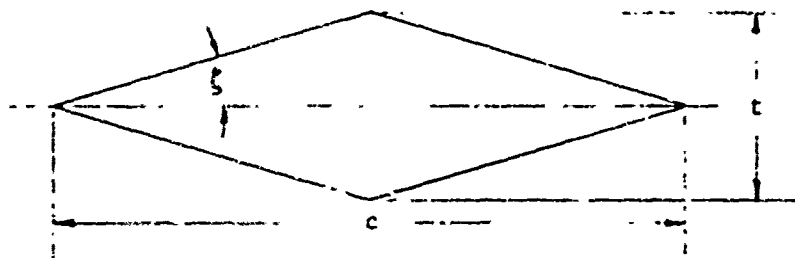
$$\frac{x_H}{c_R} = \frac{x_H - x_{or}}{c_R} \quad (59)$$

4. LIFTING SURFACE WEIGHT AND CENTER-OF-GRAVITY

The weight and center of gravity of the lifting surfaces, as formulated below, will be based on a symmetric double wedge type airfoil section. The volume of material for each fin will be calculated assuming a solid airfoil section. The resulting weight will be calculated from the volume and the density of the material used. An option between two materials, steel and aluminum alloy, is provided.

Using the approach of a solid airfoil section for the lifting surfaces will provide an estimate of what should be a near maximum weight for a set of canards or fins in a cruciform configuration.

a. Lifting Surface Weight



$$t = \tau c \quad (60)$$

$$\text{I.N. } \zeta = \frac{t}{2} / \frac{c}{2} = \frac{t}{c} \quad (61)$$

Gross Sectional Area

$$A = (4) \left(\frac{1}{2}\right) \left(\frac{t}{2}\right) \left(\frac{c}{2}\right) \quad (62)$$

$$= \frac{1}{2} tc$$

$$= \frac{1}{2} \tau c^2$$

$$\text{Where } \tau = \frac{t}{c}$$

$$c = x_{TE} - x_{LE} \quad (63)$$

$$x_{TE} = x_{or} + c_R \quad (64)$$

$$x_{LE} = x_{or} + y \cot \epsilon_L \quad (65)$$

$$c = c_R - y \cot \epsilon_L \quad (66)$$

$$\begin{aligned} \text{VOL} &= 4 \int_0^{b/2} A_{x\text{-sect}} dy \\ &= 4 \int_0^{b/2} \frac{1}{2} \tau c^2 dy \\ &= 2\tau \int_0^{b/2} (c_R - y \cot \epsilon_L)^2 dy \\ &= 2\tau \left[c_R^2 y - 2c_R \cot \epsilon_L \frac{y^2}{2} + \frac{y^3}{3} \cot^2 \epsilon_L \right]_0^{b/2} \\ &= \tau \left[bc_R^2 - \frac{1}{2} c_R b^2 \cot \epsilon_L + \frac{1}{12} b^3 \cot^2 \epsilon_L \right] \end{aligned} \quad (67)$$

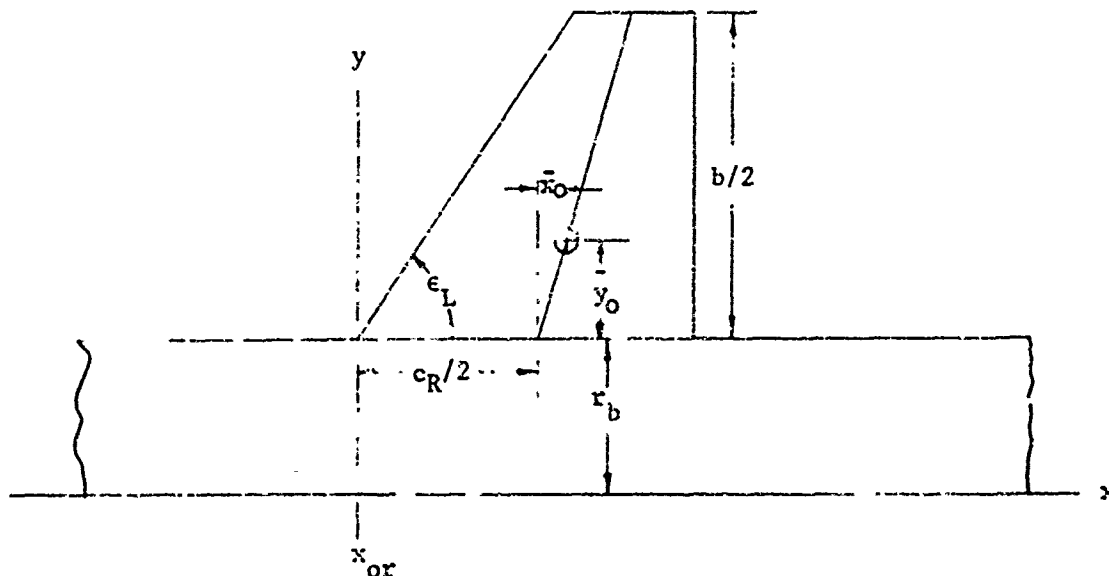
$$\begin{aligned} \text{WT} &= (\rho) (\text{VOL}) \\ &= \tau \rho \left[bc_R^2 - \frac{1}{2} c_R b^2 \cot \epsilon_L + \frac{1}{12} b^3 \cot^2 \epsilon_L \right] \end{aligned} \quad (68)$$

Where ρ is determined from

| Material | Density $\frac{\rho}{\text{lb/in}^3}$ |
|----------------|--|
| Aluminum Alloy | .101 |
| Steel | .286 |

b. Lifting Surface Center-of-Gravity

The center of gravity of each lifting surface will be calculated using the same assumption of a solid airfoil section as for the weight calculation. The coordinate system is as shown in the sketch below with the equations following.



Longitudinal Location of Center of Gravity

$$\bar{x} = x_{or} + c_R/2 + \bar{x}_0 \quad (69)$$

$$\bar{x}_0 = \frac{\text{Moment of Fin Volume about } c_R/2 \text{ Axis}}{\text{Volume per Fin}} \quad (70)$$

The volume per fin, as defined for the weight calculation, is

$$\text{Vol} = \int_0^{b/2} A_{x\text{-sect}} dy \quad (71)$$

$$\begin{aligned}
 Vol &= \int_0^{b/2} \frac{1}{2} (c_R - y \cot \epsilon_L)^2 dy \\
 &= \frac{1}{16} [4c_R^2 - 2b^2 c_R \cot \epsilon_L + \frac{1}{3} b^3 \cot^2 \epsilon_L]
 \end{aligned} \tag{72}$$

and the moment about an axis at $c_R/2$ normal to the x axis is

$$Mom_x = Vol \cdot \bar{x}_0 \tag{73}$$

$$\bar{x}_0 = \frac{Mom_x}{Vol} \tag{74}$$

$$Mom_x = \int_0^{b/2} A_{x\text{-sect}} \bar{x}_i dy \tag{75}$$

where $\bar{x}_i = y/2 \cot \epsilon_L$

$$\begin{aligned}
 Mom_x &= \int_0^{b/2} \frac{1}{2} (c_R - y \cot \epsilon_L)^2 (y/2 \cot \epsilon_L) dy \\
 &= \int_0^{b/2} \frac{1}{4} (c_R^2 y \cot \epsilon_L - 2y^2 c_R \cot^2 \epsilon_L + y^3 \cot^3 \epsilon_L) dy \\
 &= \frac{1}{32} [b^2 c_R^2 \cot \epsilon_L - \frac{2}{3} b^3 c_R \cot^2 \epsilon_L + \frac{1}{8} b^4 \cot^3 \epsilon_L]
 \end{aligned} \tag{76}$$

thus

$$\bar{x}_0 = \frac{[b^2 c_R^2 \cot \epsilon_L - \frac{2}{3} b^3 c_R \cot^2 \epsilon_L + \frac{1}{8} b^4 \cot^3 \epsilon_L]}{2[4bc_R^2 - 2b^2 c_R \cot \epsilon_L + \frac{1}{3} b^3 \cot^2 \epsilon_L]} \tag{77}$$

Lateral Location of Center of Gravity

$$\bar{Y} = r_b + \bar{y}_0 \tag{78}$$

$$\bar{y}_0 = \frac{\text{Moment of Fin Volume about } c_R}{\text{Volume per Fin}} \tag{79}$$

The volume per fin is as defined before, and the moment about an axis parallel to the x axis and located at the root chord of the surface is

$$\text{Mom}_y = \text{Vol} \cdot \bar{y}_0 \quad (80)$$

$$\bar{y}_0 = \frac{\text{Mom}_y}{\text{Vol}} \quad (81)$$

$$\text{Mom}_y = \int_0^{b/2} A_{x\text{-sect}} \bar{y}_i dy \quad (82)$$

where $y_i = y$

Thus

$$\text{Mom}_y = \int_0^{b/2} \frac{\tau}{2} (c_R - y \cot \epsilon_L)^2 dy$$

$$= \int_0^{b/2} \frac{\tau}{2} (y c_R^2 - 2y^2 c_R \cot \epsilon_L + y^3 \cot^2 \epsilon_L) dy$$

$$= \frac{\tau}{16} [b^2 c_R^2 - \frac{2}{3} b^3 c_R \cot \epsilon_L + \frac{1}{8} b^4 \cot^2 \epsilon_L] \quad (83)$$

and

$$\bar{y}_0 = \frac{[b^2 c_R^2 - \frac{2}{3} b^3 c_R \cot \epsilon_L + \frac{1}{8} b^4 \cot^2 \epsilon_L]}{[4b c_R^2 - 2b^2 c_R \cot \epsilon_L + \frac{1}{3} b^3 \cot^2 \epsilon_L]} \quad (84)$$

As the cruciform configuration is symmetrical then \bar{z}_0 is numerically equal to \bar{y}_0 , therefore

$$\bar{z}_0 = \bar{y}_0 \quad (85)$$

5. EQUATIONS FOR LIFTING SURFACE GEOMETRIC PARAMETERS

$$\epsilon_T = 90.0^\circ \quad (1A)$$

$$\lambda = \frac{c_T}{c_R} \quad (2A)$$

$$AR = \frac{4 (b/2)^2}{S_{Exp}} = \frac{4 \tan \epsilon_L (1-\lambda)}{1+\lambda} \quad (3A)$$

$$\bar{c} = \frac{2}{3} c_R \left(1 + \frac{\lambda^2}{1+\lambda}\right) \quad (4A)$$

$$\bar{y} = \frac{(1+2\lambda)(1-\lambda)}{3(1+\lambda)} c_R \tan \epsilon_L \quad (5A)$$

$$\bar{x}_{LE} = \bar{y} \cot \epsilon_L \quad (6A)$$

$$x_{LE} = y \cot \epsilon_L \quad (7A)$$

$$x_{TE} = c_R \quad (8A)$$

$$c = x_{TE} - x_{LE} = c_R - y \cot \epsilon_L \quad (9A)$$

$$\frac{b}{2} = (1 - \lambda) c_R \tan \epsilon_L \quad (10A)$$

$$S_{Exp} = 2\left(\frac{b}{2}\right) \left(\frac{c_R + c_T}{2}\right) = (1 - \lambda^2) c_R^2 \tan \epsilon_L \quad (11A)$$

$$S_{ref} = \frac{\pi}{\lambda} d_{ref}^2 \quad (12A)$$

$$x_{ce} = \frac{[3 - (1 - \lambda)^2] c_R}{3(1 + \lambda)} \quad (13A)$$

$$y_{ce} = \left[\frac{1 + \lambda - 2\lambda^2}{3(1 + \lambda)} \right] c_R \tan \epsilon_L \quad (14A)$$

6. NOMENCLATURE

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|---|-----------------|
| A | Axial Force in Missile Axis System Also, Area | lb sq in. |
| A_{WET} | Surface Area | sq in. |
| A_{x-sect} | Area of Airfoil Cross-Section | sq in. |
| AR | Lifting Surface Aspect Ratio | dim. |
| b/2 | Lifting Surface Semi-Span (y distance From Body External Contour to Lifting Surface Tip Chord | in. |
| B | Constant in Equation 46a | dim. |
| c | Length of Lifting Surface Chord | in. |
| c_R | Length of Lifting Surface Root Chord | in. |
| c_T | Lifting Surface Tip Chord | in. |
| \bar{c} | Length of Mean Aerodynamic Chord | in. |
| C | Constant in Equation 46a | dim. |
| C_{DF} | Friction Drag Coefficient | dim. |
| C_{DL} | Lifting Surface Drag Due to Lift Coefficient | dim. |
| C_{D0} | Lifting Surface Drag Coefficient at Zero Lift | dim. |
| C_f | Flat Plate Friction Drag Coefficient | dim. |
| C_A | Axial Force Coefficient in Missile Axis System | dim. |
| C_D | Drag Coefficient | dim. |
| C_{DP} | Pressure Drag Coefficient | dim. |
| C_L | Lift Coefficient | dim. |
| $C_{L\alpha}$ | Slope of Lifting Surface Linear Lift Coefficient Curve | 1/deg, 1 RAD |

| | | |
|---------------|---|--------------------|
| C_N | Normal Force Coefficient in Pitch Plane of the Missile Axis System | dim. |
| $C_{N\alpha}$ | Slope of Normal Force Coefficient | 1/deg |
| C_Y | Normal Force Coefficient in Yaw Plane of the Missile Axis System | dim. |
| C_l | Non-Linear Lift Coefficient Factor | 1/deg ² |
| d_{ref} | Reference Diameter (Diameter of Largest Cylindrical Section of Missile Body) | in. |
| dy | Differential Length in y | in. |
| D | Constant in Equation 46a | dim. |
| E | Constant in Equation 46a | dim. |
| Fwd | Forward | dim. |
| $(HM)_y$ | Hinge Moment in Pitch Plane | in.-lb |
| $(HM)_z$ | Hinge Moment in Yaw Plane | in.-lb |
| i | Constant in Equation 46a | dim. |
| j | Constant in Equation 46a | dim. |
| k | Constant in Equation 46a | dim. |
| K_{cp} | Factor Locating Lifting Surface Center of Pressure as a Fraction of \bar{c} Measured From the Leading Edge of \bar{c} | dim. |
| K_D | Constant in Equation 46a | dim. |
| K_L | Drag Due to Lift Factor | rad |
| M | Mach Number | dim. |
| M_b | Moment Due to Body Aerodynamic Forces | in.-lb |
| M_c | Moment Due to Canard Aerodynamic Forces | in.-lb |
| M_f | Moment Due to Fin Aerodynamic Forces | in.-lb |
| M_x | Moment About x Axis | in.-lb |
| M_y | Moment About y Axis | in.-lb |

| | | |
|------------------|--|--------------|
| M_z | Moment About z Axis | in.-lb |
| Mom | Moment | in.-lb |
| Mom _x | Longitudinal Moment of Lifting Surface Weight About Midpoint of Root Chord | in.-lb |
| Mom _y | Lateral Moment of Lifting Surface Weight About Root Chord | in.-lb |
| N | Normal Force in the Pitch Plane of the Missile Axis System | lb |
| q | Dynamic Pressure ($= \frac{\gamma}{2} \rho M^2$) | psf |
| r_b | Average Radius of Missile Body Between the Root Chord Leading and Trailing Edges | in. |
| R_N | Reynolds Number | dim. |
| S | Planform Area Per Pair of Lifting Surfaces | sq in./sq ft |
| S_{Exp} | Area of Two Lifting Surface Semi-Spans Outside the Body External Contour | sq in./sq ft |
| S_{ref} | Missile System Reference Area ($= \pi d_{ref}^2 / 4$) | sq in./sq ft |
| t | Thickness of Airfoil Section (Lifting Surface) | in. |
| V | Relative Velocity | fps |
| Vol | Volume of Set of Lifting Surfaces (4 Semi-Spans) | cu in. |
| Wt | Weight of Set of Lifting Surfaces (4 Semi-Spans) | lb |
| x | Longitudinal Distance | in. |
| x_{ce} | Longitudinal Distance the Planform Centroid Lies Aft of Root Chord Leading Edge | in. |
| x_{cp} | Longitudinal Location of Center of Pressure | in. |
| x_e | Body Station at End of Aft Skirt | in. |
| x_{or} | Body Station of Lifting Surface Root Chord Leading Edge | in. |
| x_l | Longitudinal Location of Hinge Axis (Canards and Fins) | in. |
| x_{LE} | Distance of Lifting Surface Leading Edge From x_{or} | in. |

| | | |
|----------------|--|-----|
| x_{TE} | Distance of Lifting Surface Trailing Edge From x_{or} | in. |
| \bar{x} | Distance Between Component Center of Pressure and Missile Center of Gravity | in. |
| x_h | Longitudinal Distance Between Center of Pressure and Hinge Axis | in. |
| \bar{x}_o | Longitudinal Distance of Lifting Surface Center of Gravity from Root Chord Midpoint | in. |
| \bar{x}_{LE} | Distance Lifting Surface Mean Aerodynamic Chord Leading Edge Lies Behind Root Chord Leading Edge | in. |
| x_1 | Body Station of Missile Body Theoretical Nose | in. |
| \bar{X} | Longitudinal Location of Lifting Surface Center of Gravity Relative to Body Station 0.0 | in. |
| y | Lateral Distance | in. |
| y_{ce} | Lateral Distance the Planform Centroid for one Semi-Span lies Outboard From the Root Chord | in. |
| y_{cp} | Lateral Location of Lifting Surface Center of Pressure Relative to Vehicle Centerline Axis | in. |
| Y | Normal Force in the Yaw Plane of the Missile Axis System | lb |
| \bar{y} | Lateral Distance of Mean Aerodynamic Chord From Root Chord | in. |
| \bar{y}_o | Lateral Distance of Lifting Surface Center of Gravity from Root Chord | in. |
| \bar{y}_b | y Distance of Missile cg From Body Centerline | in. |
| \bar{y}_h | Lateral Distance Between Center of Pressure and Hinge Axis | in. |
| \bar{Y} | Lateral Location of Lifting Surface Center of Gravity Relative to Vehicle Centerline Axis | in. |
| z | Vertical Distance | in. |
| z_{cp} | Vertical Location of Lifting Surface Center of Pressure Relative to Vehicle Centerline Axis | in. |
| \bar{z}_b | z Distance of Missile cg From Body Centerline | in. |
| \bar{z}_h | Vertical Distance Between Center of Pressure and Hinge Axis | in. |

| | | |
|-------------|--|------|
| \bar{z}_0 | Vertical Distance of Lifting Surface Center of Gravity From Root Chord | in. |
| \bar{z} | Vertical Location of Lifting Surface Center of Gravity Relative to Vehicle Centerline Axis | in. |
| \bar{z} | Centerline | dim. |

| | | |
|----------------|--|-------------|
| α | Angle of Attack in Pitch Plane | deg |
| α_{eff} | Effective Angle of Attack in Pitch Plane (Canards and Fins) | deg |
| β | Angle of Attack in Yaw Plane $\sqrt{M^2-1}$ (Where $1.0 < M \leq 10.0$) | deg dim. |
| β_{eff} | Effective Angle of Attack in Yaw Plane (Canards and Fins) | deg |
| γ | Ratio of Specific Heats | dim. |
| δ | Deflection Angle of Lifting Surface | deg |
| ϵ_L | Complement of Lifting Surface Leading Edge Sweep-Back Angle | deg |
| ϵ_T | Complement of Lifting Surface Trailing Edge Sweep-Back Angle | deg |
| ζ | Surface Angle of Airfoil Section Relative to Chord Plane (Double Wedge Section) | deg |
| λ | Lifting Surface Taper Ratio ($=c_T/c_R$) | dim. |
| π | 3.1416 | dim. |
| ρ | Density | lb/cu in. |
| τ | Thickness Ratio of Airfoil Section ($=t/c$) | dim. |

7. SUBSCRIPTS

| | |
|----|--------------------------|
| b | Body |
| c | Canard |
| cg | Center of Gravity |
| cP | Canard for Pitch Control |
| cY | Canard for Yaw Control |
| f | Fin |
| fP | Fin for Pitch Control |
| fY | Fin For Yaw Control |
| P | In Pitch Plane |
| Y | In Yaw Plane |

SECTION III

SIX DEGREES OF FREEDOM TRAJECTORY PROGRAM

A. INTRODUCTION

This document describes a versatile digital trajectory program developed by the Wasatch Division of Thiokol Chemical Corporation. The program was developed, as are most programs, in an evolutionary manner. As a result, most of the general capabilities are the result of past experience, thus making the program well adapted to most forms of missile system flight simulation.

The equations and logic permit the simulation of missile flight in three dimensions with an additional three degrees of freedom possible, i.e., the vehicle can pitch, yaw, and roll about its center-of-gravity. A spherical rotating earth model is utilized for missile location. The gravitational forces are calculated from an oblate earth model.

The program has three general capabilities in three dimensions:

(a) flight simulation of a rigid body point mass missile system, (b) flight simulation of a rigid body missile system with angular momentum considered plus attitude stability provided by a closed loop control system, and (c) flight simulation of a rigid body point mass missile system with a quasi-attitude control system which exactly balances the disturbing pitching moments. These three capabilities are primarily used in (1) performance requirements for analysis, (2) vehicle control requirements determination, and (3) vehicle stability, control and loads analysis, respectively.

Vehicle launch can occur at any azimuth and altitude and from any latitude and longitude. The vehicle is commanded with respect to an inertial system which does not rotate with the earth. Flight path through the atmosphere can be commanded by (1) input turning rates, (2) gravity turn equations, (3) steering

equations whose coefficients are determined internally, (4) rail launch equations, (5) constant altitude equations, (6) constant normal load factor equations, (7) intercept guidance equations, and (8) homing guidance equations. These different methods of flight path control can be changed for different parts of the flight, thus allowing wide variations in flight path determination and accurate results with relative ease by the user.

Program input is minimal, the input complexity being dictated by the sophistication the user wishes to employ. Mandatory input includes the missile launch conditions, data describing the flight path desired, and data describing missile characteristics. Missile characteristics include weight, thrust history, specific impulse, exit area, and aerodynamic coefficients versus Mach number. Up to four discrete propulsion stages can be simulated.

Missile thrust is computed from an input thrust history table and atmospheric back pressure. Instantaneous weight is a function of stage initial weight, weight flow, thrust, and propellant vacuum specific impulse. The capability of simulating simultaneous operation of motors having different characteristics is available by the use of separate tabular input.

A pintle nozzle thrust modulation control motor can be simulated. This thrust control system logic is broken into two separate parts: (1) the command thrust logic and (2) the controllable motor thrust dynamics. The command thrust logic or thrust control law provides the needed thrust command for the motor so the missile system will achieve the desired trajectory conditions. The criteria for evaluating the commanded thrust is established by flight performance parameters such as a specified velocity history, stipulated Mach number, commanded turning rates, minimum velocity, constrained dynamic pressure or line of sight rate.

The actual motor thrust dynamic is based on the solution of the time rate of change of chamber pressure equation. This equation is a function of nozzle throat area, internal gas properties, free volume, burning surface area, and propellant burning rate characteristics. The instantaneous vacuum thrust is evaluated from the pintle throat area and the motor chamber pressure. The motor

ballistic characteristics are evaluated from one of the three input options: (a) thrust time table, (b) chamber pressure table, or (c) surface area-web depth fraction table.

The effective thrust gimbal point can be located at any place about the missile. Pitch, yaw, and roll moments of inertia are specified as functions of instantaneous vehicle weight.

Pitch and yaw thrust vectoring are obtained from first or second order transfer functions or from an infinite autopilot gain model. Roll control results from the operation of a system separate from the main propulsive one. A first-order transfer function is used to simulate a bang-bang with deadband or proportional roll control system. Pitch, yaw, and roll control system commands can be generated by vehicle attitude errors, rates, and steady state errors.

The controlling pitch, yaw and roll moments are determined for each computed interval. The required thrust vector slew rate, duty cycle, and other thrust vector control requirements are evaluated for the TVC design stage.

Aerodynamic forces are functions of Mach number, input aerodynamic coefficients, and angle of attack. Up to a third degree normal force slope coefficient can be used. The angles of attack are modified so that flight with values up to 180 degrees can be simulated with axial forces going to zero at ± 90 degrees and normal forces zero at 0 and 180 degrees. Normal force center of pressure is a function of Mach number. Aerodynamic damping forces and moments are determined from input coefficients, rate change of angle of attack, pitch rate, and dynamic pressure.

Movable aerodynamic control fins can be simulated. Fin aerodynamic characteristics are determined from input fin lift and drag coefficient plus center of pressure and hinge location.

Dynamic forces include gravity, thrust, jet damping, and aerodynamic. The dynamics include overturning moments created by differences in thrust level

of individual motors in a clustered solid propellant rocket motor stage. These moments are determined by statistical techniques from the cluster geometry and single motor variances in burning time and total impulse.

Program options which provide utility to the users are special print capabilities, flexibility in inputting thrust time curves, variable methods of terminating a propulsion stage, and an efficient and highly sophisticated hunting procedure. The hunting procedure can maximize, minimize or isolate any dependent variable subject to a maximum of seven constraint conditions.

1. DIAGRAMS

The more important symbols with geometric interpretation are shown on Figures 17 thru 29.

2. DEFINITIONS

Input, output, and internal program parameters are designated by symbols defined in this section.

a. General Comments--Parameter units required by program logic or for input are abbreviated as follows:

| | | | |
|-----|---------------------|-----|---------------|
| dbi | Determined by input | lb | Pound |
| deg | Degree | min | Minutes |
| dim | Dimensionless | nm | Nautical mile |
| ft | Feet | rad | Radian |
| in. | Inch | sec | Second |

Multipliers are associated with many of the input parameters. Since only the unit of the product of the parameter and multiplier is specified by program logic, the units of the parameter, and multiplier are an option of the program user. Dimensions are designated dbi for parameters which have optional units. Units of the

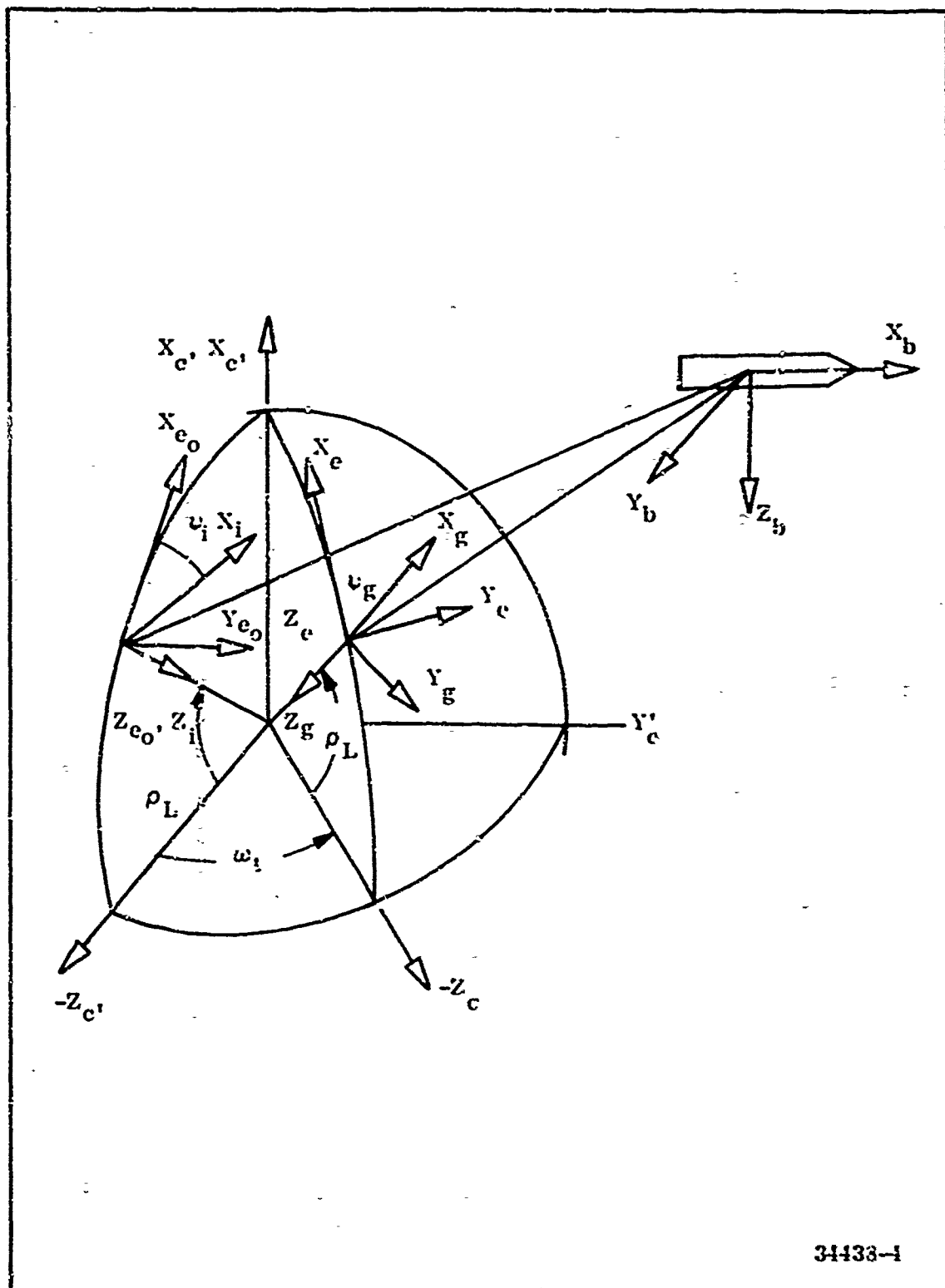


Figure 17. 3-D Coordinate Systems

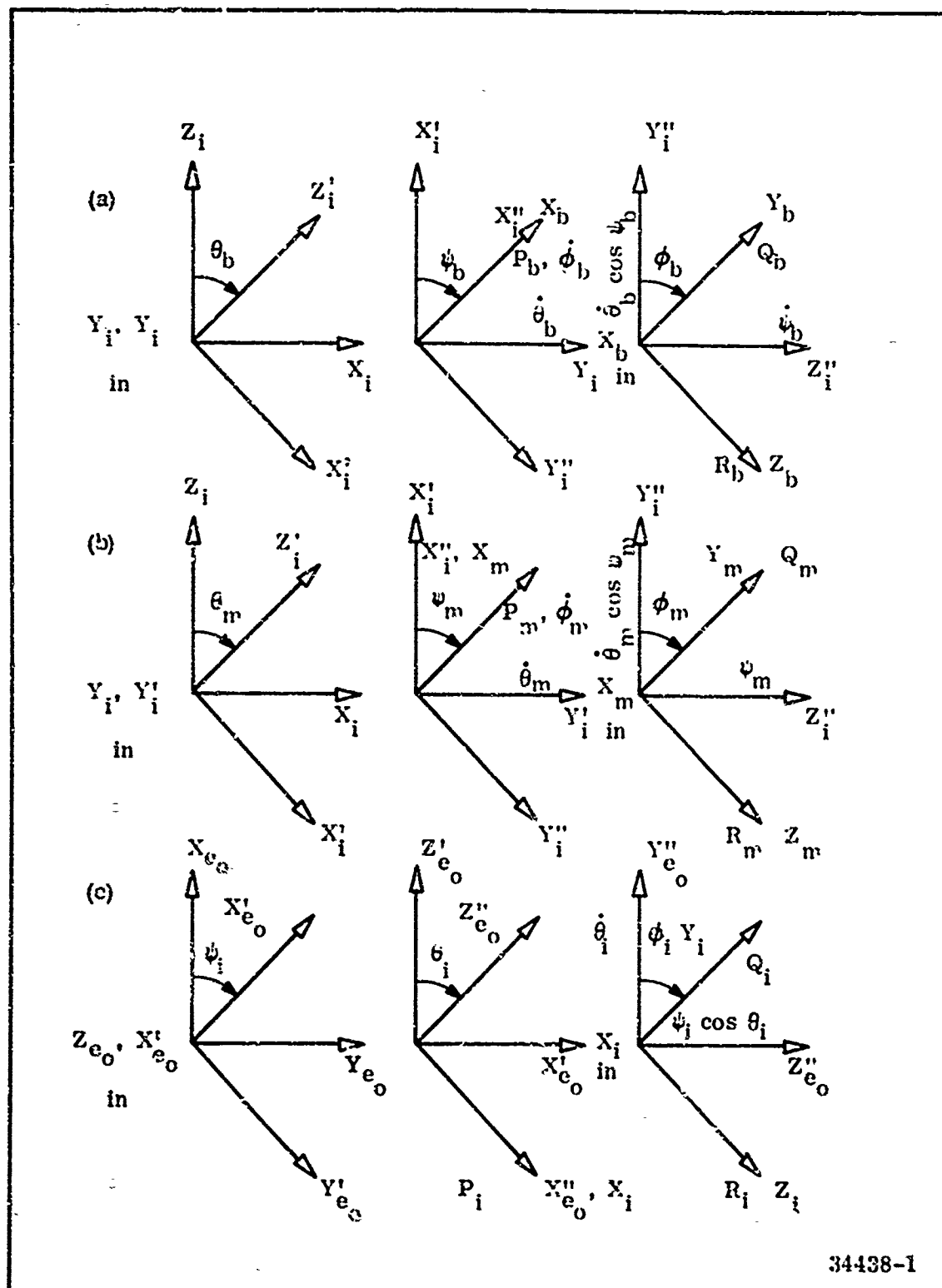


Figure 18. Euler Angles

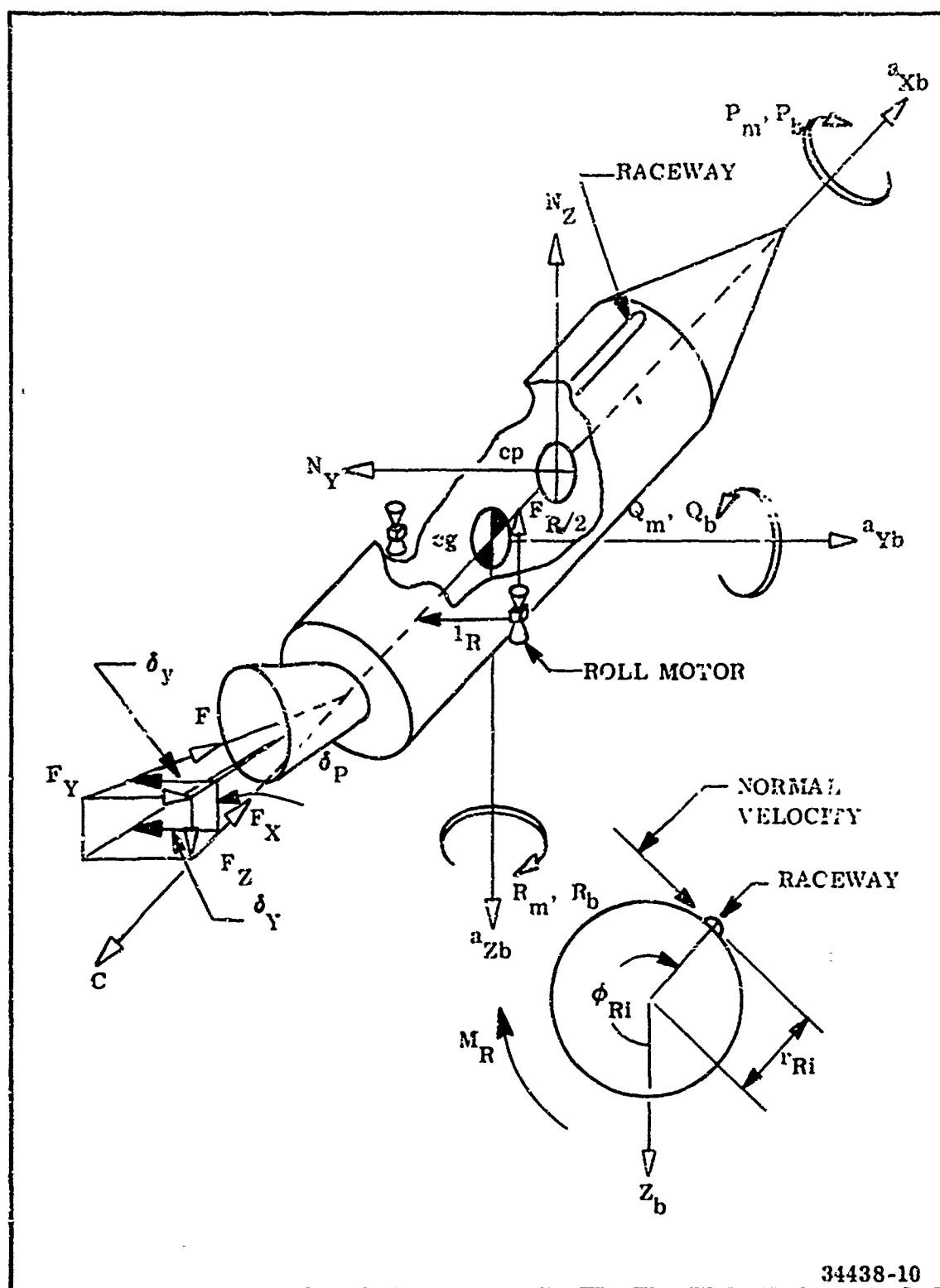
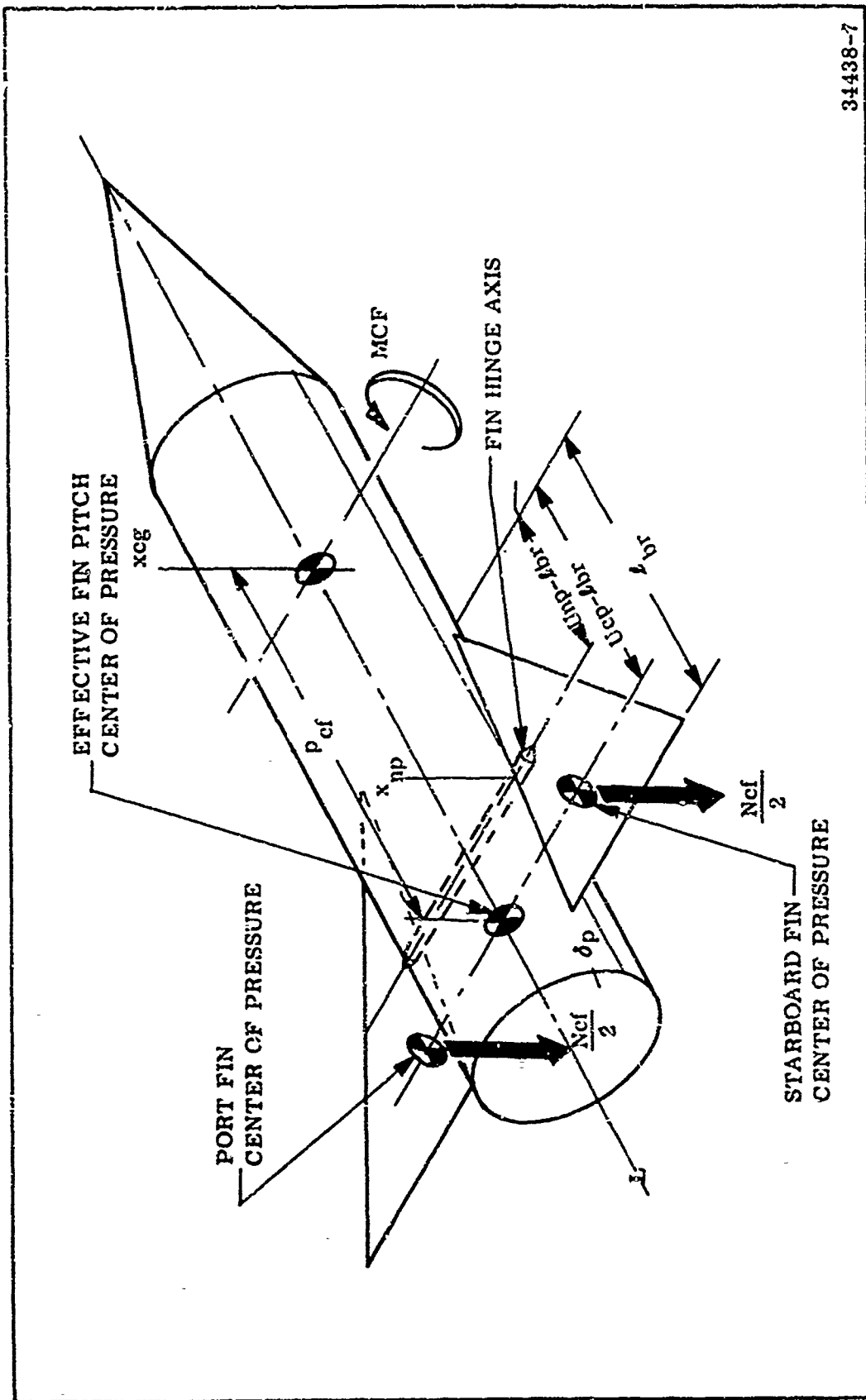
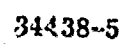


Figure 19. Forces and Rates



34438-7

Figure 20. Aerodynamic Control Fin Schematic



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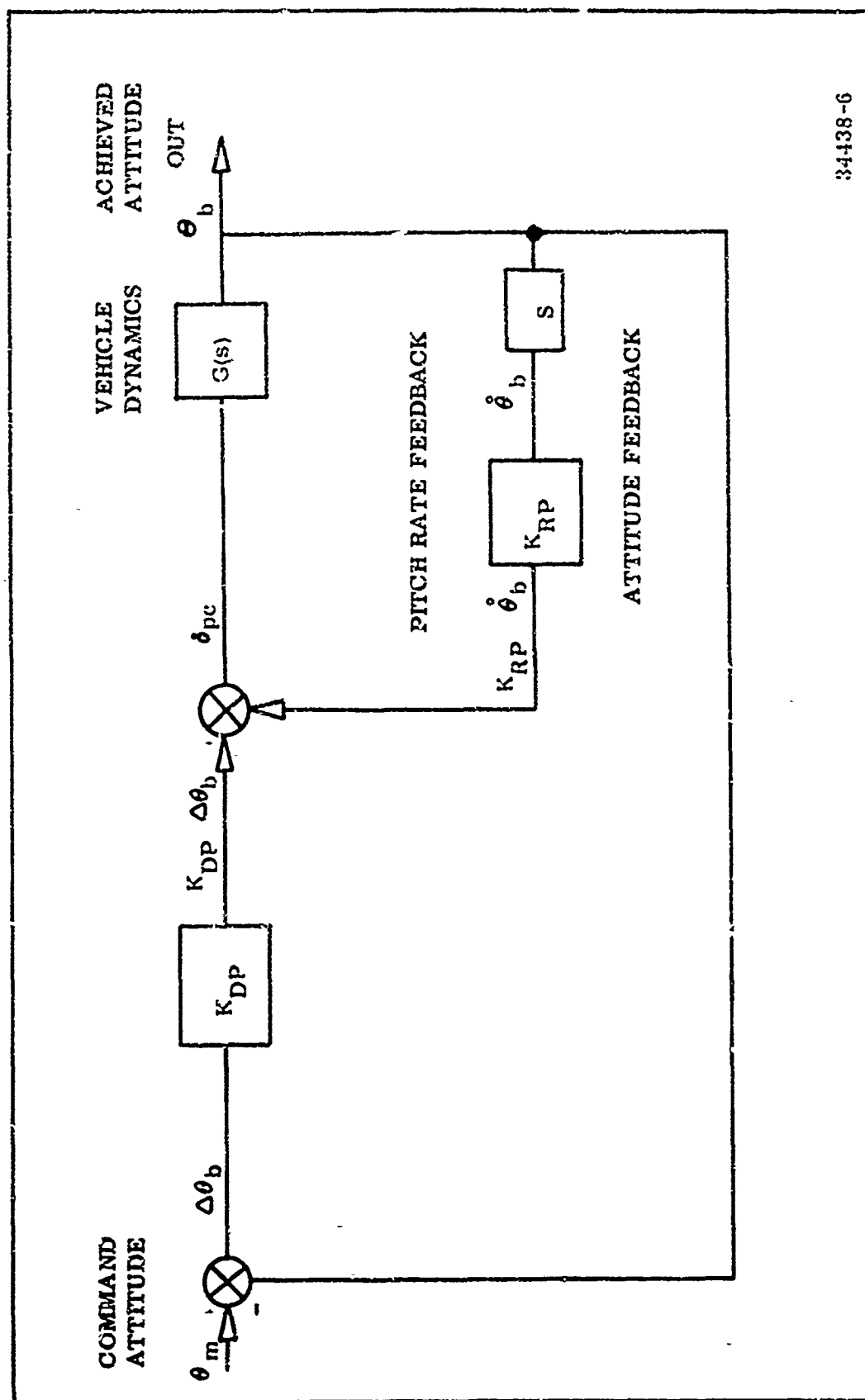


Figure 22. Control Loop Diagram

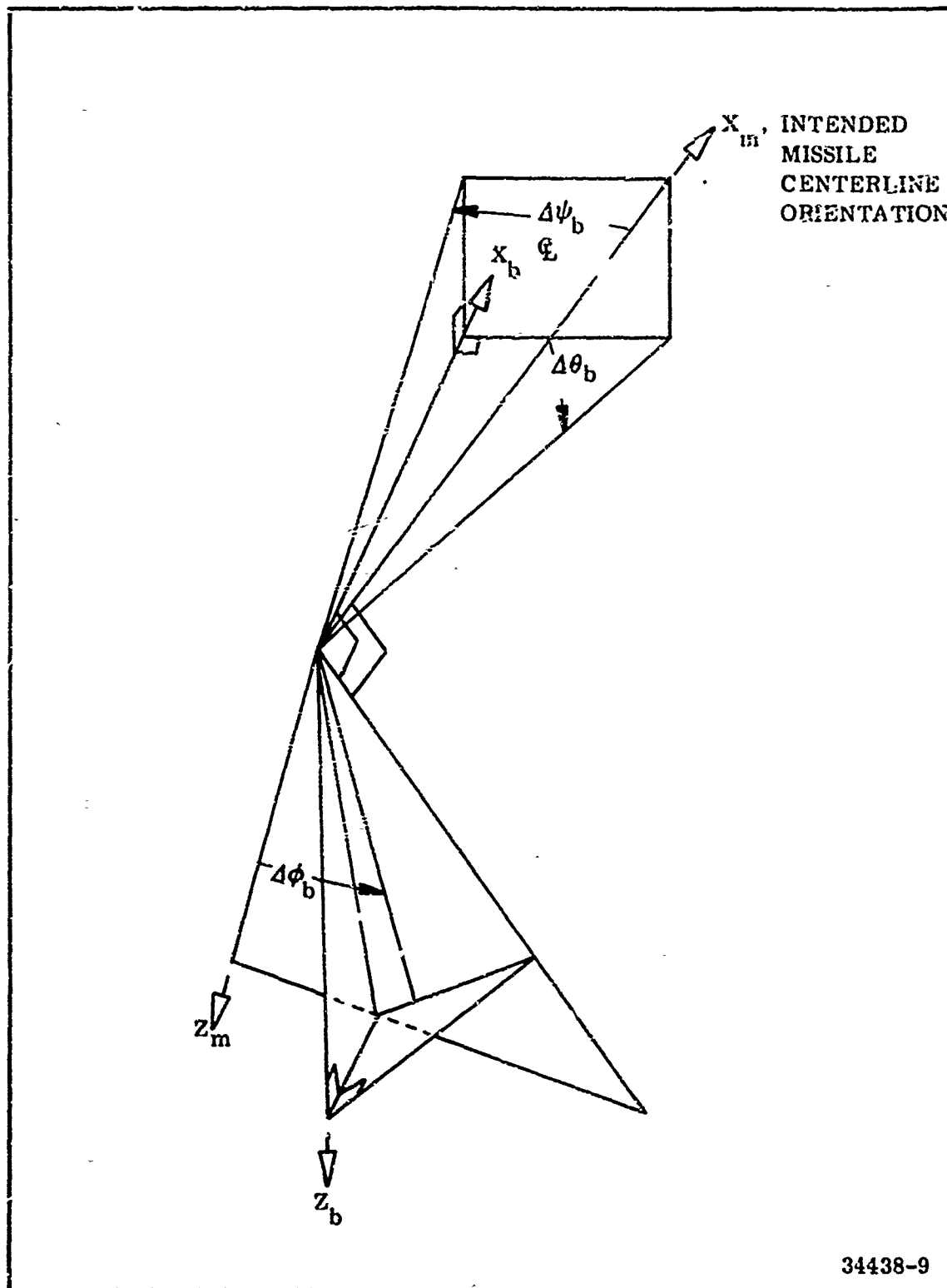


Figure 23. Vehicle Attitude Errors

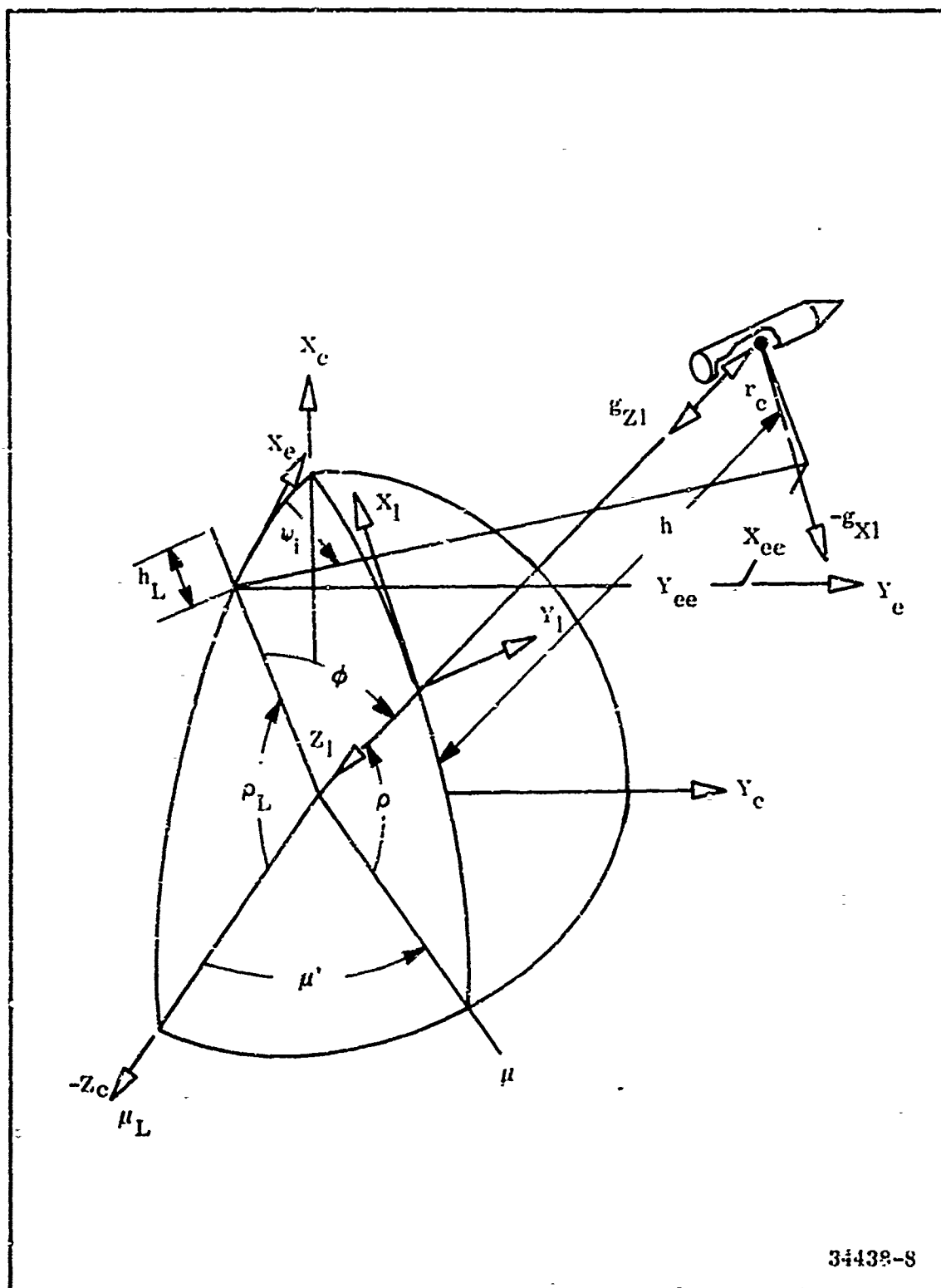
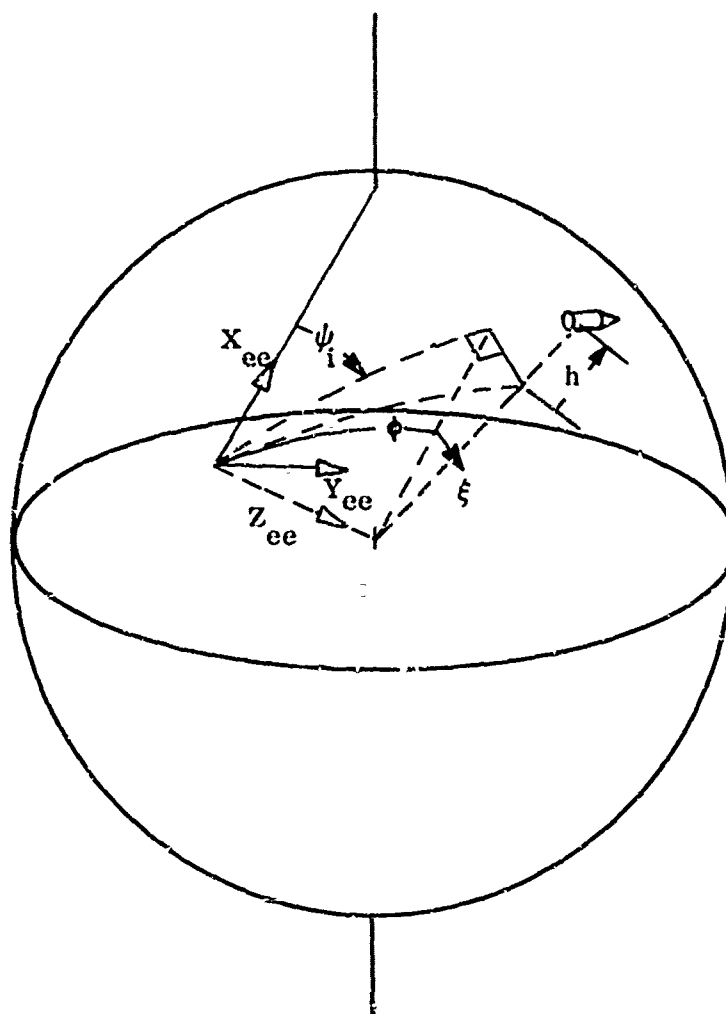


Figure 24. 3-D Missile Location



34438-12

Figure 25. 3-D Down Range-Cross Range Coordinates

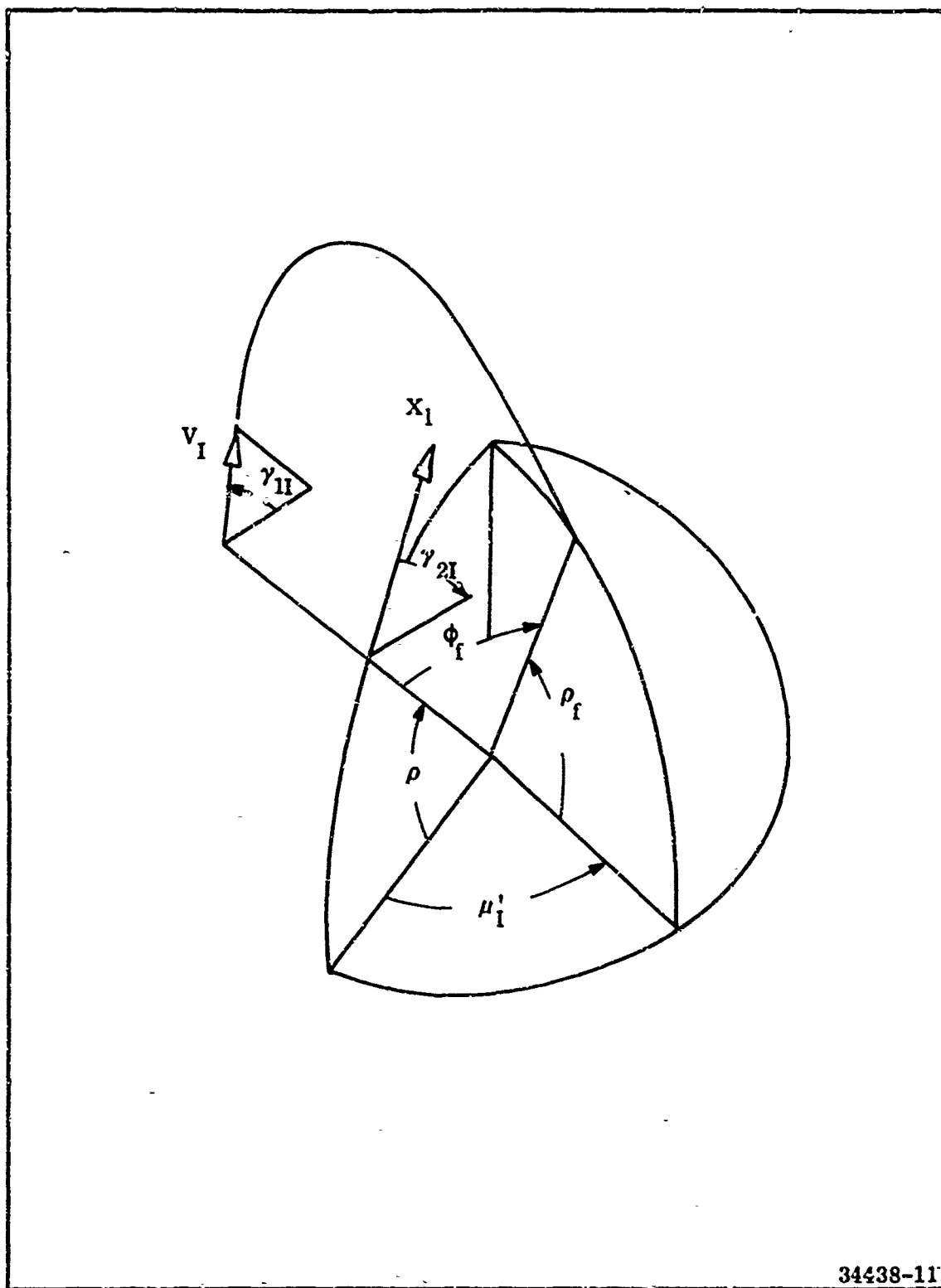
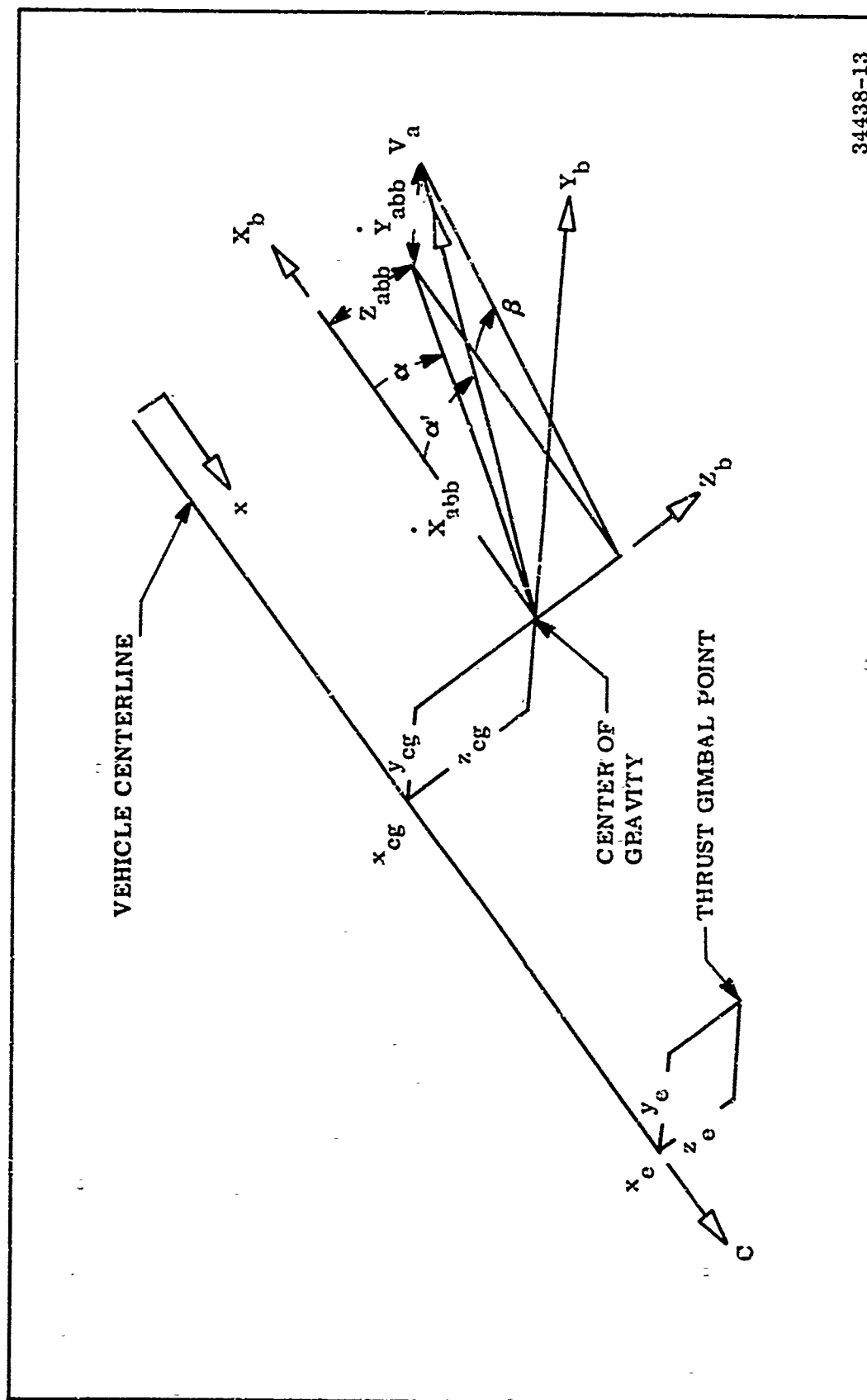


Figure 26. Impact Parameters



34438-13

Figure 27. 3-D Angles of Attack

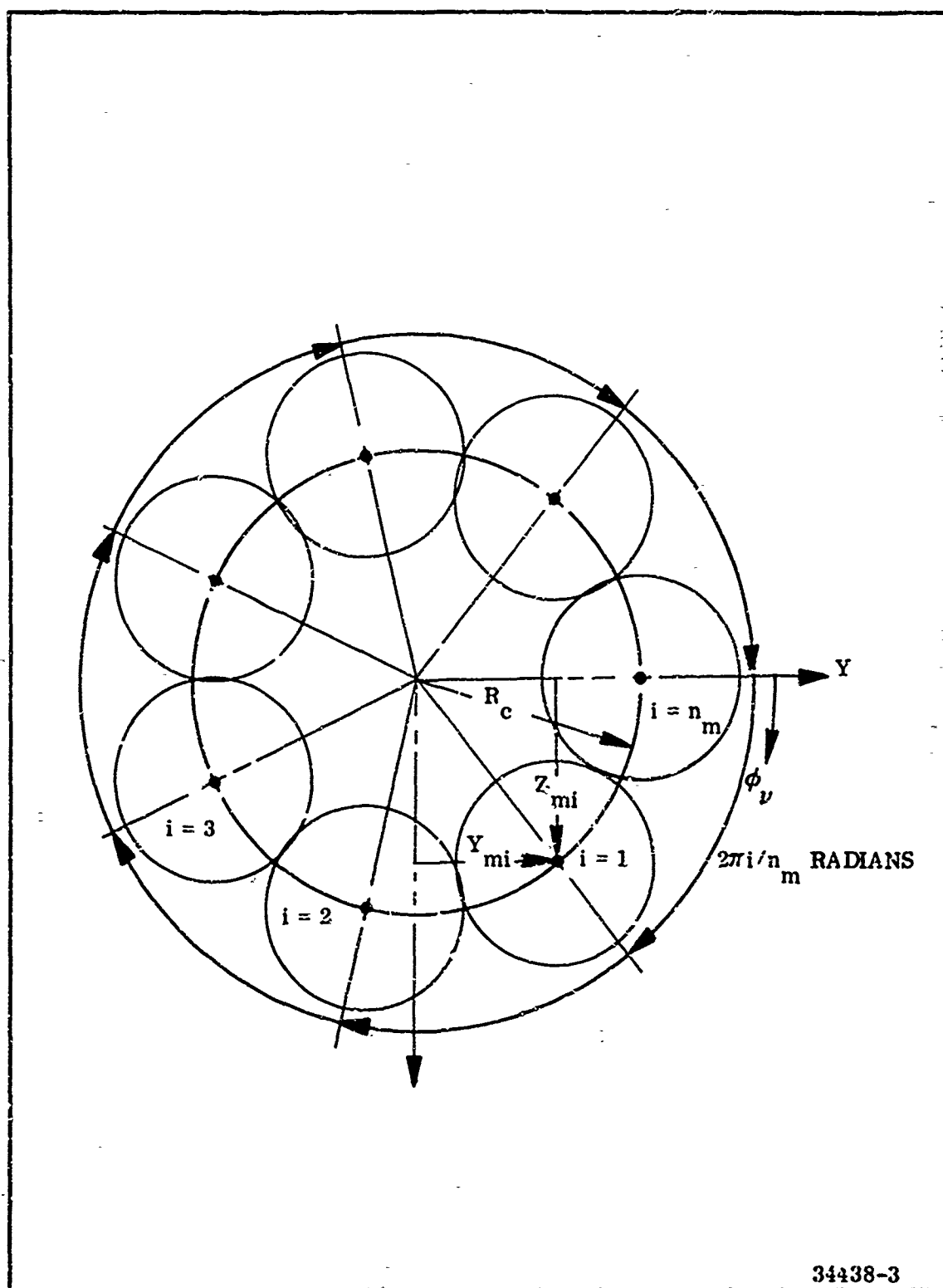
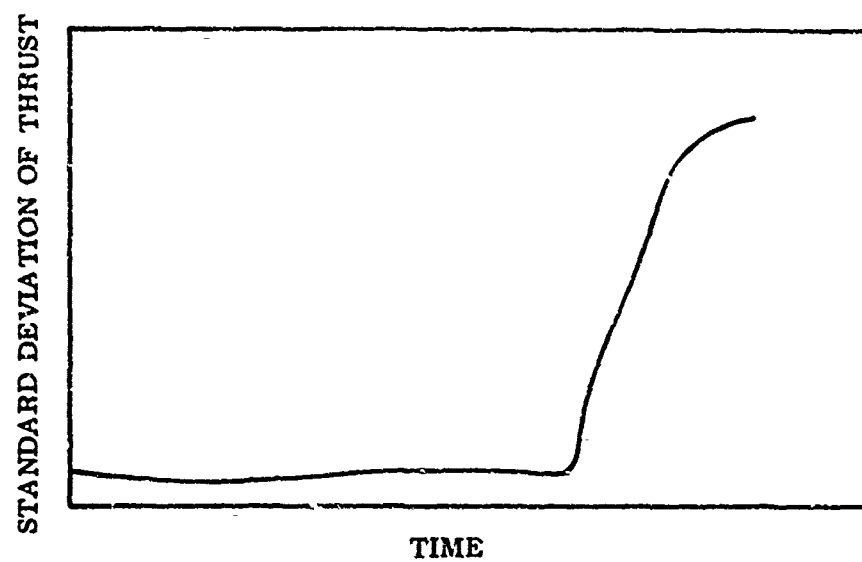
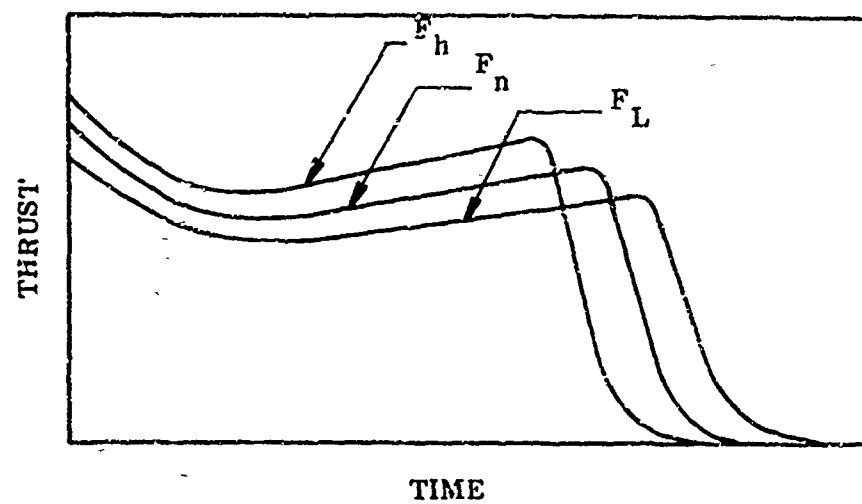


Figure 28. Clustered Motor Configuration



34438-2

Figure 29. Typical Variation of Thrust History

parameters used by the program should be noted so that the proper units are the same.

Because of the four-stage capability of the program, many parameters are applicable for each stage. When further clarification is necessary, the subscript k is shown with the symbol of the parameter.

Two tables, for a main stage and a complementary stage, are available for inputting thrust, weight, and weight flow data. Parameters which apply to one or the other table are referenced accordingly.

b. Coordinate System--Coordinates are referenced to right-handed Cartesian systems having X, Y, and Z with lower-case subscripts as the coordinate axis. For example, the e system has coordinates axis \vec{X}_{ee} , e.g., X_{ee} represents a value along the appropriate coordinate axis. In some instances, vector and matrix notation are used to simplify the writing of equation; i.e.,

$$\vec{X}_{ee} = X_{ee} \vec{i} + Y_{ee} \vec{j} + Z_{ee} \vec{k} = \begin{Bmatrix} X_{ee} \\ Y_{ee} \\ Z_{ee} \end{Bmatrix}$$

where \vec{i} , \vec{j} , and \vec{k} are unit vector parallel to the coordinate axis X_{ee} , Y_{ee} , and Z_{ee} , respectively.

The coordinate systems discussed below have coincident origins; i.e., no translation is involved in their relations with other systems. However, defining them with their origins at the conceptual locations rather than all simply rotated about one another is convenient. Furthermore, velocity and acceleration components would be affected only by rotation and not translation. The coordinate systems are shown in the illustrations appearing in Section III. A. 1 and are defined as follows:

Systems

Definitions

- b Missile orientation coordinates. Origin is fixed at the vehicle center-of-gravity with X_b parallel to the vehicle centerline, positive forward. As seen from the rear of the vehicle Z_b is positive down.
- e Earth fixed system whose origin is located at sea level at the launch latitude and longitude. The X axis is positive north, the Y_e axis is positive east, and the Z_e axis is along the launch vertical, positive down.
- e_0 Initially coincident with the e system, but does not rotate with the earth.
- g Earth fixed, launch centered, azimuth oriented coordinate system. The orientation of this system about the e system is specified by the input Euler angles ψ_g , θ_g , and ϕ_g .
- i Origin is coincident with the e_0 system. The orientation of this system is specified by input Euler angles ψ_i , θ_i , and ϕ_i .
- ee \vec{X}_{ee} and $\dot{\vec{X}}_{ee}$ are the components of missile acceleration and velocity in a right-handed Cartesian coordinate system whose origin is fixed at sea level at the input launch latitude, ρ_L and longitude μ_L . The X_e axis is positive north, Y_e axis positive east, and Z_e , the vertical axis, positive down. This coordinate system is the one in which the equations of linear motion are integrated.

\vec{X}_{ee} is defined in section B.1 as the linear momenta equations.

$$\vec{X}_{ee} = \vec{X}_{ee0} + \int_{t_0}^t \dot{\vec{X}}_{ee} dt$$

$$\dot{\vec{X}}_{ee} = \dot{\vec{X}}_{ee0} + \int_{t_0}^t \ddot{\vec{X}}_{ee} dt$$

- eo $\dot{\vec{X}}_{eo}$ are the components of velocity which are initially coincident with the e system, but do not rotate with the earth. Components in this system are not calculated directly because the eo system is an intermediate system in evaluating the missile achieved and commanded components.

$$\dot{\vec{X}}_{eo} = [A_{eo}] \dot{\vec{X}}_{ee}$$

Systems

Definitions

- ii Origin is coincident with the eo system. The orientation of this system about the eo system is specified by input Euler angles ψ_i , θ_i , and ϕ_i . The position, velocity, and acceleration in this axis system represent the components aligned with the inertial platform. Components in this system are not calculated directly because the ii system is an intermediate system in evaluating the missile achieved and commanded components.

$$\vec{X}_{ii} = [A_i] \vec{X}_{ec}$$

- bb \vec{X}_{bb} , $\dot{\vec{X}}_{bb}$ are the earth fixed launch centered components of missile position and velocity, respectively. Position, forward along missile body station axis:

$$\vec{X}_{bb} = [D]^{-1} \vec{X}_{ee} + [\dot{D}]^{-1} \vec{X}_{ee}$$

$$\vec{X}_{bb} = [D]^{-1} \vec{X}_{ee}$$

- mm Missile orientation coordinates with axis coincident with those of the b system, if control system operation is not being simulated. For simulated control operation, the coordinate axes orientation is specified by commanded turning rates or specified values evaluated by the type of flight. Components in this system are not calculated directly because the angles relatively between ii and the mm system are those of interest.

$$\vec{X}_{mm} = [D]^{-1} \vec{X}_{ee}$$

- gg Earth fixed, launch centered, azimuth oriented coordinate system. The orientation of this system about the eo system is specified by the input Euler angles ψ_g , θ_g , and ϕ_g . The velocity components of this system are used in the velocity steering logic.

$$\vec{X}_{gg} = [A_g] \vec{X}_{ee}$$

$$\dot{\vec{X}}_{gg} = [A_g] \dot{\vec{X}}_{ee}$$

$$\ddot{\vec{X}}_{gg} = [A_g] \ddot{\vec{X}}_{ee}$$

- 11 $\dot{\vec{X}}_{11}$ and $\ddot{\vec{X}}_{11}$ are the earth fixed velocity and acceleration components in the local system (the i^{11} system). \dot{X}_{11} is positive in the local north direction, \dot{Y}_{11} is positive in the local easterly direction and

Systems

Definitions

\dot{Z}_{11} is positive toward the center of the earth. Note this system travels along with the missile center.

$$\dot{\vec{X}}_{11} = [A_1]^{-1} \dot{\vec{X}}_{ee}$$

$$\ddot{\vec{X}}_{11} = [A_1]^{-1} \ddot{\vec{X}}_{ee} + [\dot{A}_1]^{-1} \dot{\vec{X}}_{ee}$$

wee $\dot{\vec{X}}_{wee}$ is the wind velocity component in the ee system.

$$\dot{\vec{X}}_{wee} = [A_1] \dot{\vec{X}}_{w11}$$

w11 $\dot{\vec{X}}_{w11}$ and $\ddot{\vec{X}}_{w11}$ are the Cartesian components of wind velocity and acceleration in the local coordinate system (the 11 system).

$$\dot{\vec{X}}_{w11} = -\dot{\nu}_w \begin{Bmatrix} \cos \psi_w \\ \sin \psi_w \\ 0 \end{Bmatrix}$$

$$\ddot{\vec{X}}_{w11} = -\ddot{\nu}_w \begin{Bmatrix} \cos \psi_w \\ \sin \psi_w \\ 0 \end{Bmatrix} - (\pi/180) \dot{\psi}_w \dot{\nu}_w \begin{Bmatrix} -\sin \psi_w \\ \cos \psi_w \\ 0 \end{Bmatrix}$$

cc \vec{X}_{cc} and $\dot{\vec{X}}_{cc}$ are the earth geocentric coordinate position and velocity with the origin at the center of the earth. The X_{cc} is positive toward the earth north pole, Y_{cc} is positive 90 degree longitude eastward from earth surface launcher point and Z_{cc} is negative through the equator at the launcher longitude.

$$\vec{X}_{cc} = \begin{bmatrix} \cos \rho_L & 0 & -\sin \rho_L \\ 0 & 1 & 0 \\ \sin \rho_L & 0 & \cos \rho_L \end{bmatrix} \vec{X}_{ee} + \gamma_e \begin{Bmatrix} \sin \rho_L \\ 0 \\ -\cos \rho_L \end{Bmatrix}$$

Systems

Definitions

$$\vec{\dot{X}}_{cc} = \begin{bmatrix} \cos \rho_L & 0 & -\sin \rho_L \\ 0 & 1 & 0 \\ \sin \rho_L & 0 & \cos \rho_L \end{bmatrix} \vec{\dot{X}}_{ee}$$

abb

$\vec{\dot{X}}_{abb}$ and $\vec{\ddot{X}}_{abb}$ are the components of missile velocity and acceleration in the missile oriented coordinate (the b system).

$$\vec{\dot{X}}_{abb} = [D]^{-1} \dot{\vec{X}}_{aee}$$

$$\vec{\ddot{X}}_{abb} = [D]^{-1} \ddot{\vec{X}}_{ee} + [\dot{D}]^{-1} \vec{\dot{X}}_{ee} - [D]^{-1} [A_1] \vec{\ddot{X}}_{w11}$$

$$- [D]^{-1} [\dot{A}_1] \vec{\dot{X}}_{w11} - [D]^{-1} [A_1] \vec{\dot{X}}_{w11}$$

Systems

Definitions

ae

\vec{X}_{ae} are the earth fixed launch centered velocity components with respect to the local ambient air.

$$\vec{X}_{ae} = \vec{X}_{ee} = \vec{X}_{wee}$$

c. Rotation Matrices--The Euler angle rotation matrices have the properties of being a uniorthogonal array. Their determinate is unity and A-inverse ($[A]^{-1}$) is equal to A-transpose ($[A]^T$). (The transpose of a matrix is obtained by interchanging rows and columns.)

The Euler angle rotation matrices used in the trajectory program are defined as follows:

Systems

Definitions

$[A_{eo}]$

The Euler angle rotation matrix which rotates the e system to the e_0 system thru the angles ρ_L at (2), ω_L at (1), and ρ_L to (2). This rotation accounts for the effect of the launcher point rotating with the earth. The matrix is defined in section B.1.c (D Matrix).

$[A_i]$

The Euler angle rotation matrix which rotates the i system to the e_0 system thru the angles ϕ_i at (1), θ_i at (2), and ψ_i at (3). These Euler angles represent the inertial platform alignment angles such that ψ_i defines the reference azimuth, θ_i defines the reference elevation and ϕ_i defines the reference roll attitude. This matrix is defined in section B.1.c. (D Matrix).

$[A_b]$

The Euler angle rotation matrix which rotates the b system to the i system thru the angles φ_b at (1), ψ_b at (3), and θ_b at (2). These angles are the achieved vehicle attitude angles.

$[D]$

The Euler angle rotation matrix which rotates the b system to the e system as

$$[D] = [A_{eo}] [A_i] [A_b]$$

A_m

The Euler angle rotation matrix which rotates the m system to the i system thru the angles ϕ_m at (1), ψ_m at (3), and θ_m at (2). These angles are the command vehicle attitude angles.

Systems

Definitions

$[K]$ The Euler angle rotation matrix which rotates the m system to the b system. The pitch ($\Delta\theta_b$), yaw ($\Delta\psi_b$), and roll ($\Delta\phi_b$) attitude error angles are the direction cosines between the achieved and desired vehicle attitude and are defined as elements of this matrix.

$$[K] = [A_m]^{-1} [A_b]$$

$[A_1]$ The Euler angle rotation matrix which rotates the e system to the 1 system thru the angles $-\rho$ at (2), μ' at (1), and ρ_L at (2). These angles are the launcher latitude, missile instantaneous change in longitude and missile instantaneous latitude. This rotation basically rotates the earth fixed launcher coordinate to the local earth fixed coordinates. Winds and gravity are defined in local coordinates then transformed to the e system for inclusion in the equations of motion.

$[A_g]$ The Euler angle rotation matrix which rotates the e system to the g system thru the generalized coordinate orientation angles ϕ_g at (1), ψ_g at (3), and θ_g at (2). This rotation is used in velocity steering logic.

$[A_{TM}]$ The Euler angle rotation matrix which rotates the e system to the TM system thru the angle ζ at (1), ϕ at (2), and ψ at (3). These angles are the firing azimuth angle, down range angle, and cross range angle. This rotation matrix is used in evaluation of the missile-target coordinates.

$[A_c]$ The Euler angle rotation matrix which rotates the vehicle velocity vector to the m system thru the angles φ_c at (1), α_c at (2), and β'_c at (3). This rotation is used in commanding the desired vehicle attitude.

$[A_{\gamma 1}]$ The Euler angle rotation matrix which rotates the local azimuth oriented velocity vector to the missile velocity vector thru the elevation flight path angle.

$[A_{\gamma 2}]$ The Euler angle rotation matrix which rotates the local velocity vector in the 11 system to the local azimuth orient velocity vector thru the azimuth flight path angle.

$$\begin{Bmatrix} v_e \\ 0 \\ 0 \end{Bmatrix} = [A_{\gamma 1}] [A_{\gamma 2}] \vec{x}_{11}$$

Systems

Definitions

- $[A_\alpha]$ The Euler angle rotation matrix which rotates the roll and yaw compensated no-wind velocity vector to the b system thru the no-wind angle of attack $\bar{\alpha}$.
- $[A_\beta']$ The Euler angle rotation matrix which rotates the roll oriented no-wind velocity vector to the roll and yaw compensated no-wind velocity vector thru the angle $\bar{\beta}'$.
- $[\phi]$ The Euler angle rotation matrix which rotates the no-wind velocity vector such that the z axis passes thru the center of the earth. This rotation is used in evaluating the local vehicle back angle attitude.
- k Stage number. For example, one value of the parameter \bar{I}_Y is needed in each stage, and \bar{I}_{YK} appears in many equations as the particular value of \bar{I}_Y applicable to the current stage.
- o An initial condition, e.g., the trajectory start time, t_0 .
- f The value of a parameter at impact or intercept.
- J The final value in a table. Several functions are input in tabular form, and often it is unnecessary to fill one entire table to define a function. Thus, in some equations involving tabular functions, statements like "if $W > W_J \dots$ " appear.
- First derivative with respect to time, e.g., the pitch thrust vector deflection angular rate $\dot{\delta}_p$ is $d\delta_p/dt$.
- .. Second derivative with respect to time, e.g., the vehicle pitch angular acceleration $\ddot{\theta}_b$ is $d^2\theta_b/dt^2$.
- Input modified by the program, e.g., the input radius of the earth r_e' if input zero is set to 20,926,490 feet.

Symbols

Symbols appearing in this document are defined on the following pages.

Those symbols which are input to the program or output from the program have their associated "L-numbers" following the description. Input data have L-numbers less than 5,000, output data have L-numbers greater than (or equal) to 5,000.

a, A

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|--|--------------|
| a_f | Input value of the dependent variable to be isolated by the hunting procedure (P1) (L0082) | (dbi) |
| a'_s | Input nozzle separation polynomial coefficient used in the separated flow nozzle thrust equation. If input zero is set to 0.3 (Lk017) | (dim) |
| a_{TC} | Target transverse acceleration (L5446) | (g's) |
| a_{TCj} | Input target earth reference acceleration crosswise to the target velocity vector for the j-th period of the target dynamical condition table (L0643, 647, etc) | (g's) |
| a_{Tj} | Input transformation constant used in the simultaneous hunting procedure (P2) j - 1, 2, ... 7 (L0099, 108, etc) | (dbi) |
| a_{TN} | Target normal to its velocity vector acceleration (L5445) | (g's) |
| a_{TNj} | Input target earth reference acceleration normal to the target velocity vector for the j-th period of the target dynamical condition table (L0642, 646, etc) | (g's) |
| a_{TT} | Target tangential acceleration (L5444) | (g's) |
| a_{TTj} | Input target earth reference acceleration tangential to the target velocity vector for the j-th period of the target dynamical condition table (L0641, 645, etc) | (g's) |
| a_{Xb} | Component of vehicle acceleration due to total thrust and aerodynamic forces. Positive in the direction of the coordinate axes of b system (L5504) | (g's) |

a, A

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|--|------------------------|
| $a_{Xb(B1)}$ | Vehicle acceleration due to total thrust and aerodynamic force at the termination of stage I (L5911) | (g's) |
| $a_{Xb(B2)}$ | Vehicle acceleration due to total thrust and aerodynamic force at the termination of stage II (L5936) | (g's) |
| $a_{Xb(B3)}$ | Vehicle acceleration due to total thrust and aerodynamic force at the termination of stage III (L5961) | (g's) |
| $a_{Xb(B4)}$ | Vehicle acceleration due to total thrust and aerodynamic force at the termination of stage IV (L5986) | (g's) |
| a_{Yb} | Component of vehicle acceleration due to total thrust and aerodynamic forces. Positive in the direction of the coordinate Y axes of the b system (L5505) | (g's) |
| a_{Zb} | Components of vehicle acceleration due to total thrust and aerodynamic forces. Positive in the direction of the coordinate Z axes of b system (L5506) | (g's) |
| $a_{o, jk}$ | Input constants used in the Z_{gg} and constant components nontarget dependent pitch steering equations for the k-th stage (Lk391-392) | (rad) |
| A_{ax} | Earth fixed axial acceleration, constrain to be greater than zero, during rail launch type of flight. | (ft/sec ²) |
| A_{eC} | Input complementary thrust-weight table stage nozzle exit area (Lk104) | (ft ²) |
| A_{Eij} | Elements of the (A_E) matrix which define the commanded turning rates for type 2 flight. | (deg/sec) |
| A'_{eM} | Input main thrust-weight table input stage nozzle exit area (Lk011) | (ft ²) |

a, A

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|----------------------|---|------------------------|
| A_{FWI}^i, A_{FWI} | Input and output respectively Stage I vacuum thrust to liftoff weight used in the vehicle characteristics pertinent to roll requirement (L0675) | (g's) |
| A_L | Input amplitude of limit cycle for the k -th stage. (Lk386) | (deg) |
| A_{ri}^i | Input and utilized relative integration tolerance, $j = 1, 2, \dots, 7$ (L0281, 283, etc) | (dbi) |
| A_{SI} | Burn surface area (L5079). | (in ²) |
| A_t | Pintle nozzle throat area. Used in TMC logic (L5735). | (in ²) |
| \dot{a}_t | Time rate change of pintle throat area (L5785). | (in ² /sec) |
| A_t^i | Input absolute allowable break-up tolerance of time (L0306). | (dim) |
| A_{tcc} | Commanded throat area (L5080). | (in ²) |
| A_x^i | Input absolute allowable break-up tolerance of target value (L0308). | (sec) |
| A_{XI} | Propellant extinguishment throat area (L5085). | (in ²) |

b, B

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|--|---|
| b_{jk} | Input constants used in the \ddot{X}_{gg} , \dot{X}_{gg}^2 , and \dot{X}_{gg}^3 components of the nontarget dependent pitch steering equation for the k-th stage, $j = 1, 2, 3$ (Lk393-395). | (rad-sec/ft rad-sec ² /ft and rad-sec) |
| b'_s | Input nozzle separation polynomial coefficient used in the separated flow nozzle thrust equation if input zero is set to 0.7 (Lk018). | (dim) |
| BD | Input basic deck number (L0000). | (dim) |
| B'_t | Input relative allowable break-up tolerance of time (L0307). | (dim) |
| B'_x | Input relative allowable break-up tolerance of target value (L0309). | (dim) |

c, C

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-------------------|---|--------------|
| c'_s | Input nozzle separation polynomial coefficient used in the separated flow nozzle thrust equation. If input zero is set to 0.884 (Lk019). | (dim) |
| C | Instantaneous aerodynamic axial force (L5164). | (lb) |
| \bar{C}' | Input stage axial force control function and multiplier. If input zero, the multiplier is set to one; if nonzero, the axial force is determined from input and multiplied by \bar{C} (Lk186). | (dim) |
| C_a | Speed of sound at the missile (L5066). | (ft/sec) |
| C_A | Instantaneous aerodynamic axial force coefficient (L5573). | (dim) |
| C_{Aj} | Input and instantaneous (with Mach number M_j) aerodynamic axial force coefficients, respectively, where $j = 1, 2, \dots, 15$ per stage (Lk189, 191, etc). | (dim) |
| C_{BN} | Added aerodynamic base drag coefficient due to nozzles not thrusting (L5574). | (dim) |
| C'_D | Input and calculated nozzle efficiency coefficient used in the separated flow nozzle thrust equation (Lk015). | (dim) |
| C_{Dz} | Instantaneous aerodynamic pitch movable fin drag coefficient (L5566). | (dim) |
| \bar{C}'_{Dz} | Input aerodynamic pitch fin drag coefficient multiplier. If zero set equal to one (Lk708). | (dim) |
| C^{\wedge}_{Dz} | Instantaneous aerodynamic pitch movable fin total drag coefficient (L5579). | (dim) |
| C_{Dzj} | Input aerodynamic pitch fin drag coefficient $j = 1, 2, \dots, 15$ per stage (Lk713, 719, etc). | (dim) |

c, C

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-----------------|---|-----------------------|
| C_{Fyj} | Input thrust system proportionality system gain of the j-th type TMC (L0804, 814, etc). | (dim) |
| C_{FI} | Thrust coefficient (Lk5081). | (dim) |
| C_{FO} | Thrust coefficient at optimum expansion ($P_e = P_a$) (L5082). | (dim) |
| \hat{C}_{Ly} | Instantaneous aerodynamic yaw movable fin total lift coefficient (L5577). | (dim) |
| \bar{C}'_{lz} | Input aerodynamic nonlinear pitch fin drag coefficient multiplier. If input zero is set to 1.0 (Lk707). | (dim) |
| C_{iz} | Instantaneous aerodynamic pitch movable fin nonlinear fin lift coefficient (L5565). | (1/deg ²) |
| C_{Lz} | Instantaneous aerodynamic pitch movable fins linear fin lift coefficient (L5564). | (1/deg ²) |
| C_{lzj} | Input and calculated aerodynamic pitch fin nonlinear lift coefficient j = 1, 2, ..., 15 per stage (Lk712, 718, etc) | (1/deg ²) |
| \bar{C}'_{Lz} | Input aerodynamic linear pitch fin lift coefficient multiplier. If input zero is set to 1.0 (Lk706). | (dim) |
| \hat{C}_{Lz} | Instantaneous aerodynamic pitch movable fin total lift coefficient (L5578). | (dim) |
| C_{Lzj} | Input and calculated aerodynamic pitch fin nonlinear lift coefficient j = 1, 2, ..., 15 per stage (Lk711, 717, etc). | (1/deg ²) |
| C_{MQ} | Calculated and unadjusted for translation aerodynamic pitch damping moment due to pitch rate coefficient (L5575). | (1/deg) |
| C_{MQj} | Input aerodynamic pitch damping moment due to pitch rate coefficient where j = 1, 2, ..., 15 per stage (Lk306, 309, etc). | (1/deg) |

c, C

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|----------------------------------|--|---|
| $C_{M\dot{\alpha}}$ | Calculated and unadjusted for translation aerodynamic pitch damping moment due to rate change of angle of attack coefficient (L5576). | (1/deg) |
| $C_{M\dot{\alpha}j}$ | Input aerodynamic pitch damping moment due to rate change of angle of attack coefficient where $j = 1, 2, \dots, 15$ per stage (Lk307, 310, etc). | (1/deg) |
| C_N | Instantaneous aerodynamic normal force coefficient (L5569). | (dim) |
| C_{N1} C_{N2} C_{N3} | Instantaneous first, second, and third derivatives, respectively, of C_N with respect to the angle of attack (L5570, 5571, 5572). | (1/deg) ₂ 1/deg ₃ 1/deg) |
| $C_{N1, 2, 3j}$ | Input values of $C_{N1, 2, 3}$ respectively, corresponding to M_j where $j = 1, 2, \dots, 15$ per stage (Lk224-226, 229-231). | (deg/deg ² /deg ³) |
| C_{RRj} | Input raceway aerodynamic force coefficient corresponding to the M_{Rj} , $j = 1, 2, \dots, 10$ (Lk674, 676). | (dim) |
| $C_{\delta z}$ | Aerodynamic pitch fin axial force (L5155). (lb) | |

d, D

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|---|--------------|
| dC_a/dh | Partial derivative of the speed of sound with altitude (L5067). | (1/sec) |
| dP_a/dh | Partial derivative of ambient pressure with altitude (L5069). | (lb/ft) |
| D_b | Propellant burn depth. Used in TMC logic (L5733). | (in) |
| D_B | Output TVC duty cycle stage case diameter from axial force reference area. | (in) |
| D_i | Input roll control system hysteresis for the i-th zone, $i = 1, 2$, or 3 (Lk640, 650, etc). | (dim) |
| D_p | Input diameter of propellant (Lk001). | (in) |
| D_{rl} | Rail launch friction drag (L5154). | (lb) |
| D_{RN} | Input aerodynamic reference diameter (Lk298). | (ft) |
| D_y | Input initial or restart discontinuity print flag (L0009). | (dim) |

e, E

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|---|--------------------------------------|
| e | Eccentricity of the missile path during the glide phase (L5112). | (dim) |
| E/m | Total missile energy per unit mass during the glide phase. Potential energy at the launcher is taken as zero (L5109). | (ft ² -sec ²) |

f, F

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-----------------|--|--------------|
| f_D | Input and flag specifying maximization and isolation of the same parameter used in hunt procedure (P2). If f_D is nonzero, the function f is maximized relative to the independent variables x_2, x_3, \dots, x_n and is isolated to a value f_D by varying x_1 (L0089). | (dbi) |
| f_{Gik} | Input attitude control system gain control flag. if equal to zero, input gains are utilized; if not equal to zero, the automatic gains are utilized for the j -th control zone, $i = 1, 2$, or 3 ; and k -th stage, $k = 1, 2, 3$, or 4 (Lk456, 465, etc). | (dim) |
| F | Total instantaneous thrust acting along missile centerline. Positive when thrust vector points forward along missile centerline (L5122). | (lb) |
| \bar{F} | Instantaneous delivered thrust per motor during the TVC design stage. | (lb) |
| F_C | Instantaneous complementary thrust (L5127). | (lb) |
| $\frac{A}{F}_C$ | Thrust required to maintain V_c ; i. e., retarding axial force used in TMC logic (L5134). | (lb) |
| F_{CALOS} | Command thrust to provide acceleration proportional to LOS rate used in TMC logic (L5137). | (lb) |
| F_{cclos} | Command thrust to provide a minimum missile to target closing rate used in TMC logic (L5138). | (lb) |

f, F

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|----------------|--|--------------|
| F_{Cj} | Input value of the complementary vacuum thrust to be used during $t_{Cj} \leq t \leq t_{C(j+1)}$, where $j = 1, 2, \dots, 25$ per stage (Lk112, 115). | (lb) |
| F_{com} | Commanded altitude thrust used in TMC logic (L5130). | (lb) |
| F_{cqmax} | Maximum thrust so that the vehicle will not exceed the maximum dynamic pressure used in TMC logic (L5136). | (lb) |
| F_{cqmin} | Require thrust so that the vehicle will maintain the minimum dynamic pressure used in TMC logic (L5135). | (lb) |
| F_{CV} | Instantaneous complementary vacuum thrust (L5128). | (lb) |
| \dot{F}_{CV} | Instantaneous complementary vacuum thrust time rate (L5129). | (lb/sec) |
| F_{CV} | Commanded vacuum thrust used in TMC logic (L5131). | (lb) |
| F_D | Instantaneous roll control system phase plane signal (L5449). | (deg) |
| F_h | Vacuum thrust of the σ_{tb} short-time trace. | (lb) |
| F_{JFy} | Jet damping yawing transverse force (L5149). | (lb) |
| F_{JDz} | Jet damping pitching transverse force (L5149). | (lb) |
| F_L | Vacuum thrust of the σ_{tb} long-time trace. | (lb) |
| F_M | Instantaneous main thrust (L5124). | (lb) |
| F_{Mj} | Input value of the main vacuum thrust to be used during $t_{Mj} \leq t \leq t_{Mj+1}$, where $j = 1, 2, \dots, 25$ per stage (Lk021, 024, etc). | (lb) |

| <u>f, F</u> | | |
|----------------|---|--------------|
| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
| F_{MV} | Instantaneous main vacuum thrust (L5125). | (lb) |
| \dot{F}_{MV} | Instantaneous main vacuum thrust rate (L5126). | (lb) |
| F_n | Nominal vacuum thrust of each motor. | (lb) |
| F_N | Nominal altitude thrust used in TMC logic. | (lb) |
| \bar{F}_q | Delivered motor thrust (\bar{F}) at t_{Bq} during TVC design stage. | (lb) |
| F_R | Instantaneous roll control thrust. Positive if the vehicle is intended to rotate clockwise as seen from the rear of the vehicle. (L5714). | (lb) |
| \dot{F}_R | Time rate change of roll control thrust (L5769). | (lb/sec) |
| F_{Rc} | Instantaneous roll control system thrust command signal (L5721). | (lb) |
| F_{RO} | Input per stage initial roll thrust (Lk424). | (lb) |
| F_{TDy} | Movable nozzle tail-wag-dog force in yaw, positive to the right (L5147). | (lb) |
| F_{TDz} | Movable nozzle tail-wag-dog force in pitch, positive down (L5148). | (lb) |
| F_v | Instantaneous total vacuum thrust (L5123). | (lb) |
| F_{VN} | Nominal vacuum thrust used in TMC logic (L5132). | (lb) |
| $ F/\dot{W} $ | Instantaneous effective specific impulse (L5115). | (sec) |
| FWI | Input Stage I vacuum thrust to liftoff weight used in the vehicle characteristics pertinent to roll requirement (L0675). | (g's) |
| F_x | Components of total vehicle thrust parallel to the coordinate axes of the b system (L5141). | (lb) |

f, F

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|------------------|---|--------------|
| F_X | Thrust force along nozzle centerline (L5144). | (lb) |
| F_y | Components of total vehicle thrust parallel to the coordinate axes of the b system (L5142). | (lb) |
| F_Y | Component of total vehicle thrust moved to nozzle centerline, positive right (L5145). | (lb) |
| F_{yj} | Input thrust control law code for the j-th type of TMC table (L6800, 810, etc). | (dim) |
| F_z | Components of total vehicle thrust parallel to the coordinate axes of the b system (L5143). | (lb) |
| F_Z | Component of total vehicle thrust normal to nozzle centerline, positive down (L5146). | (lb) |
| $F_{\Delta i}$ | Input maximum roll control thrust for the i-th zone, $i = 1, 2$, or 3 (Lk641, 651, 661). | (lb) |
| F_{vave} | Output TVC duty cycle stage average vacuum thrust. | (lb) |
| F_{vac} | Nominal input vacuum thrust time curve | (lb) |
| \bar{F}_{vac} | Instantaneous vacuum motor thrust | (lb) |
| \bar{F}_{vacq} | Output vacuum motor thrust (\bar{F}_{vac}) during the TVC design stage at t_{Bq} | (lb) |

g, G

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|---|----------------------------|
| g_e | Gravitational force at the missile. | (ft/sec ²) |
| g_e | Input mass conversion gravity. If input zero, set equal to 32.174 (L0024). | (ft/sec ²) |
| g_e' | Input gravitational acceleration at the surface of the reference body. If input zero, set equal to 32.14625 (L0025). | (ft/sec ²) |
| g_i | Lagrangian constraining function of the i-th dependent variables y_i used in the hunting procedure (P2). | (dbi) |
| g_{PI} | Fraction of propellant removed (L5084). | (dim) |
| g_{WI} | Percent web (L5077). | (dim) |
| g_{xe} | Launch centered earth fixed northerly component of gravity (L5041). | (ft/sec ²) |
| g_{xl} | Local northerly component of gravity (L5038). | (ft/sec ²) |
| g_{ye} | Launch centered earth fixed easterly component of gravity (L5042). | (ft/sec ²) |
| g_{yl} | Local easterly component of gravity (L5039). | (ft/sec ²) |
| g_{ze} | Launch centered earth fixed downward component of gravity (L5043). | (ft/sec ²) |
| g_{zl} | Local downward component of gravity (L5040). | (ft/sec ²) |
| G_z | Partial derivatives of altitude acceleration to vehicle altitude (L5455). | (ft/sec ² -deg) |
| G | Lagrangian constraining function maximized or minimized to provide an external of the function f subject to one or more constraints used in the hunting procedure (P2). | (dim) |

h, H

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|---|------------------------|
| h | Missile geometric altitude. Distance between the surface of the reference body and the missile measured along the local vertical. Positive away from the reference body (L5028) | (ft) |
| \dot{h} | Time rate change of missile geometric altitude rate between the surface of the reference body and missile measured along the local vertical positive away from the reference body (L5029) | (ft/sec) |
| \ddot{h} | Instantaneous altitude acceleration (L5030) | (ft/sec ²) |
| h_a | Apogee altitude of the missile during the glide phase (L5031) | (nm) |
| h_{ab} | Altitude above launcher (L5034) | (ft) |
| $h_{a(B1)}$ | Apogee altitude of the glide phase if the powered flight were to end at the termination of stage I (L5915) | (nm) |
| $h_{a(B2)}$ | Apogee altitude of the glide phase if the powered flight were to end at the termination of stage II (L5940) | (nm) |
| $h_{a(B3)}$ | Apogee altitude of the glide phase if the powered flight were to end at the termination of stage III (L5965) | (nm) |
| $h_{a(B4)}$ | Apogee altitude of the glide phase if the powered flight were to end at the termination of stage IV (L5990) | (nm) |
| h_{ap} | Height of apogee + paragee (L5033) | (nm) |
| $h_{(B1)}$ | Missile geometric altitude at the termination of stage I (L5902) | (ft) |
| $h_{(B2)}$ | Missile geometric altitude at the termination of stage II (L5927) | (ft) |
| $h_{(B3)}$ | Missile geometric altitude at the termination of stage III (L5952) | (ft) |

h, H

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|--|--------------|
| $h_{(B4)}$ | Missile geometric altitude at the termination of stage IV (L5977) | (ft) |
| h_{BI} | Base geopotential altitude associated with the atmosphere representation | (ft) |
| h_j | Input coramanded altitude used in the constant altitude type of flight (Ty=8) (L0313, 320, etc) | (ft) |
| h_e | Input altitude of atmospheric entry (L0042) | (ft) |
| h_E | Input altitude above which ambient pressure and aerodynamic forces are zero and speed of sound is 1,000 ft/sec. If input zero is set to 300,000 ft (L0021) | (ft) |
| h_f | Input altitude at the termination of the glide phase (L0039) | (ft) |
| h_j | Input wind velocity altitude associated with v_{wj} and ψ_{wj} where $j = 1, 2, \dots, 30$ (L0410, 413, etc) | (ft) |
| h_L | Input launcher altitude (L0019) | (ft) |
| h_{MI} | Estimated altitude at target intercept (L5442) | (ft) |
| h_{mxwd} | Input altitude of maximum wind velocity. Also flag to set up wind table per MMRBM wind shear criteria (L0682) | (ft) |
| h_p | Perigee altitude of the missile during the glide phase (L5032) | (nm) |
| $h_{p(B1)}$ | Perigee altitude of the glide phase if the powered flight were to end at the termination of stage I (L5914) | (nm) |
| $h_{p(B2)}$ | Perigee altitude of the glide phase if the powered flight were to end at the termination of stage II (L5939) | (nm) |
| $h_{p(B3)}$ | Perigee altitude of the glide phase if the powered flight were to end at the termination of stage III (L5964) | (nm) |

h, H

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|--|--------------|
| $h_{p(B4)}$ | Perigee altitude of the glide phase if the powered flight were to end at the termination of stage IV (L5989) | (nm) |
| h_T | Target altitude (L5730) | (ft) |
| h_{To} | Input target initial altitude at the start of the target maneuvering (L0634) | (ft) |
| h_α | Input final attitude of maximum wind shear used in TVC duty cycle slew rate calculations (L0672) | (ft) |
| h_β | Input initial attitude of maximum wind shear used in TVC duty cycle slew rate calculations (L0673) | (ft) |
| h_o | Input missile altitude at the trajectory start time (L0012) | (ft) |
| H_e | Heating parameter. Integral of qv from stage initiation to the time being printed (L5747) | (lb/ft) |
| \dot{h}_T | Target altitude rate (L5780) | (ft/sec) |

i, I

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|---|-------------------------|
| i | Orbital inclination angle (L5111) | (deg) |
| I | Total missile impulse measured from stage initiation to the time being printed (L5737) | (lb-sec) |
| \bar{I} | Output motor thrust impulse for TVC duty cycle stage | (lb-sec) |
| $I_{FC(1)}$ | Calculated complementary table nozzle back pressure impulse for stage I (L5847) | (lb-sec) |
| $I_{FC(2)}$ | Calculated complementary table nozzle back pressure impulse for stage II (L5862) | (lb-sec) |
| $I_{FC(3)}$ | Calculated complementary table nozzle back pressure impulse for stage III (L5877) | (lb-sec) |
| $I_{FC(4)}$ | Calculated complementary table nozzle back pressure impulse for stage IV (L5892) | (lb-sec) |
| $I_{FM(1)}$ | Calculated main table nozzle back pressure impulse for stage I (L5841) | (lb-sec) |
| $I_{FM(2)}$ | Calculated main table nozzle back pressure impulse for stage II (L5856) | (lb-sec) |
| $I_{FM(3)}$ | Calculated main table nozzle back pressure impulse for stage III (L5871) | (lb-sec) |
| $I_{FM(4)}$ | Calculated main table nozzle back pressure impulse for stage IV (L5886) | (lb-sec) |
| I_n | Input stage movable portion nozzle movement of inertia about the gimbal point (Lk483) | (slug-ft ²) |
| I_{PRD} | Pitch inertia rotation damping moment integral (L5193) | (ft-lb-sec) |
| I_P | Pitch control thrust impulse from stage initiation to the time being printed (L5739) | (lb-sec) |
| \bar{I}_P | Output pitch control thrust impulse per control motor from TVC duty cycle initiation to stage termination | (lb-sec) |
| I_R | Auxiliary roll control system delivered total impulse (L5745) | (lb-sec) |

i, I

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|---|--------------|
| I_{RRD} | Roll inertia rotation damping moment integral (L5195) | (ft-lb-sec) |
| I_{spaug} | Input and output estimated TVC system caused specific impulse augmentation (positive) or degradation (negative). Used in trajectory TVC Design program refly (L0679) | (sec) |
| I_{spC} | Input complementary specific impulse used to compute vehicle weight flow. If zero weight flow is determined from input weight flow (L5852) | (sec) |
| $I_{spC(1)}$ | Calculated complementary table adjusted to vacuum specific impulse for stage I (L5852) | (sec) |
| $I_{spC(2)}$ | Calculated complementary table adjusted to vacuum specific impulse for stage II (L5867) | (sec) |
| $I_{spC(3)}$ | Calculated complementary table adjusted to vacuum specific impulse for stage III (L5882) | (sec) |
| $I_{spC(4)}$ | Calculated complementary table adjusted to vacuum specific impulse for stage IV (L5897) | (sec) |
| I_{spM} | Input main specific impulse used to compute vehicle weight flow. If zero, weight flow is determined from the input weight flow. Also output in the TVC duty cycle (Lk010) | (sec) |
| $I_{spM(1)}$ | Calculated main table adjusted to vacuum specific impulse for stage I (L5846) | (sec) |
| $I_{spM(2)}$ | Calculated main table adjusted to vacuum specific impulse for stage II (L5861) | (sec) |
| $I_{spM(3)}$ | Calculated main table adjusted to vacuum specific impulse for stage III (L5876) | (sec) |
| $I_{spM(4)}$ | Calculated main table adjusted to vacuum specific impulse for stage IV (L5891) | (sec) |
| I_{SPRi} | Input roll control motor specific impulse for the i-th zone, $i = 1, 2, \text{ or } 3$ (Lk646, 656, 666) | (sec) |
| I_V | Total missile vacuum impulse, measured from stage initiation to the time being printed (L5738) | (lb-sec) |

i, I

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-------------------|---|--------------|
| $I_{V(B1)}$ | Total missile vacuum impulse for stage I (L5913) | (lb-sec) |
| $I_{V(B2)}$ | Total missile vacuum impulse for stage II (L5938) | (lb-sec) |
| $I_{V(B3)}$ | Total missile vacuum impulse for stage III (L5963) | (lb-sec) |
| $I_{V(B4)}$ | Total missile vacuum impulse for stage IV (L5988) | (lb-sec) |
| \bar{I}_V | Output motor vacuum thrust impulse for TVC duty cycle stage | (lb-sec) |
| I'_{vC} | Input complementary stage total vacuum impulse (Lk196) | (lb-sec) |
| I''_{vC} | Vacuum impulse under input complementary thrust curve (L5105) | (lb-sec) |
| $I_{vC(1)}$ | Calculated input vacuum corrected complementary table time adjusted thrust integral for stage I (L5849) | (lb-sec) |
| $I_{vC(2)}$ | Calculated input vacuum corrected complementary table time adjusted thrust integral for stage II (L5863) | (lb-sec) |
| $I_{vC(3)}$ | Calculated input vacuum corrected complementary table time adjusted thrust integral for stage III (L5879) | (lb-sec) |
| $I_{vC(4)}$ | Calculated input vacuum corrected complementary table time adjusted thrust integral for stage IV (L5893) | (lb-sec) |
| $\hat{I}_{vC(1)}$ | Calculated complementary table input total impulse adjusted to vacuum condition for stage I (L5849) | (lb-sec) |
| $\hat{I}_{vC(2)}$ | Calculated complementary table input total impulse adjusted to vacuum condition for stage II (L5863) | (lb-sec) |
| $\hat{I}_{vC(3)}$ | Calculated complementary table input total impulse adjusted to vacuum conditions for stage III (L5878) | (lb-sec) |
| $\hat{I}_{vC(4)}$ | Calculated complementary table input total impulse adjusted to vacuum conditions for stage IV (L5893) | (lb-sec) |

i. 1

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-------------------|--|--------------|
| $I_{vC(1)}^*$ | Calculated complementary table vacuum adjusted thrust integral for stage I (L5850) | (lb-sec) |
| $I_{vC(2)}^*$ | Calculated complementary table vacuum adjusted thrust integral for stage II (L5863) | (lb-sec) |
| $I_{vC(3)}^*$ | Calculated complementary table vacuum adjusted thrust integral for stage III (L5879) | (lb-sec) |
| $I_{vC(4)}^*$ | Calculated complementary table vacuum adjusted thrust integral for stage IV (L5893) | (lb-sec) |
| I_{vM}' | Input main stage total vacuum impulse (Lk005) | (lb-sec) |
| I_{vM}'' | Vacuum impulse under input main thrust curve (L5104) | (lb-sec) |
| $I_{vM(1)}$ | Calculated input vacuum corrected main table time adjusted thrust integral for stage I (L5843) | (lb-sec) |
| $I_{vM(2)}$ | Calculated input vacuum corrected main table time adjusted thrust integral for stage II (L5858) | (lb-sec) |
| $I_{vM(3)}$ | Calculated input vacuum corrected main table time adjusted thrust integral for stage III (L5873) | (lb-sec) |
| $I_{vM(4)}$ | Calculated input vacuum corrected main table time adjusted thrust integral for stage IV (L5888) | (lb-sec) |
| $\hat{I}_{vM(1)}$ | Calculated main table input total impulse adjusted to vacuum conditions for stage I (L5842) | (lb-sec) |
| $\hat{I}_{vM(2)}$ | Calculated main table input total impulse adjusted to vacuum conditions for stage II (L5857) | (lb-sec) |
| $\hat{I}_{vM(3)}$ | Calculated main table input total impulse adjusted to vacuum conditions for stage III (L5872) | (lb-sec) |
| $\hat{I}_{vM(4)}$ | Calculated main table input total impulse adjusted to vacuum conditions for stage IV (L5887) | (lb-sec) |
| $I_{vM(1)}^*$ | Calculated main table vacuum adjusted thrust integral for stage I (L5844) | (lb-sec) |
| $I_{vM(2)}^*$ | Calculated main table vacuum adjusted thrust integral for stage II (L5859) | (lb-sec) |

i, I

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-------------------|---|--------------|
| $I_{VM(3)}^*$ | Calculated main table vacuum adjusted thrust integral for stage III (L5874) | (lb-sec) |
| $I_{VM(4)}^*$ | Calculated main table vacuum adjusted thrust integral for stage IV (L5889) | (lb-sec) |
| I_{VT}' | Input total of the main and complementary vacuum impulse (Lk004) | (lb-sec) |
| $I_{VT(1)}$ | Calculated input vacuum corrected main and complementary impulse corrected for stage I (L5855) | (lb-sec) |
| $I_{VT(2)}$ | Calculated input vacuum corrected main and complementary impulse time corrected for stage II (L5870) | (lb-sec) |
| $I_{VT(3)}$ | Calculated input vacuum corrected main and complementary impulse time corrected for stage III (L5885) | (lb-sec) |
| $I_{VT(4)}$ | Calculated input vacuum corrected main and complementary impulse time corrected for stage IV (L5900) | (lb-sec) |
| $\hat{I}_{VT(1)}$ | Calculated input main and complementary impulse corrected to vacuum condition for stage I (L5853) | (lb-sec) |
| $\hat{I}_{VT(2)}$ | Calculated input main and complementary impulse corrected to vacuum conditions for stage II (L5868) | (lb-sec) |
| $\hat{I}_{VT(3)}$ | Calculated input main and complementary impulse corrected to vacuum conditions for stage III (L5883) | (lb-sec) |
| $\hat{I}_{VT(4)}$ | Calculated input main and complementary impulse corrected to vacuum conditions for stage IV (L5898) | (lb-sec) |
| $I_{VT(1)}^*$ | Calculated main and complementary vacuum adjusted thrust integral for stage I (L5854) | (lb-sec) |
| $I_{VT(2)}^*$ | Calculated main and complementary vacuum adjusted thrust integral for stage II (L5869) | (lb-sec) |
| $I_{VT(3)}^*$ | Calculated main and complementary vacuum adjusted thrust integral for stage III (L5884) | (lb-sec) |

i, I

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|----------------|--|---------------------------|
| $I_{VT(4)}^*$ | Calculated main and complementary vacuum adjusted thrust integral for stage IV (L5899) | (lb-sec) |
| I_{VT}'' | Output integral of the stage main plus complementary thrust tables as adjusted by the calculated multipliers | (lb-sec) |
| \bar{I}_X | Input roll moment of inertia multiplier (Lk477) | (dbi) |
| I_{Xj} | Input total vehicle roll moment of inertia weight input W_j , where $j = 1, 2, \dots, 15$ per stage (Lk494, 504) | (slug ft ²) |
| I_{XX} | Roll moment of inertia about vehicle center-of-gravity (L5175) | (ft-lb-sec ²) |
| \dot{I}_{XX} | Time rate change of roll moment of inertia (L5184) | (ft-lb-sec) |
| I_{XY} | Roll-yaw product of inertia about vehicle center-of-gravity (L5176) | (ft-lb-sec ²) |
| \dot{I}_{XY} | Time rate change of roll-yaw product of inertia (L5185) | (ft-lb-sec) |
| I_{XYj} | Input total vehicle roll-yaw product of inertia corresponding to the total weight input W_j , where $j = 1, 2, \dots, 15$ per stage (Lk495, 505) | (slug ft ²) |
| I_{XZ} | Roll-pitch product of inertia about vehicle center-of-gravity (L5177) | (ft-lb-sec ²) |
| \dot{I}_{XZ} | Time rate change of roll-pitch product of inertia (L5186) | (ft-lb-sec) |
| I_Y | Yaw control thrust impulse from stage initiation to the time being printed (L5740) | (lb-sec) |
| \bar{I}_Y | Input moment of inertia multiplier (Lk475) | (dbi) |
| I_{Yj} | Input total vehicle pitch moment of inertia corresponding to the total vehicle weight input W_j where $j = 1, 2, \dots, 15$ per stage (Lk490, 500) | (dbi) |
| \bar{I}_y | Output yaw control thrust impulse per control motor from TVC stage initiation to stage termination | (lb-sec) |

I, I

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|--|---------------------------|
| $I_{VT(4)}^*$ | Calculated main and complementary vacuum adjusted thrust integral for stage IV (L5809) | (lb-sec) |
| i_{VT}'' | Output integral of the stage main plus complementary thrust tables as adjusted by the calculated multipliers | (lb-sec) |
| \bar{I}_X | Input roll moment of inertia multiplier (Lk477) | (dbi) |
| I_{Xj} | Input total vehicle roll moment of inertia weight input W_j , where $j = 1, 2, \dots, 15$ per stage (Lk494, 504) | (slug ft ²) |
| I_{XX} | Roll moment of inertia about vehicle center-of-gravity (L5175) | (ft-lb-sec ²) |
| i_{XX} | Time rate change of roll moment of inertia (L5184) | (ft-lb-sec) |
| I_{XY} | Roll-yaw product of inertia about vehicle center-of-gravity (L5176) | (ft-lb-sec ²) |
| i_{XY} | Time rate change of roll-yaw product of inertia (L5185) | (ft-lb-sec) |
| I_{XYj} | Input total vehicle roll-yaw product of inertia corresponding to the total weight input W_j , where $j = 1, 2, \dots, 15$ per stage (Lk495, 505) | (slug ft ²) |
| I_{XZ} | Roll-pitch product of inertia about vehicle center-of-gravity (L5177) | (ft-lb-sec ²) |
| i_{XZ} | Time rate change of roll-pitch product of inertia (L5186) | (ft-lb-sec) |
| I_Y | Yaw control thrust impulse from stage initiation to the time being printed (L5742) | (lb-sec) |
| \bar{I}_Y | Input moment of inertia multiplier (Lk475) | (dbi) |
| I_{Yj} | Input total vehicle pitch moment of inertia corresponding to the total vehicle weight input W_j , where $j = 1, 2, \dots, 15$ per stage (Lk490, 500) | (dbi) |
| \bar{I}_Y | Output yaw control thrust impulse per control motor from TVC stage initiation to stage termination | (lb-sec) |

i, I

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------------------|--|---------------------------|
| I_{YRD} | Yaw inertia rotation damping moment integral (L5194) | (ft-lb-sec) |
| I_{YY} | Pitch moment of inertia about vehicle center-of-gravity (L5179) | (ft-lb-sec ²) |
| \dot{I}_{YY} | Time rate change of pitch moment of inertia (L5188) | (ft-lb-sec) |
| I_{YZ} | Yaw-pitch product of inertia about vehicle center-of-gravity (L5180) | (ft-lb-sec ²) |
| \dot{I}_{YZ} | Time rate change of yaw-pitch product of inertia (L5189) | (ft-lb-sec) |
| I_{YZj} | Input total vehicle yaw pitch product of inertia corresponding to the total vehicle weight input W_j , where $j = 1, 2, \dots, 15$ per stage (Lk496, 506) | (slug ft ²) |
| \bar{I}_Z | Input yaw moment of inertia multiplier (Lk476) | (dbi) |
| I_{Zj} | Input total vehicle yaw moment of inertia corresponding to the total vehicle weight input W , where $j = 1, 2, \dots, 15$ per stage (Lk492, 502) | (slug ft ²) |
| I_{ZXj} | Input total vehicle pitch-roll product of inertia corresponding to the total vehicle weight input W_j , where $j = 1, 2, \dots, 15$ per stage (Lk497, 507) | (slug ft ²) |
| I_{ZZ} | Yaw moment of inertia about vehicle center-of-gravity (L5183) | (ft-lb-sec ²) |
| \dot{I}_{ZZ} | Time rate change of yaw moment of inertia (L5192) | (ft-lb-sec) |
| $I_{\dot{\delta}P}$ | Sum of pitch angular thrust vectoring velocities from stage initiation to the time being printed (L5741) | (deg) |
| $\bar{I}_{\dot{\delta}P}$ | Sum of pitch angular thrust vectoring velocities from stage initiation to the time being printed corrected for dither (L5116) | (deg) |
| $I_{\dot{\delta}Y}$ | Sum of yaw angular thrust vectoring velocities from stage initiation to the time being printed (L5742) | (deg) |
| $\bar{I}_{\dot{\delta}Y}$ | Sum of yaw angular thrust vectoring velocities from stage initiation to the time being printed corrected for dither (L5117) | (deg) |

i, J

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|---|--------------|
| J | Input gravitational value which accounts for the earth's oblateness (L0023) | (dim) |

k, K

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|---|--------------------|
| K_3 | Input quantity which determines stage termination (Lk003) | (dbi) |
| K_a | Input isolation-maximization control function. If zero, isolation is specified and if nczero, maximization of the dependent variables will occur used in hunting procedure (PI) (L0076) | (dim) |
| K_{BD} | Input flag which stipulates that the main nozzle exit area will be used in the base drag calculations when splitting main and complementary tables to allow for up to 47 thrust time points (Lk108) | (dim) |
| K_{cv} | Commanded thrust velocity error gain used in TMC (L5452) | (lb-sec/ft) |
| K_{cq} | Commanded thrust dynamic pressure error gain used in TMC (L5453) | (ft ²) |
| $K_{cl,2}$ | Input lower and upper limits, respectively, for computation of orbital elements and impact determination computations (L0037, 38) | (dbi) |
| K_{dc} | Input and output stage number of TVC duty cycle stage (L0671) | (dim) |
| K_{DP} | Instantaneous control system pitch attitude error gain (L5461) | (dim) |
| K_{DPj} | Input control system pitch attitude error gain for the j-th control region j = 1, 2, or 3 (Lk450, 459, etc) | (dim) |
| K_{DR} | Instantaneous control system roll attitude error gain (L5463) | (dim) |
| K_{DRi} | Input roll control system attitude error gain for the i-th zone, i = 1, 2, or 3 (Lk643, 653, 663) | (dim) |
| K_{DY} | Instantaneous control system yaw attitude error gain (L5462) | (dim) |
| K_{DYj} | Input control system yaw attitude error gain for the j-th control region j = 1, 2, or 3 (Lk451, 450, etc) | (dim) |

k, K

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|--|--------------|
| K'_{FC} | input multiplier of the complementary vacuum thrust. If input zero for the k-th stage and $I'_{vT} = I'_{vT} = 0$, the complementary thrust for the k-th stage are zero (Lk100) | (dim) |
| K''_{FC} | Calculated vacuum scale factor for back pressure term for complementary thrust time table | (dim) |
| $K^*_{FC(1)}$ | Calculated complementary table thrust multiplier for stage I (L5851) | (dim) |
| $K^*_{FC(2)}$ | Calculated complementary table thrust multiplier for stage II (L5866) | (dim) |
| $K^*_{FC(3)}$ | Calculated complementary table thrust multiplier for stage III (L5881) | (dim) |
| $K^*_{FC(4)}$ | Calculated complementary table thrust multiplier for stage IV (L5896) | (dim) |
| K_{fj} | Input limit of the j-th type of flight where $j = 1, 2, \dots$, or 16 (L0312, 319, etc) | (dbi) |
| K_{FM} | Input multipliers of the main vacuum thrust (Lk007) | (dim) |
| K''_{FM} | Calculated vacuum scale factor for back pressure term for main thrust time table | (dim) |
| $K^*_{FM(1)}$ | Calculated main table thrust multiplier for stage I (L5845) | (dim) |
| $K^*_{FM(2)}$ | Calculated main table thrust multiplier for stage II (L5860) | (dim) |
| $K^*_{FM(3)}$ | Calculated main table thrust multiplier for stage III (L5875) | (dim) |
| $K^*_{FM(4)}$ | Calculated main table thrust multiplier for stage IV (L5890) | (dim) |
| K_{Fyj} | Input limit of the j-th type TMC (L0802, 812, etc) | (dbi) |
| K_{Gik} | Input attitude control system gain zone limits ($i = 1, 2$, or 3) and the k-th stage $k = 1, 2, 3$, or 4 (Lk458, 467) | (dbi) |

k, K

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|--|--------------|
| K_{glk} | Input quantity which designates the start of the acquisition zone for evaluation of the steering equation coefficient for the k-th stage, $k = 1, 2, 3$, or 4 (Lk398) | (dbi) |
| K_{g2k} | Input quantity which designates the end of the acquisition zone for evaluation of the steering equation coefficient for the k-th stage, $k = 1, 2, 3$, or 4 (Lk400) | (dbi) |
| K_h | Input wind altitude multiplier and flag. If zero, no wind effects are considered (L0407) | (dbi) |
| K_{HGj} | Input navigation constant used in the Homing Guidance (Ty=11) (L0313, 320, etc) | (dim) |
| K_{ij} | i-th row, j-th column of the [K] Euler angle rotation matrix which rotates the m system to the b system. These elements are the direction cosines between the achieved and desired vehicle attitude, ie, the error angles. | |
| K_{IP} | Instantaneous control system angle of attack gain (L5469) | (dim) |
| K_{IPj} | Input pitch angle of attack gain for the j-th control region $j = 1, 2$, or 3 (Lk454, 463, etc) | (dim) |
| K_{LR} | Roll control attitude bias gain (L5466) | (1/sec) |
| K_{IY} | Instantaneous control system angle of side slip gain (L5465) | (dim) |
| K_{IYj} | Input yaw angle of slide slip gain for the j-th control region $j = 1, 2$, or 3 (Lk455, 464) | (dim) |
| K_{Jj} | Input value of that parameter at which the weight W_{JTj} is to be jettisoned where $j = 1, 2, \dots$ or 8 (L0051, 54, etc) | (dbi) |
| K'_k | Input stage start control function. If 1, 2, 3, or 4, the run starts at the initiation of the first, second, third, or fourth stage, respectively if input zero set equal to 1 (L0003) | (dim) |

k, K

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-----------------|---|--------------|
| K_{Lz} | Instantaneous aerodynamic pitch movable fin drag due to lift factor (L5567) | (dim) |
| \bar{K}'_{Lz} | Input aerodynamic pitch fin drag due to lift multiplier. If zero set equal to 1 (Lk709) | (dim) |
| K_{Lzj} | Input aerodynamic pitch fin drag due to lift factor (Lk714, 720, etc.) | (rad) |
| K_{Mj} | Input quantity which designates the limit of the j-th mode type end where $j = 1, 2, \dots, 10$ (L062, 605, etc) | (dim) |
| K_{NOk} | Input complementary thrust-weight table weight carryover flag for the k-th stage. If K_{Ok} and K_{NOk} are nonzero, separation has occurred with regards to the complementary weight. If K_{Ok} is nonzero and K_{NOk} is zero, the total vehicle weight at the termination of the k-1 stage is used as the initial weight of the k-th stage (Lk107) | (dim) |
| K_{Ok} | Input main thrust-weight table weight carryover flag for the k-th stage. If zero, separation has occurred with regards to the main and complementary weights. If nonzero, the main weight at the termination of the k-1 stage is used as the initial main weight of the k-th stage (Lk012) | (dim) |
| K_p | Pressure rate gain used in pintle area control law in the TMC (L5451) | (sec) |
| K_{cf} | Input aerodynamic pitch fin deflection angle multiplier (Lk705) | (dim) |
| K_Q | Input aerodynamic pitch damping moment due to pitch rate multiplier (Lk301) | (dim) |
| K_{RC} | Input roll control system flag. If equal 1, an auxiliary roll thruster system is simulated. If equal 2, aerodynamic central fins are used (Lk405) | (dim) |
| K_{RP} | Instantaneous control system pitch rate gain (L5467) | (sec) |

k, K

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|--|----------------------------|
| K_{RPj} | Input control system pitch attitude rate gain for j-th control region, $j = 1, 2, \text{ or } 3$ (Lk452, 461, etc) | (sec) |
| K_{RR} | Instantaneous control system roll rate gain (L5469) | (sec) |
| K_{RRi} | Input roll control system attitude rate gain for the i-th zone, $i = 1, 2, \text{ or } 3$ (Lk645, 655, 665) | (sec) |
| K_{RY} | Instantaneous control system yaw rate gain (L5468) | (sec) |
| K_{RYj} | Input control system yaw attitude rate gain for the j-th control region, $j = 1, 2, \text{ or } 3$ (Lk453, 462, etc.) | (sec) |
| K_S | Pressure error gain used in pintle area control law in the TMC (L5450) | (in. ⁴ /lb-sec) |
| K_S | Input stage print control function. A nonzero value is required to print the trajectory at the termination of each stage during the hunting procedure (L0074) | (dim) |
| F_{sh} | Input shaper control flag where: if it equals zero, ignore routine 1. maximize range, 2. maximize payload to a given range, or 3. determine payload to a circular orbit (L0598) | (dim) |
| K'_{tc} | Input complementary switching time multiplier. If zero, the program assumes a value of 1 (Lk102) | (dim) |
| K_{tj} | Input value when a trajectory printout is desired where $j = 1, 2, \dots, 8$ (L0237, 239, etc) | (dbi) |
| K'_{tm} | Input main switching time multipliers. If zero, the program assumes a value of 1. If σ_s is designated at t_B , then K_3 is multiplied by K'_{tm} . (Lk009) | (dbi) |
| K_{tm} | Output for the TVC duty cycle stage, the main switching time multiplier | (dim) |
| K_{TPF} | Input titled print flag (L0683) | (dim) |

k, K

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|--------------------|---|----------------------------|
| K_{Tto} | Input quantity which designates the start of target maneuvering (L0631) | (dbi) |
| K_v | Input wind speed multiplier (L0408) | (dbi) |
| K'_{WC} | Input complementary weight flow multiplier. If input zero is set to 1.0 (Lk101) | (dim) |
| K_{WM} | Input mainweight flow multiplier. If input zero is set to 1.0 (Lk008) | (dim) |
| K_{XXX} | Commanded thrust system gain. Set equal to K_{CPR} if $F_y=3$ and K_{ALOS} if $F_y=6$ (L5454) | (dim) |
| K'_{ycf} | Input aerodynamic yaw fin deflection angle multiplier (Lk704) | (dim) |
| K_{yk} | Input gain constant in the non-target dependent yaw steering equation for the k-th stage (Lk401) | (dim) |
| K_Z | Altitude error gain used in type 8 flight (L5456) | (deg/ft) |
| $K_{\dot{Z}}$ | Altitude rate gain used in type 8 flight (L5457) | (deg-sec/ft) |
| $K_{\ddot{Z}}$ | Altitude acceleration gain used in type 8 flight (L5458) | (deg-sec ² /ft) |
| $K_{\dot{\alpha}}$ | Input aerodynamic pitch damping moment due to time rate change of angle of attack multiplier (Lk303) | (dim) |
| K_{γ} | Input glide phase termination control function. A value of plus 1 will specify impact after apogee, while a minus 1 will specify impact before apogee (L0040) | (dim) |
| K_{δ} | Input thrust control flag. If zero, control thrust is determined from instantaneous vehicle thrust. If 1, the control thrust is obtained from the instantaneous main stage thrust, if 2 control thrust is nonexistent (Lk434) | (dim) |

k, K

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------------|--|---------------------|
| K_{Δ}^i | Input side impulse multiplier. If input zero is set to 1 (Lk387) | (dim) |
| $K_{\ddot{\theta}}$ | Command attitude pitch attitude angular acceleration gain used in type of flight 8 and 9 (L5459) | (sec ²) |
| $K_{\dot{\psi}}$ | In-out wind azimuth multiplier (L0409) | (dim) |
| $K_{\ddot{\psi}}$ | Command attitude, yaw attitude angular acceleration gain used in type of flight 8 and 9 (L5460) | (sec ²) |

l, L

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|----------------|--|--------------|
| l_{bz} | Input pitch fin base root length (Lk703) | (ft) |
| l_{cp} | Vehicle center-of-gravity to aerodynamic center-of-pressure distance (L5596) | (ft) |
| l_e | Gimbal point to vehicle center-of-gravity distance (L5593) | (ft) |
| l_E | Nozzle exit to center-of-gravity distance (L5594) | (ft) |
| l_{hz} | Pitch movable control fin center-of-pressure to hinge axis lever arm (L5602) | (ft) |
| l_r | Missile travel distance on the rail launcher used in ground launch tape of flight (Ty=6) (L5113) | (ft) |
| l_n | Movable portion of the nozzle center-of-gravity to gimbal point distance (L5595) | (ft) |
| l_N | Vehicle center-of-gravity to stop-start motor thrust point distance (L5597) | (ft) |
| l_{Pa} | Aft end of propellant grain to center-of-gravity distance (L5599) | (ft) |
| l_{Pf} | Forward end of propellant grain to center-of-gravity distance (L5598) | (ft) |
| l_{Ri} | Input thruster roll control lever arm for the i-th center zone (Lk638, 648, 658) | (ft) |
| $l_{\delta R}$ | Input roll fin radial center-of-pressure to missile centerline distance (Lk404) | (ft) |
| $l_{\delta y}$ | Yaw movable control fin center-of-pressure to vehicle center-of-gravity lever arm (L5600) | (ft) |
| $l_{\delta z}$ | Pitch movable control fin center-of-pressure to vehicle center-of-gravity lever arm (L5601) | (ft) |
| L_D | Drag velocity loss from stage ignition (L5746) | (ft/sec) |
| $L_{D(B1)}$ | Drag velocity loss for stage I (L5907) | (ft/sec) |

L, L

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|--|--------------|
| $L_{D(B2)}$ | Drag velocity loss for stage II (L5932) | (ft/sec) |
| $L_{D(B3)}$ | Drag velocity loss due to back pressure for stage III (L5957) | (ft/sec) |
| $L_{D(B4)}$ | Drag velocity loss for stage IV (L5982) | (ft/sec) |
| L_F | Output total velocity loss due to back pressure from stage initiation to the time being printed (L5743) | (ft/sec) |
| $L_{F(B1)}$ | Total thrust velocity loss due to back pressure for stage I (L5908) | (ft/sec) |
| $L_{F(B2)}$ | Total thrust velocity loss due to back pressure for stage II (L5931) | (ft/sec) |
| $L_{F(B3)}$ | Total thrust velocity loss due to back pressure for stage III (L5956) | (ft/sec) |
| $L_{F(B4)}$ | Total thrust velocity loss due to back pressure for stage IV (L5981) | (ft/sec) |
| L_g | Gravity losses, from trajectory initiation to the time being printed (L5748) | (ft/sec) |
| $L_{g(B1)}$ | Gravity velocity loss for stage I (L5908) | (ft/sec) |
| $L_{g(B2)}$ | Gravity velocity loss for stage II (L5933) | (ft/sec) |
| $L_{g(B3)}$ | Gravity velocity loss for stage III (L5918) | (ft/sec) |
| $L_{g(B4)}$ | Gravity velocity loss for stage IV (L5983) | (ft/sec) |
| L_j | Input control system where $j = 1, 2, \dots, 10$ per stage. If zero, a limit is not applied; otherwise, L_j limits the following parameters where the statement number is j (1) $K_{DP} \Delta \theta_b$, (2) δ_{Pc} , (3) δ_P , (4) $\dot{\delta}_P$ and (5) $\ddot{\delta}_P$, (6) $K_{DY} \Delta \psi_b$, (7) δ_{YC} , (9) $\dot{\delta}_Y$ (10) $\ddot{\delta}_Y$ (Lk440-449) | (deg) |

1, L

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|--|--------------|
| L_{RCi} | Input maximum roll control thrust for the i-th zone, $i = 1, 2$, or 3 (Lk642, 652, 662) | (lb) |
| L_v | Output ideal velocity vectoring losses (L5118) | (ft/sec) |
| $L_{V(B1)}$ | Vectoring velocity loss for stage I (L5909) | (ft/sec) |
| $L_{V(B2)}$ | Vectoring velocity loss for stage II (L5934) | (ft/sec) |
| $L_{V(B3)}$ | Vectoring velocity loss for stage III (L5959) | (ft/sec) |
| $L_{V(B4)}$ | Vectoring velocity loss for stage IV (L5984) | (ft/sec) |

m, M

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|------------------|--|---------------------------|
| m | Instantaneous missile mass (L5092) | (lb-sec ² /ft) |
| M | Missile Mach number (L5063) | (dim) |
| M _{Aj} | Input Mach number for aerodynamic axial representation where j = 1, 2, ..., 15 per stage (Lk188, 190, etc) | (dim) |
| M _{CP} | Controlling moment about vehicle center-of-gravity in roll (L5210) | (ft-lb) |
| M _{CQ} | Controlling moment about vehicle center-of-gravity in pitch (L5208) | (ft-lb) |
| M _{CR} | Controlling moment about vehicle center-of-gravity in yaw (L5209) | (ft-lb) |
| M _{CYG} | Aerodynamic axial force center-of-gravity offset yawing moment (L5229) | (ft-lb) |
| M _{CZG} | Aerodynamic axial force center-of-gravity offset pitching moment (L5230) | (ft-lb) |
| M _{Dj} | Input Mach number for aerodynamic representation where j = 1, 2, ..., 15 per stage (Lk305, 308, etc) | (dim) |
| M _{DP} | Perturbing moment about vehicle center-of-gravity in roll (L5207) | (ft-lb) |
| M _{DQ} | Perturbing moment about vehicle center-of-gravity in pitch (L5205) | (ft-lb) |
| M _{DR} | Perturbing moment about vehicle center-of-gravity in yaw (L5206) | (ft-lb) |
| M _{FCP} | Auxiliary roll thrust control moment (L5225) | (ft-lb) |
| M _{FCQ} | Thrust vector control pitching moment (L5223) | (ft-lb) |
| M _{FCR} | Thrust vector control yawing moment (L5224) | (ft-lb) |

m, M

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|---|-----------------|
| M_{F_j} | Input Mach number for aerodynamic fin representation where $j = 1, 2, \dots, 15$ per stage (Lk710, 716, etc) | (dim) |
| M_{FOP} | Thrust offset rolling moment due to pitch and yaw TVC (L5216) | (ft-lb) |
| M_{FOQ} | Thrust offset pitching moment (L5214) | (ft-lb) |
| M_{FOR} | Thrust offset yawing moment (L5215) | (ft-lb) |
| M_{FVP} | Rolling moment about vehicle center-of-gravity due to vortexing effect of axial gas flow through the nozzle (L5219) | (ft-lb) |
| M_{Hy} | Torque about the yaw fin hinge axis (L5247) | (ft-lb) |
| M_{Hz} | Torque about the pitch fin hinge axis (L5248) | (ft-lb) |
| MIN_j | Input minimum velocity or constant Mach number of the j -th type of TMC (L0806, 816, etc) | (dim or ft/sec) |
| M_{JDQ} | Jet damping pitching moment (L5220) | (ft-lb) |
| M_{JDR} | Jet damping yawing moment (L5221) | (ft-lb) |
| M_{IP} | Unbalanced roll moment about vehicle center-of-gravity (L5204) | (ft-lb) |
| M_{IQ} | Unbalanced pitching moment about vehicle center-of-gravity (L5202) | (ft-lb) |
| M_{IR} | Unbalanced yaw moment about vehicle center-of-gravity (L5203) | (ft-lb) |
| $M_{hy\max}$ | Output maximum of the absolute value yaw fin hinge torque for the TVC design stage | (ft-lb) |
| $M_{hz\max}$ | Output maximum of the absolute value pitch fin hinge torque for the TVC design stage | (ft-lb) |

m, M

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|---|--------------|
| M_{NDQ} | Aerodynamic damping moment about vehicle center-of-gravity in pitch (L5235) | (ft-lb) |
| M_{NDR} | Aerodynamic damping moment about vehicle center-of-gravity in yaw (L5236) | (ft-lb) |
| M_{Nj} | Input Mach number for aerodynamic normal force coefficient representation where $j = 1, 2, \dots, 15$ per stage (Lk223, 228, etc) | (dim) |
| M_{NP} | Aerodynamic rolling moment about vehicle center-of-gravity (L5213) | (ft-lb) |
| M_{NQ} | Aerodynamic yawing moment about vehicle center-of-gravity (L5211) | (ft-lb) |
| M_{NF} | Aerodynamic yawing moment about vehicle center-of-gravity (L5212) | (ft-lb) |
| M_{NSQ} | Aerodynamic static pitching moment about vehicle center-of-gravity (L5332) | (ft-lb) |
| M_{NSR} | Aerodynamic static yawing moment about vehicle center-of-gravity (L5233) | (ft-lb) |
| M_{PAC} | Pitch aerodynamic control moment per radian angle of attack (L5241) | (ft-lb) |
| M_{PAD} | Pitch aerodynamic disturbing moment per radian angle of attack (L5244) | (ft-lb) |
| M_{PCD} | Total pitch control moment per radian deflection angle (L5251) | (ft-lb) |
| M_{PDA} | Total pitch disturbing moment per radian angle of attack (L5250) | (ft-lb) |
| M_{PMC} | Pitch main thrust control moment per radial TVC deflection angle (L5234) | (ft-lb) |
| M_{PRR} | Pitch inertial rotation reaction moment used in the automatic gain logic (L5235) | (ft-lb) |

m, M

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|--|--------------|
| M_{PTC} | Pitch total thrust control moment per radian TVC deflection angle (L5231) | (ft-lb) |
| \bar{M}_Q | Input aerodynamic pitch damping moment due to pitch rate multiplier (Lk299) | (dim) |
| $M_{q\alpha}$ | Output Mach number at maximum $q\alpha'$ during the TVC duty cycle stage | (dim) |
| M_{RAC} | Roll aerodynamic control moment per radian fin deflection angle (L5243) | (ft-lb) |
| M_{RAP} | Aerodynamic rolling moment induced by raceways (L5222) | (ft-lb) |
| M'_{Rj} | Input Mach number for aerodynamic rolling moment, $j = 1, 2, \dots, 10$ (Lk673, 675, etc) | (dim) |
| M_{RRR} | Roll Rotation Reaction moment used in the automatic gain logic (L5240) | (ft-lb) |
| M_{TDQ} | Movable nozzle tail-wag-dog moment about vehicle center-of-gravity in pitch (L5217) | (ft-lb) |
| M_{TDR} | Movable nozzle tail-wag-dog moment about vehicle center-of-gravity in yaw (L5218) | (ft-lb) |
| M_y | Mode type | (dim) |
| M'_y | Input initial or restart type of mode control flag (L0007) | (dim) |
| M_{YAC} | Yaw aerodynamic control moment per radian angle of side slip (L5242) | (ft-lb) |
| M_{YAD} | Yaw aerodynamic disturbing moment per radian angle of side slip (L5245) | (ft-lb) |
| M_{yj} | Input and output mode type control where $j = 1, 2, \dots, 10$. If 1 rigid body with controls, and 2 rigid body with controls (L0600, 603, etc) | (dim) |

m, M

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|--------------------------|---|--------------|
| M_{YRR} | Yaw inertial rotation reaction moment used in the automatic altitude gain logic (L5239) | (ft-lb) |
| $\bar{M}_{\dot{\alpha}}$ | Input aerodynamic pitch damping moment due to rate change of angle of attack multiplier (Lk300) | (dim) |
| $M_{\delta P}$ | Rolling moment due to the aerodynamic control force (L5228) | (ft-lb) |
| $M_{\delta Q}$ | Pitching moment due to the aerodynamic control force (L5226) | (ft-lb) |
| $M_{\delta R}$ | Yawing moment due to the aerodynamic control force (L5227) | (ft-lb) |

n, N

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|---|--------------|
| n_{dc} | Output of number TVC duty cycle t_B data points | (dim) |
| n_g | Output number of velocity data points used in calculating the coefficients for the pitch steering equations | (dim) |
| n_i | Output iteration number of the hunting procedure | (dim) |
| n | Burning rate exponent used in internal ballistic evaluation is set to 0.6 if not input (Lk097) | (dim) |
| n'_c | Input and output internally calculated number of control nozzles for the cluster motor logic (Lk38i) | (dim) |
| n'_m | Input and output internally calculated number of motors in the stage cluster (Lk38l) | (dim) |
| n_{t1} | Input trajectory number limit. No more than n trajectories will be computed during the hunting procedure (P1) by varying X (L0075) | (dim) |
| n_{t2} | Input specified maximum number of hunt predictions (P2) beyond the initial array. If n_{t2} is input a negative number, the hunt will restart after $ n_{t2} $ iterations (L0090) | (dim) |
| \tilde{N}_k | Input normal force control function and normal force multiplier. If input zero, the multiplier is set to 1 and if nonzero, the normal force is determined from input and multiplied by N_k where $k = 1, 2, 3, 4$ (Lk22l) | (dim) |
| N_{NVA} | Force normal to velocity vector per radian angle of attack (L516l) | (lb) |
| N_{PAC} | Pitch aerodynamic control normal force per radian fin deflection angle (L5158) | (lb) |

n, N

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|----------------|--|--------------|
| N_{PAD} | Pitch aerodynamic disturbing normal force per radian angle of attack (L5159) | (lb) |
| N_{PCD} | Total pitch control normal force per radian deflection angle (L5162) | (lb) |
| N_{PDA} | Total pitch disturbing normal force per radian angle of attack (L5160) | (lb) |
| N_{PEA} | Pitch trim normal force per radian angle of attack (L5163) | (lb) |
| N_{PY} | Aerodynamic force due to damping in yaw (L5167) | (lb) |
| N_{PZ} | Aerodynamic force due to damping and pitch (L5168) | (lb) |
| | Instantaneous yaw aerodynamic axial normal forces directed opposite to the direction of the Y_b axis (L5165) | (lb) |
| N_Z | Instantaneous pitch aerodynamic normal forces directed opposite to the direction of the Z_b axes (L5166) | (lb) |
| $N_{\delta y}$ | Aerodynamic yaw fin normal force (L5156) | (lb) |
| $N_{\delta z}$ | Aerodynamic pitch fin normal force (L5157) | (lb) |

p, P

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-----------------------------|--|----------------------------|
| P | Glide phase orbital period (L5014) | (min) |
| P _a | Ambient pressure at the missile (L5068) | (lb/ft ²) |
| P* | Main motor nozzle critical pressure used in separated flow equations (L5072) | (lb/in. ²) |
| P _{arC} | Input complementary table thrust reference atmospheric pressure (Lk109) | (lb/ft ²) |
| P _{aRM} | Input main table thrust reference atmospheric pressure (Lk020) | (lb/ft ²) |
| P _b | Instantaneous vehicle angular roll velocity, roll clockwise is positive (L5709) | (deg/sec) |
| \dot{P}_b | Instantaneous vehicle angular roll acceleration, roll clockwise positive (L5759) | (deg/sec ²) |
| P _{bo} | Input initial vehicle roll rate (L0033) | (deg/sec) |
| P _c | Main motor chamber pressure used in separated flow equation (L5734) | (lb/in. ²) |
| \dot{P}_C | Time rate change of chamber pressure (L5784) | (lb/in. ² -sec) |
| P _{ca} | Output action time average motor chamber pressure for the TVC design duty cycle stage | (lb/in. ²) |
| P _{cc} | Commanded chamber pressure used in pintle motor control logic (L5071) | (lb/in. ²) |
| P _e | Main motor exit pressure used in separated flow equations (L5074) | (lb/ft ²) |
| PL-DA GB, K, KB, N, O | Input flag where nonzero values are required if printlines DA, GB, K, KB, N, O are desired (L0200-209) | (dim) |
| P _d | Base pressure | (lb/in. ²) |
| P _m | Instantaneous desired roll turning rate (L5403) | (deg/sec) |

p, P

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|---|------------------------|
| P_{\max} | Maximum allowable chamber pressure used in internal ballistic evaluation (Lk099) | (lb/in. ²) |
| P_{Mj} | Input vehicle roll turning rate positive if the vehicle is intended to roll clockwise looking at it from the aft end (Ty=1) (L0315, 322, etc) | (deg/sec) |
| P_s | Main motor nozzle separation pressured used in separated flow equations (L5073) | (lb/in. ²) |
| P_1 | Input flag to specify hunt procedure (P1) (L0073) | (dim) |
| P_2 | Input flag to specify hunt procedure (P2). If $P_2 = 0$, by-pass hunt procedure 2; $P_2 = 1$, use a linear response; $ P_2 = 2$, use a quadratic response surface where +2 maximizes and -2 minimizes; $ P_2 = 3$, use an incomplete quadratic response surface where +3 maximizes and -3 minimizes. (L0084) | (dim) |

q, Q

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-------------------|---|---------------------------|
| $q_{q\alpha'}$ | Output dynamic pressure at maximum $q\alpha'$ during the TVC duty cycle stage | (lb/ft) |
| $q\alpha'_{\max}$ | Output product of the maximum absolute value of the dynamic pressure-angle of attack for the TVC design stage | (lb-deg/ft ²) |
| q | Missile dynamic pressure (L5070) | (lb/ft ²) |
| $q_{\max j}$ | Input maximum allowable dynamic pressure of the j-th type of TMC (L807, 817, etc) | (lb/ft ²) |
| q_{\min} | Input minimum allowable dynamic pressure of the j-th type of TMC (L0808, 818, etc) | (lb/ft ²) |
| $q\alpha'$ | Product of total angle of attack and dynamic pressure (L5110) | (lb/deg/ft ²) |
| $q_{(B1)}$ | Missile dynamic pressure at the termination of stage I (L5912) | (lb/ft ²) |
| $q_{(B2)}$ | Missile dynamic pressure at the termination of stage II (L5937, | (lb/ft ²) |
| $q_{(B3)}$ | Missile dynamic pressure at the termination of stage III (L5962, | (lb/ft ²) |
| $q_{(B4)}$ | Missile dynamic pressure at the termination of stage IV (L5987) | (lb/ft ²) |
| \dot{Q}_b | Instantaneous vehicle angular pitch velocity. Pitch up is positive (L5707) | (deg/sec) |
| \ddot{Q}_b | Instantaneous vehicle angular pitch acceleration. Pitch up positive (L5757) | (deg/sec ²) |
| Q_{bo} | Input initial vehicle pitch rate (L0031) | (deg/sec) |
| Q_m | Instantaneous desired pitch turning rate (L5401) | (deg/sec) |

q, Q

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|--|--------------|
| Q_{mj} | Input vehicle pitch turning rate. Positive if the vehicle is intended to pitch up (Ty=1) (L0313, 320, etc) | (deg/sec) |
| Q_{mo} | Input initial command pitch attitude (L0028) | (deg) |

r, R

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|---|--------------------------|
| r_a | Distance between the center of the reference body and apogee during the glide phase | (ft) |
| r_b | Propellant burn rate (L5783) | (m/sec) |
| r'_{b1000} | Input burning rate of propellant at 1,000 lb/in ² chamber pressure and flag to determine evaluation option (Lk002) | (in/sec) |
| r_c | Instantaneous distance between the center of the reference body and the missile (L5035) | (ft) |
| r'_c | Value of r_c at the beginning of the glide phase | (ft) |
| r_{co} | Initial missile radius from center of earth | (ft) |
| r_e | Radius of the earth | (ft) |
| r'_e | Input geometric radius of the earth. If input zero, set equal to 20,926,400 (L0026) | (ft) |
| r_f | Radial distance at the termination of the glide phase | (ft) |
| r_p | Distance between the center of the reference body and perigee during the glide phase | (ft) |
| r_{Ri} | Input distance from the vehicle centerline to the i-th raceway center of pressure, $i = 1, 2$ (Lk66S, 671) | (in) |
| R | Altitude associated geopotential earth radius used in atmosphere model | (ft) |
| R^* | Universal gas constant | (joules/ kilogram °K) |
| R_b | Instantaneous vehicle angular yaw velocity. Yaw right is positive (L5708) | (deg/sec) |

r, R

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|----------------|---|-------------------------|
| \dot{R}_b | Instantaneous vehicle angular yaw acceleration. Yaw right positive (L5758) | (deg/sec ²) |
| R_{bo} | Input initial vehicle yaw rate (L0032) | (deg/sec) |
| R_c | Input radius of cluster for the k-th stage (Lk382) | (ft) |
| R_m | Instantaneous desired yaw turning rate (L5402) | (deg/sec) |
| P_{MI} | Estimated range to target intercept (L5400) | (ft) |
| R_{mj} | Input vehicle yaw turning rate positive if the vehicle is intended to turn right (Ty=1) (L0314, 321, etc) | (deg/sec) |
| R_{MT} | Missile to target range distance (L5437) | (ft) |
| \dot{R}_{MT} | Time rate change of missile to target distance (L5438) | (ft/sec) |
| R_{PFV} | Output ratio of motor chamber pressure to vacuum thrust of the main thrustable of the TVC design stage | (1/in. ²) |
| RR | Input reference run number (L0001) | (dim) |
| RUN | Input run number (L0002) | (dim) |

s, S

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|--|--------------------|
| S | Missile ground range. Distance along the surface of the earth measured clockwise from the launch vertical to the local vertical down range (L5018) | (ft) |
| \dot{S} | Time rate change of missile down range (L5019) | (ft/sec) |
| S_a | Total missile ground range at flight apogee (L5022) | (nm) |
| S_c | Missile cross ground range. Distance along the surface of the earth measured clockwise from launch azimuth (L5028) | (ft) |
| \dot{S}_c | Time rate change of missile cross range (L5021) | (ft/sec) |
| S_{CMI} | Estimated earth surface cross range at target intercept (L5443) | (ft) |
| S_{co} | Input initial earth surface cross-range at trajectory start time (L0043) | (nm) |
| S_E | Total missile ground range to atmospheric entry (L5023) | (nm) |
| S_f | Total missile ground range at the termination of the glide phase (L5024) | (nm) |
| S_{Fz} | Input aerodynamic pitch fin lift and drag coefficient reference area (Lk700) | (ft ²) |
| $S_{f(B1)}$ | Total missile ground range at the termination of the glide phase if the powered flight were to end at the termination of stage I (L5905) | (nm) |
| $S_{f(B2)}$ | Total missile ground range at the termination of the glide phase of the powered flight were to end at the termination of stage II (L5930) | (nm) |

s, S

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|--|--------------------|
| $S_{f(B3)}$ | Total missile ground range at the termination of the glide phase if the powered flight were to end at the termination of stage III (L5955) | (nm) |
| $S_{f(B4)}$ | Total missile ground range at the termination of the glide phase if the powered flight were to end at the termination of stage IV (L5980) | (nm) |
| S_{MI} | Estimated earth surface down range at target intercept (L5441) | (ft) |
| S_{PF} | Input missile platform area used in calculating tumbling aerodynamic axial force coefficients (Lk218) | (ft ²) |
| S_{RC} | Input aerodynamic chord force coefficient reference areas (Lk165) | (ft ²) |
| S_{RN} | Input aerodynamic normal force coefficient reference area (Lk220) | (ft ²) |
| S_{RRi} | Input reference area of the i-th raceway, i = 1, 2 (Lk667, 670) | (ft ²) |
| S_s | Missile slant ground range. Distance along earth surface from the launch vertical to the local vertical slantwise (L5025) | (ft) |
| S_{sh} | Input target range or orbital altitude (L0599) | (nm) |
| SST_2 | Start time stage II (L5006) | (sec) |
| SST_3 | Start time stage III (L5007) | (sec) |
| SST_4 | Start time stage IV (L5008) | (sec) |
| S_T | Target down range (L5731) | (ft) |
| S_{TC} | Target cross range (L5732) | (ft) |
| S_{TCO} | Input initial target position cross range (L0537) | (nm) |

s, S

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|----------------|--|--------------|
| S_{TO} | Input initial target position down range (L0636) | (nm) |
| S_y | Input initial or restart special print flag (L0008) | (dim) |
| S_o | Input missile ground range at the trajectory start time (L0013) | (ft) |
| \dot{S}_T | Target down range rate (L5781) | (ft/sec) |
| \dot{S}_{TC} | Target cross range rate (L5782) | (ft/sec) |

t, T

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|---|--------------|
| t | Instantaneous time (L5000) | (sec) |
| t_a | Total flight time to the glide phase apogee altitude (L5012) | (sec) |
| t_{Ba} | Output TVC duty cycle stage time | (sec) |
| t_B | Time from the current stage initiation (L5001) | (sec) |
| t_{B2} | Time from stage II initiation zero if I-II staging has not occurred (L5002) | (sec) |
| t_{B3} | Time from stage III initiation zero if II-III staging has not occurred (L5003) | (sec) |
| t_{B4} | Time from stage IV initiation zero if III-IV staging has not occurred (L5004) | (sec) |
| t_{Bf} | Trajectory burnout time for the stage below (L5009) | (sec) |
| t_{Bqj} | Output stage time which TVC duty points occur | (sec) |
| t_{cj} | Input limit of the computing interval Δt_{cj} where $j = 1, 2, \dots, 8$ (L0169, 171, etc) | (sec) |
| t'_{Cj} | Input complementary thrust-weight switching time from stage initiation where $j = 1, 2, 3, \dots, 25$ per stage (Lk111, 114, etc) | (sec) |
| t_E | Total flight time to atmospheric entry (L5013) | (sec) |
| t_f | Total flight time to the termination of the glide phase (L5014) | (sec) |
| $t_{f(B1)}$ | Total flight time to the termination of the glide phase if the powered flight were to end at the termination of stage I (L5916) | (sec) |

t, T

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|----------------|---|--------------|
| $t_{f(B2)}$ | Total flight time to the termination of the glide phase if the powered flight were to end at the termination of stage II (L5941) | (sec) |
| $t_{f(B3)}$ | Total flight time to the termination of the glide phase if the powered flight were to end at the termination of stage III (L5966) | (sec) |
| $t_{f(B4)}$ | Total flight time to the termination of the glide phase if the powered flight were to end at the termination of stage IV (L5991) | (sec) |
| t_k | Stage start time (L5005) | (sec) |
| t_k^i | Input start time with the initial stage K_k (L0005) | (sec) |
| t_{MI} | Estimated time to intercept (L5439) | (ft) |
| t_{Mj}^i | Input main thrust-weight switching time from stage initiation where $j = 2, 3, \dots$, or 25 per stage (Lk023, 026, etc) | (sec) |
| t_{Pj} | Input limit of the main printline print interval where $j = 1, 2, \dots, 8$ (L0185, 187, etc) | (sec) |
| t_{pj} | Input limit of the auxiliary printline print interval where $j = 1, 2, \dots, 11$ (L0221, 223, etc) | (sec) |
| $t_{q\alpha'}$ | Output TVC duty cycle stage time at maximum $q\alpha'$ | (sec) |
| t_{Ri}^i | Input operating time from stage initiation of the roll control function for the i -th zone, $i = 2, 3$ (Lk647, 667) | (sec) |
| t_T | Time from target maneuvering initiation (L5010) | (sec) |
| t_{Tj} | Input target time terminating the j -th target acceleration value of dynamical condition table (L0640, 644, etc) | (sec) |

t, T

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-------------------|--|--------------|
| t_{TS} | Target start time (L5011) | (sec) |
| t_{VPj} | Input time value for specific velocity - time profile used in $Fy=1$ TMC $j = 1, 2, \dots, 15$ (L0870, 872, etc) | (sec) |
| $t_{\eta P}$ | Output stage time at which maximum magnitude pitch thrust vector deflection angle occurs during the TVC design stage (δ_{Pmax}) | (sec) |
| t_o | Input trajectory start time (L0004) | (sec) |
| T_{Bj} | Input staging values flag, $j = 1, 2, \dots, 5$ (L0270, 272, etc) | (dim) |
| T_{mj} | Input maximum print region flag (L0260, 262, etc) | (dim) |
| T_{Tj} | Input transformation flag used in hunting procedure (P2) $j = 1, 2, \dots, 7$ (L0098, 107, etc) | (dim) |
| TMC_j | Input thrust dynamic mode of the j -th type TMC (L0803, 813, etc) | (dim) |
| T_M | Instantaneous molecular scale temperature | (°K) |
| T_{MB}, T_{MBj} | Base molecular scale temperature and tabular values associated with the atmosphere representation | (°K) |
| T_{Tj} | Input transformation flag used in hunting procedure (P2) $j = 1, 2, \dots, 7$ (L0098, 107, ..., 152) | (dim) |
| T_y | Type of flight | (dim) |
| T'_{yk} | Input initial or restart type of flight control flag (L0006) | (dim) |
| T_{yj} | Input and output type of flight control flag where $j = 1, 2, \dots, \text{or } 16$ (L0310, 317 etc) | (dim) |

u, U

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|---|--------------|
| u_j | Elements $\{j = 1, 2, \dots, 5\}$ of the vector containing the numeric value of the independent variables used in the generation of steering coefficients | (dbi) |
| $[U_1]$ | Matrix containing specified elements u_j for use in the steering equation coefficient acquisition | (dbi) |
| $[U_2]$ | A vector containing specified elements u_j for use in the steering equation coefficient acquisition | (dbi) |
| U_{cz} | Output pitch aerodynamic control fin center of pressure as a ratio of fin chord length (L5568) | (dim) |
| U_{czi} | Input pitch aerodynamic control fin center of pressure as a ratio of fin chord length (Lk715, Lk721) | (dim) |
| $[U_g]$ | A vector which contains a scaled version of the steering equation steering coefficients | (dim) |
| U_{gi} | Elements of the $[U_g]$ vector which are the scaled version of the steering equation steering coefficients $i = 1, 2, 3, \text{ or } 4$ | (dim) |
| U_{go} | Mean of the regressed least squares fit for use in the steering equation coefficient acquisition | (dim) |
| U_{hz} | Input pitch movable control fin hinge axis to the leading fin base root location distance to the pitch fin base root length ratio (Lk702) | (dim) |

v, V

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-----------------|--|------------------------|
| v_{TO} | Input target initial velocity at start of start of target maneuvering (L0632) | (ft/sec) |
| v_w | Instantaneous wind speed change (L5056) | (ft/sec) |
| \dot{v}_w | Instantaneous wind speed time rate change (L5057) | (ft/sec) |
| v_{wj} | Input (with altitude h) wind speeds where $j = 1, 2, \dots, 30$ (L0411, 414, etc) | (ft/sec) |
| V_a | Missile velocity with respect to air (L5049) | (ft/sec) |
| V_{aE} | Velocity with respect to the ambient air at entry (L5058) | (ft/sec) |
| V_C | Target transverse velocity (L5727) | (ft/sec) |
| V_{cI} | Chamber volume (L5078) | (in. ³) |
| V_e | Missile earth referenced velocity (L5046) | (ft/sec) |
| \dot{V}_e | Time rate change of missile earth reference velocity (L5047) | (ft/sec ²) |
| \dot{V}_{ecq} | Command acceleration to constrain dynamic pressure used in the TMC command logic (L5062) | (ft/sec ²) |
| V_{ek} | Earth fixed velocity at stages (L5048) | (ft/sec) |
| V_{eo} | Input missile velocity at the trajectory start time (L0010) | (ft/sec) |
| V_I | Missile inertial velocity (L5050) | (ft/sec) |
| V_{Ia} | Missile inertial velocity at apogee if powered flight ends at the time being printed (L5041) | (ft/sec) |
| $V_{I(B1)}$ | Missile inertial velocity at the termination of stage I (L5901) | (ft/sec) |
| $V_{I(B2)}$ | Missile inertial velocity at the termination of stage II (L5926) | (ft/sec) |

v, V

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-----------------|---|------------------------|
| $V_{I(B3)}$ | Missile inertial velocity at the termination of stage III (L5951) | (ft/sec) |
| $V_{I(B4)}$ | Missile inertial velocity at the termination of stage IV (L5976) | (ft/sec) |
| V_{IE} | Inertial velocity at entry conditions (L5059) | (ft/sec) |
| V_{If} | Missile inertial velocity at apogee and impact of intercept, respectively, if powered flight and the atmosphere end at the time being printed (L5042) | (ft/sec) |
| $V_{If(B1)}$ | Missile inertial velocity at the termination of the glide phase if the powered flight were to end at the termination of stage I (L5918) | (ft/sec) |
| $V_{If(B2)}$ | Missile inertial velocity at the termination of the glide phase if the powered flight were to end at the termination of stage II (L5945) | (ft/sec) |
| $V_{If(B3)}$ | Missile inertial velocity at the termination of the glide phase if the powered flight were to end at the termination of stage III (L5968) | (ft/sec) |
| $V_{If(B4)}$ | Missile inertial velocity at the termination of the glide phase if the powered flight were to end at the termination of stage IV (L5993) | (ft/sec) |
| V_N | Target normal velocity (L5726) | (ft/sec) |
| V_T | Target tangential velocity (L5725) | (ft/sec) |
| V_{VPj} | Input earth reference velocity for the specific velocity - time profile used in $F_y=1$, TMC $j = 1, 2, \dots, 15$ (L0871, 873, etc) | (ft/sec) |
| V_{xxx} | Command velocity used in the TMC command logic. V_{ecv} if $F_y = 1$, V_{ecm} if $F_y = 4$ (L5060) | (ft/sec ²) |
| \dot{V}_{xxx} | Command acceleration used in the TMC command logic. \dot{V}_{ecv} if $F_y = 1$, \dot{V}_{ecm} if $F_y = 2$, and zero if $F_y = 1$ and $F_y = 2$ (L5061) | (ft/sec ²) |

v, V

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|----------------|--|--------------|
| \dot{v}_{Cj} | Target transverse acceleration (L5777) | (ft/sec) |
| \dot{v}_{Nj} | Target normal acceleration (L5776) | (ft/sec) |
| \dot{v}_{Tj} | Target tangential acceleration (L5775) | (ft/sec) |

w, W

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-----------------|--|--------------|
| W | Total instantaneous missile weight (L5093) | (lb) |
| \dot{W} | Total expended instantaneous missile mass flow weight (L5094) | (lb/sec) |
| \bar{W} | Input stage weight multiplier. If input zero, is set internally to one and if nonzero, the input weight used in the mass properties table W_j ($j = 1, 2, \dots, 15$) is multiplied by W (Lk478) | (dim) |
| $\dot{\bar{W}}$ | Instantaneous total motor weight flow | (lb/sec) |
| W_B | Instantaneous gross vehicle weight minus the useful load (L5095) | (lb) |
| $W_{(B1)}$ | Total missile weight at the termination of stage I (L5904) | (lb) |
| $W_{(B2)}$ | Total instantaneous missile weight at the termination of stage II (L5929) | (lb) |
| $W_{(B3)}$ | Total instantaneous missile weight at the termination of stage III (L5954) | (lb) |
| $W_{(B4)}$ | Total instantaneous missile weight at the termination of stage IV (L5979) | (lb) |
| W_C | Total instantaneous expended complementary weight (L5099) | (lb) |
| \dot{W}_C | Total instantaneous expended complementary weight flow rate (L5100) | (lb/sec) |
| \hat{W}_C | Total complementary weight flow at t_{Cj} | (lb/sec) |
| \dot{W}_{Cj} | Input complementary weight flow at t_{Cj}^1 where $j = 1, 2, \dots, 25$ per stage (Lk113, 116, etc) | (lb/sec) |
| W_{Cok} | Input initial complementary weight for the k-th stage (Lk105) | (lb) |
| W_{exi} | Input estimated weight of the TVC system expended weight during the TVC design stage during the original vehicle flight (L0678) | (lb) |

w, W

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|----------------|---|--------------|
| W_{JT} | Total weight jettisoned (L5096) | (lb) |
| W_{JTj} | Input weight to be jettisoned when σ_j parameter had K_j value (L0049, 52, etc) | (lb) |
| W_j | Input vehicle weight to relate the input moment of inertia values $j = 1, 2, \dots, 15$ per stage (Lk488-498) | (lb) |
| W_{kdc} | Output main motor stage weight for the design stage | (lb) |
| W_M | Total instantaneous expended main weight (L5097) | (lb) |
| \dot{W}_M | Total instantaneous expended main weight flow rate (L5098) | (lb/sec) |
| \dot{W}_{Mj} | Input main weight flow at t_{Mj} where $j = 1, 2, \dots, 25$ per stage (Lk022, 025, etc) | (lb/sec) |
| \hat{W}_{Mj} | Total instantaneous main weight flow at t_{Mj} where $j = 1, 2, \dots, \text{ or } 25$ | (lb/sec) |
| W_{MO} | Input initial main weight for the k-th stage (Lk006) | (lb) |
| \dot{W}_{MP} | Mass flow rate of gases thru pintle nozzle throat (L5786) | (lb/sec) |
| W_n | Input stage movable portion nozzle weight (Lk482) | (lb) |
| W_{PL} | Input payload weight (L0020) | (lb) |
| W_{pr} | Weight of propellant removed. Used in TMC logic (L5736) | (lb) |
| \dot{W}_q | Output motor weight flow (\dot{W}) at t_{Bq} the TVC duty cycle point | (lb/sec) |
| W_R | Instantaneous expended weight due to roll control motor operation (L5720) | (lb) |
| \dot{W}_R | Roll control system mass flow rate (L5770) | (lb/sec) |

w, W

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|--|--------------|
| W_S | Stage weight (L5101) | (lb) |
| W_{SC} | Initial weight of complementing motor (L5103) | (lb) |
| W_{SM} | Initial weight of main motor (L5102) | (lb) |
| W_{TVC} | Input and output estimated TVC system fixed weight. Used in TVC design stage for the reflly option (L0677) | (lb) |
| W_{ol} | Input stage I liftoff weight used in roll control requirements (L0676) | (lb) |
| W_o | Output TVC duty cycle stage liftoff weight used in the roll control requirements | (lb) |

x, X

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|------------------|---|------------------------|
| \dot{X}_{abb} | X component of missile velocity with respect to the ambient air in the b system (L5507) | (ft/sec) |
| \ddot{X}_{abb} | x component of missile acceleration with respect to ambient air in the b system (L5510) | (ft/sec ²) |
| \dot{X}_{db} | Inertial component of missile velocity along x_b axis (L5537) | (ft/sec) |
| \ddot{X}_b | Missile acceleration along vehicle body axes, position forward (L5540) | (ft/sec ²) |
| X_{cc} | Earth centered missile position northern axis component (L5513) | (ft) |
| \dot{X}_{cc} | Northern component of missile velocity in earth centered coordinates (L5516) | (ft/sec) |
| \ddot{X}_{cc} | Northern component of missile acceleration in earth centered coordinates (L5519) | (ft/sec ²) |
| x_{cg} | Instantaneous center-of-gravity body station numbers (L5584) | (ft) |
| x_{cgj} | Input instantaneous (with total vehicle weight, W_j) center-of-gravity body station numbers, respectively, where $j = 1, 2, \dots, 15$ per stage (Lk489, 499, etc) | (dbi & ft) |
| X_{cgq} | Output vehicle center-of-gravity at t_{Bq} ; the TVC duty cycle point | (ft) |
| x_{cp} | Input and instantaneous (with Mach number M) aerodynamic normal force center of pressure body station numbers, respectively, where $j = 1, 2, \dots, 15$ per stage respectively (L5583) | (ft & dbi) |
| x_{cpj} | Input and output instantaneous (with Mach number M) aerodynamic normal force center of pressure body station numbers, respectively, where $j = 1, 2, \dots, 15$ per stage (Lk227, 232, etc) | (dbi & ft) |
| x'_e | Input stage thrust gimbal body station numbers, also output for the TVC duty cycle (Lk431) | (ft) |

x, X

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-----------------|--|------------------------|
| x_E^1 | Input and computed stage nozzle exit body station (Lk419) | (ft) |
| X_{gg} | Instantaneous component of vehicle position in the generalized coordinates down range from launcher (L5522) | (ft) |
| \dot{X}_{gg} | Instantaneous component of vehicle velocity in the generalized coordinates down range from launcher (L5525) | (ft/sec) |
| \ddot{X}_{gg} | Instantaneous component of vehicle acceleration in the generalized coordinates down range from launcher (L5528) | (ft/sec ²) |
| x_{hz} | Input missile body station of the pitch fin hinge axis (Lk701) | (ft) |
| x_{ij} | Input initial array reference independent variable designated by code input that is used in hunting procedure (P2) (L0092, 101, etc) | (dbi) |
| x_j | Independent variable designated by code input that is varied during hunting procedure (P2) where $j = 1, 2, \dots, \text{or } 7$ | (dbi) |
| x_{Lj} | Input lower limit that an independent variable may assume a value in hunt procedure (P2) where $j = 1, 2, \dots, 7$ (L0161-167) | (dbi) |
| x_n | Input stage movable portion of nozzle center-of-gravity body station (Lk484) | (dbi) |
| x_{nf} | Input body station of nozzle flange. Use 1 in the TVC design program (L0680) | (ft) |
| x_{Pa} | Computed stage aft end propellant grain body station (L5588) | (ft) |
| x_{Pa}^1 | Input stage aft end of propellant grain body station (Lk418) | (ft) |

x, X

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|------------------|--|------------------------|
| x_{Pc} | Input missile body station of the centroid of the platform area (Lk219) | (ft) |
| x_{pf} | Computed stage forward end of propellant grain body station (L5587) | (ft) |
| x'_{Pf} | Input stage forward end of propellant grain body station (Lk417) | (ft) |
| x'_{RQ} | Input and calculated pitch damping moment due to pitch rate reference moment point body station (Lk302) | (dbi & ft) |
| $x'_{R\alpha}$ | Input and calculated pitch damping moment due to rate change of angle of attack reference moment point body station (Lk304) | (dbi & ft) |
| x_{Uj} | Input upper limit that an independent variable may assume a value used in hunt procedure (P2) where $j = 1, 2, \dots, 7$ (L0154-160) | (dbi) |
| \dot{X}_{wee} | Transformed launcher northerly component of wind velocity at missile location (L5549) | (ft/sec) |
| \dot{X}_{wl1} | Local northerly component of wind velocity (L5531) | (ft/sec) |
| \ddot{X}_{wl1} | Local time rate change of northern component of wind velocity (L5534) | (ft/sec) |
| \dot{X}_{11} | Local northerly component of missile velocity (L5534) | (ft/sec) |
| \ddot{X}_{11} | Local northerly component of missile acceleration (L5546) | (ft/sec ²) |
| \dot{X}_{111} | Local northerly component of missile inertial velocity (L5552) | (ft/sec) |
| X | Output independent variable designated by code input that is varied during the hunting procedure {P1} | (dbi) |
| X_{cco} | Initial earth centered missile northern axis component | (ft) |

x, X

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-----------------|--|------------------------|
| X_{cg} | Input stage center-of-gravity position multiplier (Lk479) | (dbi) |
| \bar{X}_{cp} | Input stage aerodynamic normal force center of pressure multiplier (Lk222) | (dbi) |
| \bar{X}_e | Input stage thrust gimbal position multiplier (Lk430) | (dbi) |
| \dot{X}_{ee} | Instantaneous components of vehicle velocity, north of the launcher (L5701) | (ft/sec) |
| X_{ee} | Instantaneous component of vehicle position north of launcher (L5704) | (ft) |
| \ddot{X}_{ee} | Instantaneous northerly component of vehicle acceleration at launcher (L5751) | (ft/sec ²) |
| X_{ee}^* | Northern component along launcher of missile position | (ft) |
| X_{eeo} | Initial component of vehicle position north of launcher | (ft) |
| \dot{X}_{eeo} | Initial component of vehicle velocity north of launcher | (ft/sec) |
| X_i | Input value of the first guess of X used in hunting procedure (L0080) | (dbi) |
| X_j | Output independent variable used in hunting procedure (P2) where j = 1, 2, ..., or 7 | (dbi) |
| \bar{X}_j | Computed value of X during the hunting procedure (P1) where j = 1, 2, ..., 4 | (dbi) |

y, Y

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|------------------|--|------------------------|
| \dot{Y}_{abb} | Y component of the missile velocity with respect to the ambient air in the b system (L5508) | (ft/sec) |
| \ddot{Y}_{abb} | y component of missile acceleration with respect to the ambient air in the b system (L5511) | (ft/sec) |
| \dot{Y}_{bb} | Inertial component of missile velocity along y_b axis (L5538) | (ft/sec) |
| \ddot{Y}_b | Inertial component of missile acceleration y_b axes (L5541) | (ft/sec) |
| Y_{cc} | Earth centered missile position east from launcher (L5514) | (ft) |
| \dot{Y}_{cc} | East from launcher component of missile velocity in earth centered coordinate (L5517) | (ft/sec) |
| \ddot{Y}_{cc} | East from launcher component of missile acceleration in earth centered coordinates (L5520) | (ft/sec ²) |
| y_{cg} | Center-of-gravity offset bias distance positive in the Z_b direction (L5585) | (ft) |
| y'_{cg} | Input center-of-gravity offset bias distance in yaw, positive to the right (Lk481) | (dbi) |

y, Y

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-----------------|--|------------------------|
| y_{cgj} | Input instantaneous 'with total vehicle weight, (W) center of gravity butt line number, where $j = 1, 2, \dots, 15$ per stage (Lk493, 503, etc) | (dbi and ft) |
| y_e | Thrust gimbal yaw point eccentricity position in the Y_b axis direction (L5589) | (ft) |
| y_e' | Input stage thrust gimbal yaw eccentricities. Positive in the Y_b axis direction (Lk432) | (ft) |
| Y_{gg} | Instantaneous component of vehicle position in the generalized coordinates cross range from launcher (L5523) | (ft) |
| \dot{Y}_{gg} | Instantaneous component of vehicle velocity in the generalized coordinates crosswise from launcher (L5526) | (ft/sec) |
| \ddot{Y}_{gg} | Instantaneous component of vehicle acceleration in the generalized coordinates crosswise from launcher (L5529) | (ft/sec ²) |
| y_i | Dependent variable used in hunting procedure (P2) where $j = 1, 2, \dots, \text{or } 7$ | (dbi) |
| y_{Li} | Input desired dependent variable or lower constraint boundary of the dependent variable designated by code input that is used in hunting procedure (P2) where $j = 1, 2, \dots, 7$ (L0095, 104, etc) | (dbi) |

y, Y

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|------------------|---|------------------------|
| y_{Ui} | Input upper constraint boundary of the dependent variable designated by code input that is used in hunting procedure (P2) where $j = 1, 2, \dots, 7$ (L0096, 105, etc) | (dbi) |
| \ddot{y}_{wee} | Transformed launcher easterly component of wind velocity at missile location (L5550) | (ft/sec) |
| \dot{y}_{wll} | Local easterly component of wind velocity (L5532) | (ft/sec) |
| \ddot{y}_{wll} | Local time rate change of easterly component of wind velocity (L5535) | (ft/sec ²) |
| \dot{y}_{ll} | Local easterly component of missile velocity (L5544) | (ft/sec) |
| \ddot{y}_{ll} | Local easterly component of missile acceleration (L5547) | (ft/sec ²) |
| \dot{y}_{lll} | Local easterly component of missile inertial velocity (L5553) | (ft/sec) |
| y_{cco} | Initial earth centered missile position east from launcher | (ft) |
| y_{ee} | Instantaneous component of vehicle position east of launcher (L5705) | (ft) |

y, Y

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-----------------|--|------------------------|
| \dot{y}_{ee} | Instantaneous components of vehicle velocity, east of the launcher (L5703) | (ft/sec) |
| \ddot{y}_{ee} | Instantaneous eastern component of vehicle acceleration at launcher (L5752) | (ft/sec ²) |
| y_{ee}^* | Eastern component along launcher of missile position | (ft) |
| y_{eeo} | Initial component of vehicle position east of launcher | (ft) |
| \dot{y}_{eeo} | Initial component of vehicle velocities east of launcher | (ft) |

z, Z

| <u>Symbol</u> | <u>Definition</u> | <u>Unit</u> |
|------------------|---|------------------------|
| z | Input dependent variable to be maximized or minimized designated by code input used in the hunting procedure (P2) | (dbi) |
| z_{cg} | Center-of-gravity offset bias distance, positive down (L5586) | (dbi) |
| z'_{cg} | Input center-of-gravity offset bias distance, in pitch, positive down (Lk480) | (dbi) |
| z_{cgj} | Input instantaneous (with total vehicle weight, W_j) center-of-gravity offsets, respectively, where $j = 1, 2, \dots, 15$ per stage. Positive in the Z_b axis direction (Lk491, 501, etc) | (dbi and ft) |
| z_e | Thrust gimbal pitch point position in the Z_b axis direction (L5590) | (ft) |
| z'_e | Input stage thrust gimbal pitch point eccentricities, respectively. Positive in the Z_b axis direction (Lk433) | (dbi and ft) |
| \dot{z}_{abb} | z component of missile velocity with respect to the ambient air in the b system (L5509) | (ft/sec) |
| \ddot{z}_{abb} | z component of missile acceleration with respect to the ambient air in the b system (L5512) | (ft/sec ²) |
| \dot{z}_{bb} | Inertial component of missile velocity along z_b axis. (L5539) | (ft/sec) |

z, Z

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-----------------|--|------------------------|
| \ddot{Z}_b | Inertial components of missile acceleration along z_b axis (L5542) | (ft/sec ²) |
| Z | Output primary dependent variable which is to be maximized or minimized used in hunting procedure (P2) | (dbi) |
| Z_j | Output secondary or constrained dependent variables which are used in hunting procedure (P2), $j = 1, 2, \dots, 7$ | (dbi) |
| Z_{cc} | Earth centered missile position away from earth axis at launcher longitude (L5515) | (ft) |
| \dot{Z}_{cc} | Away from launcher longitude component of missile velocity in earth centered coordinates (L5518) | (ft/sec) |
| \ddot{Z}_{cc} | Away from launcher longitude component of missile acceleration in earth centered coordinates (L5521) | (ft/sec ²) |
| Z_{cco} | Initial earth centered missile position away from earth axis at launcher longitude | (ft) |
| Z_{ee} | Instantaneous component of vehicle position negative up from sea level launcher latitude (L5706) | (ft) |
| \dot{Z}_{ee} | Instantaneous component of vehicle velocity negative up from sea level launcher latitude (L5703) | (ft/sec) |
| \ddot{Z}_{ee} | Instantaneous downward component of vehicle acceleration at launcher (L5753) | (ft/sec ²) |

z, Z

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|------------------|--|------------------------|
| Z_{ee}^* | Downward component along launcher of missile position | (ft) |
| Z_{eeo} | Initial component of vehicle position negative up from sea level launcher | (ft) |
| \dot{Z}_{eeo} | Initial component of vehicle velocity negative up from sea level launcher | (ft/sec) |
| Z_{gg} | Instantaneous component of vehicle positive vertical from launcher (L5524) | (ft) |
| \dot{Z}_{gg} | Instantaneous component of vehicle velocity in the generalized coordinates vertical from launcher (L5527) | (ft/sec) |
| \ddot{Z}_{gg} | Instantaneous component of vehicle acceleration in the generalized coordinates vertical from launcher (L5530) | (ft/sec ²) |
| \dot{Z}_{wee} | Transformed launcher downward component of wind velocity at missile location (L5551) | (ft/sec) |
| \dot{Z}_{wll} | Local downward component of wind velocity (L5533) | (ft/sec) |
| \ddot{Z}_{wll} | Local time rate change of downward component of wind velocity (L5536) | (ft/sec ²) |
| \dot{Z}_{11} | Local downward component of missile velocity (L5545) | (ft/sec) |
| \ddot{Z}_{11} | Local downward component of missile acceleration (L5548) | (ft/sec ²) |

z, Z

Symbol

Definition

Units

\dot{z}_{11}

Local downward component of missile
inertial velocity
(L5554)

(ft/sec)

| <u>α</u> | | |
|----------------------------|---|--------------|
| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
| α | Instantaneous pitch angle of attack; positive if the vehicle centerline is above the air velocity vector (L5301) | (deg) |
| $\dot{\alpha}$ | Time rate change of angle of attack (L5302) | (deg/sec) |
| α' | Total vehicle angle of attack; angle between the centerline of the vehicle and the missile air velocity vector; always positive (L5309) | (deg) |
| $\bar{\alpha}$ | Still wind angle of attack (L5310) | (deg) |
| $\bar{\alpha}'$ | Still air total angle of attack (L5305) | (deg) |
| $\dot{\bar{\alpha}}$ | Time rate change of still wind angle of attack (L5307) | (deg/sec) |
| α_{c_j} | Input command angle of attack (L5303) | (deg) |
| α_c | Commanded angle of attack | (deg) |
| α_{c_j} | Input commanded angle of attack used in the constant angle of attack and angle of side slip ($Ty = 2$) (L0313, 320, etc) | (deg) |
| α'_d | Input nozzle half angle used in the separated flow nozzle thrust equation (L0316) | (deg) |
| α_E | Effective pitch angle of attack used to compute the aerodynamic normal force (L5311) | (deg) |
| α'_E | Effective total angle of attack used to compute the aerodynamic normal force (L5304) | (deg) |
| α_f | Angle of attack rotated to command vertical | (deg) |
| α_{ml} | Commanded angle of attack for constant angle of attack flight ($Ty = 2$) (L5312) | (deg) |
| α_{maxj} | Input limit of angle of attack during the j-th type of flight (L0315, 322, etc) | (deg) |

Symbol

α
Definition

Units

α_p

Propellant diffusivity used in internal ballistic
evaluation is set to 0.00027 if not input (Lk09u)

(in.²/sec)

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------------|--|--------------|
| β | Angle of side slip. Positive if the vehicle centerline is left of the air velocity vector when viewed from the rear of the vehicle (L5315) | (deg) |
| $\dot{\beta}$ | Time rate change of angle of side slip (L5316) | (deg/sec) |
| $\bar{\beta}$ | Still wind angle of side slip (L5318) | (deg) |
| $\dot{\bar{\beta}}$ | Time rate change of still wind angle of side slip (L5308) | (deg/sec) |
| $\bar{\beta}'$ | Still wind angle of side slip in the commanded coordinate system used to evaluate the local bank angle (L5319) | (deg) |
| β_c | Commanded angle of side slip (L5317) | (deg) |
| β_{c_j} | Input commanded angle of side slip used in the constant angle of attack and angle of side slip ($T_y = 2$) (L5314, 321, etc) | (deg) |
| β_E | Effective yaw angle of side slip used to compute the aerodynamic normal face (L5320) | (deg) |
| $\beta_{\Delta t}$ | Angle of side slip rotated to the commanded horizontal | (deg) |

γ, Γ

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|------------------|---|--------------|
| γ_d' | Input and output calculated ratio of specific heats of the rocket motor exhaust gases. If input zero 1.18 is used. Used in separated flow nozzle thrust equations (Lk014) | (dim) |
| γ_G | Calculated local angle of velocity to be gained (L5335) | (deg) |
| γ_M | Relative azimuthal velocity vector angle in missile-target coordinates (L5336) | (deg) |
| $\dot{\gamma}_M$ | Relative azimuthal velocity vector angular rate in missile-target coordinates (L5337) | (deg) |
| γ_R | Output required velocity flight path angle at the missile instantaneous position (L5334) | (deg) |
| γ_T | Target pitch flight path angle (L5728) | (deg) |
| γ_{TO} | Input initial target flight path angle at start of target maneuvering (L0633) | (deg) |
| γ_1 | Pitch flight path angle. Angle between the earth referenced velocity vector and the local tangent plane. Positive away from the earth (L5321) | (deg) |
| $\dot{\gamma}_1$ | Pitch flight path angular rate. Positive up (L5322) | (deg/sec) |
| γ_{1E} | Pitch flight path angle with respect to the ambient air at entry conditions (L5327) | (deg) |
| γ_{1I} | Inertial pitch flight path angle. Angle between the inertial velocity vector and the local tangent plane. Positive away from the earth (L5330) | (deg) |
| γ_{1IE} | Entry conditions inertial pitch flight path angles, if powered flight and the atmospheric end at the time being printed (L5328) | (deg) |
| γ_{1If} | Impact or intercept inertial pitch flight path angle, if powered flight and the atmosphere end at the time being printed (L5332) | (deg) |

γ, Γ

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------------|--|--------------|
| γ_1 (B1) | Pitch flight path angle at the termination of Stage I angle between the earth referenced velocity vector and the local tangent plane. Positive away from the earth (L5903) | (deg) |
| γ_1 (B2) | Pitch flight path angle at the termination of Stage II. Angle between the earth referenced velocity vector and the local tangent plane. Positive away from the earth (L5928) | (deg) |
| γ_1 (B3) | Pitch flight path angle at the termination of Stage III. Angle between the earth referenced velocity vector and the local tangent plane. Positive away from the earth (L5953) | (deg) |
| γ_1 (B4) | Pitch flight path angle at the termination of Stage IV. Angle between the earth referenced velocity vector and the local tangent plane. Positive away from the earth (L5978) | (deg) |
| γ_{1If} (B1) | Impact or intercept inertial pitch flight path angle if the powered flight were to end at the termination of Stage I (L5917) | (deg) |
| γ_{1If} (B2) | Impact or intercept inertial pitch flight path angle if the powered flight were to end at the termination of Stage II (L5942) | (deg) |
| γ_{1If} (B3) | Impact or intercept inertial pitch flight path angle if the powered flight were to end at the termination of Stage III (L5967) | (deg) |
| γ_{1If} (B4) | Impact or intercept inertial pitch flight path angle if the powered flight were to end at the termination of Stage IV (L5992) | (deg) |
| γ_{10} | Input flight path angle at the trajectory start time, $-180^\circ < \gamma_{10} \leq 180^\circ$ (L0011) | (deg) |
| γ_2 | Azimuthal flight path angle. Angle between the hori- zontal projection of the earth reference velocity vector and the local north. Positive clockwise from north (L5323) | (deg) |

γ, Γ

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-----------------------|--|--------------|
| $\dot{\gamma}_2$ | Azimuthal flight path angular rate (L5324) | (deg/sec) |
| γ_{2i} | Inertial azimuth flight path angle. Angle between local north clockwise to the projection of the inertial velocity vector on the local tangent plane (L5331) | (deg) |
| γ_{2ia} | Inertial azimuth flight path angle at apogee (L5326) | (deg) |
| γ_{2ie} | Entry conditions inertial yaw flight path azimuth angle, if powered flight and the atmosphere end at the time being printed (L5329) | (deg) |
| γ_{2if} | Impact or intercept inertial yaw flight path azimuthal angle, if powered flight and the atmosphere end at the time being printed (L5333) | (deg) |
| γ_{20} | Input azimuthal flight path angle at trajectory start time (L0044) | (deg) |
| Γ_d | Ratio of specific heats functional constants used in separated flow thrust equations | (dim) |
| $\dot{\gamma}_\Gamma$ | Target pitch flight path angular rate (L5778) | (deg/sec) |

δ, Δ

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|----------------------------------|--|-------------------------|
| δ_{ave} | Output average TVC deflection angle per control motor for the TVC design stage | (deg) |
| δ_{me} | Input maximum vector angle design limit also output in TVC design duty cycle (L0681) | (deg) |
| δ_{MI} | Azimuth flight path error to intercept. Used in type 10 flight (L5338) | (deg) |
| δ_{MR} | Input roll system fin misalignment angle (Lk403) | (deg) |
| δ_{MP} | Input nozzle misalignment angle in pitch (Lk389) | (deg) |
| δ_{MT} | Seeker yaw look angle (L5351) | (deg) |
| $\dot{\delta}_{MT}$ | Seeker yaw look angular rate (L5352) | (deg/sec) |
| δ_{MY} | Input nozzle misalignment angle in yaw (Lk390) | (deg) |
| δ_p | Pitch thrust deflection angle. Positive up (L5716) | (deg) |
| $\dot{\delta}_p$ | Pitch thrust deflection angular rate positive up (L5713) | (deg/sec) |
| $\ddot{\delta}_p$ | Pitch thrust deflection angular acceleration angle positive up (L5763) | (deg/sec ²) |
| $\bar{\delta}_p$ | Modified pitch thrust deflection angle to include limit cycle and misalignment angle (L5342) | (deg) |
| δ_{Pc} | Pitch plane thrust deflection commands (L5339) | (deg) |
| $\delta_{PO}, \dot{\delta}_{PO}$ | Input per stage initial pitch thrust vector deflection angle and angular rate at the trajectory initiation or stage initiation (Lk420-421) | (deg and deg/sec) |
| δ_{PH} | Pitch nozzle deflection angle at final altitude of maximum wind shear | (deg) |
| δ_{PL} | Nozzle deflection angle at initial altitude of maximum wind shear | (deg) |

δ, Δ

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-----------------------|---|-------------------------|
| $\bar{\delta}_{Pmax}$ | Output maximum magnitude pitch thrust vector deflection angles respectively, per control motor for the TVC design stage | (deg) |
| δ_{Pmax}^i | Maximum pitch deflection outside region of maximum wind shear | (deg) |
| $\dot{\delta}_{Pmax}$ | Output maximum pitch thrust vector deflection angular rate, respectively for the TVC design stage | (deg/sec) |
| δ_{Pq} | Pitch thrust deflection angle at t_{Bj} | (deg) |
| $\bar{\delta}_{Pq}$ | Output modified the TVC design duty cycle points pitch thrust deflection angle at t_{Bj} | (deg) |
| δ_{PW} | Maximum pitch within region of maximum wind shear | (deg) |
| $\bar{\delta}_S$ | Output pitch slew angle for TVC design stage | (deg) |
| δ_S | TVC design stage vehicle slew angle | (deg) |
| $\dot{\delta}_S$ | Output control system design slew rate for TVC design stage | (deg/sec) |
| δ_R | Aerodynamic roll fins deflection angle (L5718) | (deg) |
| $\dot{\delta}_R$ | Aerodynamic roll fins deflection angular rate (L5715) | (deg/sec) |
| δ_{Rc} | Commanded roll control fin deflection angle (L5341) | (deg) |
| δ_y | Yaw thrust deflection angle, positive left (L5717) | (deg) |
| $\dot{\delta}_Y$ | Yaw thrust deflection angular rate, positive left (L5714) | (deg/sec) |
| $\ddot{\delta}_y$ | Yaw thrust deflection angular acceleration angle positive left | (deg/sec ²) |
| $\bar{\delta}_Y$ | Modified yaw thrust deflection angle to include limit cycle and misalignment angles (L5343) | (deg) |
| δ_{Yc} | Yaw plane thrust deflection commands (L5340) | (deg) |

δ, Δ

Symbol

Definition

Units

$\delta_{YO}, \dot{\delta}_{YO}$

Input per stage initial yaw thrust vector deflection angle and angular rate at the trajectory initiation or stage initiation (Lk422-423)

(deg and deg/
sec)

| <u>δ, Δ</u> | | |
|------------------------------------|--|--------------|
| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
| Δ_a | Input hunting procedure (P1) values that "a" should be computed within the isolation or maximization routine (L0083) | (dbi) |
| Δ'_a | Pitch flare-in angle (L5349) | (deg) |
| Δ_{ak} | Pitch flare in constant used in evaluation Δ'_{ak} for restart (L5347) | (deg) |
| Δ'_b | Yaw flare-in angle (L5350) | (deg) |
| Δ_{bk} | Flare-in constant used in evaluating Δ'_{bk} for restart (L5348) | (deg) |
| Δ_{dc} | Input value of number of desired duty cycle points (100 maximum) if input zero, set equal to 50 (L0670) | (dim) |
| Δ_h | Calculated altitude difference of the target and missile (L5435) | (ft) |
| $\dot{\Delta}_h$ | Calculated time rate change of the altitude difference of the target and missile (L5436) | (ft/sec) |
| ΔQ_b | Input stage pitch attitude reaction angular impulse; i. e., added to θ_b at staging (Lk428) | (deg) |
| ΔR_b | Input stage yaw attitude reaction angular impulse; i. e., added to ψ_b at staging (Lk429) | (deg) |
| Δ_s | Calculated earth surface down range difference of the target and missile (L5431) | (ft) |
| $\dot{\Delta}_s$ | Calculated time rate change of the earth surface down range difference of the target and missile (L5432) | (ft/sec) |
| Δ_s_c | Calculated earth surface cross range difference of the target and missile (L5433) | (ft) |
| $\dot{\Delta}_s_c$ | Calculated time rate change of the earth surface cross range difference of the target and missile (L5434) | (ft/sec) |

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-------------------|--|--------------|
| Δt_{cj} | Input computing interval during $t_{cj-1} \leq t \leq t_{cj}$ where $J = 1, 2, \dots, 8$ (L0168, 170, etc) | (sec) |
| Δt_{pj} | Input main printing interval during $t_{p(j-1)} \leq t \leq t_{pj}$ where $J = 1, 2, \dots, 8$ (L0184, 186, etc) | (sec) |
| Δt_{pj} | Input auxiliary printline interval during $t_{p(j-1)} \leq t \leq t_{pj}$ where $j = 1, 2, \dots, 8$ (L0220, 222, etc) | (sec) |
| Δv | Ideal missile velocity resulting from achieved thrust (L5744) | (ft/sec) |
| $\Delta v_{(B1)}$ | Ideal missile velocity for Stage I (L5910) | (ft/sec) |
| $\Delta v_{(B2)}$ | Ideal missile velocity for Stage II (L5935) | (ft/sec) |
| $\Delta v_{(B3)}$ | Ideal missile velocity for Stage III (L5960) | (ft/sec) |
| $\Delta v_{(B4)}$ | Ideal missile velocity for Stage IV (L5985) | (ft/sec) |
| ΔX | Input increments that X is incremented during the hunting procedure (P1) (L0081) | (dbi) |
| Δx_{ij} | Input increment of x_{ij} used in incrementing during hunting procedure (P2), $J = 1, 2, \dots, 7$ (L0093, 102, etc) | (dbi) |
| $\Delta \theta_b$ | Vehicle pitch attitude error angle (L5344) | (deg) |
| $\Delta \phi_b$ | Vehicle roll attitude error angle (L5348) | (deg) |
| $\Delta \psi_b$ | Vehicle yaw attitude error angle (L5345) | (deg) |

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-----------------------|--|--------------|
| ϵ | Total angle of attack roll orientation angle. Angle between total angle of attack plane and yaw axis. Measured counterclockwise (L5353) | (deg) |
| $\bar{\epsilon}$ | No wind total angle of attack roll orientation angle (L5354) | (deg) |
| ϵ_{cj} | Input tolerance on the j-th condition of constraint used in hunt procedure (P2) where $J = 1, 2, \dots, 7$ (L0097, 106, etc) | (dbi) |
| ϵ_d | Input and output nozzle expansion ratio used in the separated flow nozzle thrust equations (Lk013) | (dim) |
| ϵ_m | Input flag to specify model error used in hunt procedure (P2). If $\epsilon_m < 0$, the model will be iterated until an extremal solution has a 95 percent probable model error. If $\epsilon_m = 0$, the extremal solution is obtained without regard to probable model error (L0087) | (dim) |
| ϵ_{MI} | Flight path error to estimated intercept (L5355) | (deg) |
| ϵ_{MT} | Seeker pitch look angle (L5356) | (deg) |
| $\dot{\epsilon}_{MT}$ | Seeker pitch look angular rate (L5357) | (deg/sec) |
| ϵ_s | Main motor nozzle separation expansion ratio used in separated flow equation (L5075) | (dim) |
| ϵ_z | Input value specifying the tolerance of the predicted maximization parameter (z). Used in the hunt procedure (P2) (L0086) | (dbi) |

ζ

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-----------------|--|--------------|
| ζ | Cross range angle. Angle between local vertical and vertical on firing azimuth down range location. Positive if positive is left of firing azimuth (L5358) | (deg) |
| $\dot{\zeta}$ | Cross range angular rate (L5359) | (deg/sec) |
| ζ_c | Input stage pitch control systems damping ratio for the thrust vector deflection second-order transfer function (Lk436) | (dim) |
| ζ_v | Input vehicle controlled damping ratio (Lk438) | (dim) |
| ζ_T | Target azimuthal flight path angle (L5729) | (deg) |
| ζ_{TO} | Input initial target azimuthal flight path angle at start of target maneuvering (L0635) | (deg) |
| ζ_{zj} | Input constant altitude ($T_y = 8$) control damping ratio where $J = 1, 2, \dots$, or 16 (L0315, 322, etc) | (dim) |
| ζ_o | Initial cross range angle | (deg) |
| $\dot{\zeta}_T$ | Target azimuthal path angular rate (L5779) | (deg/sec) |

η

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|--|--------------|
| η | Transformed value of the independent variable x used in hunt procedure (P2) | (dbi) |
| η_{ba} | Acceleration load factor along velocity vector (L5169) | (g's) |
| η_{bn} | Acceleration load factor normal to the velocity vector (L5171) | (g's) |
| η_{bt} | Acceleration load factor transverse to the velocity vector (L5170) | (g's) |
| η_{cn} | Commanded load normal factor | (g's) |
| η_{cj} | Input command normal load factor for constant load factor type of flight where J = 1, 2, ..., or 13 (Ty = 9) (L0313, 320, etc) | (g's) |
| η_{ct} | Commanded load crosswire factor | (g's) |
| η_{ctj} | Input command load factor crosswise to the velocity vector used for constant load factor type of flight where j = 1, 2, ... (Ty = 9) (L0314, 321, etc) | (g's) |
| η_{ln} | Achieved load factor normal to the velocity vector in the commanded local roll coordinates | (g's) |
| η_{lt} | Achieved load factor crosswise to the velocity vector in the command local roll coordinates | (g's) |
| η_{vr} | Input disturbing roll nozzle vortex multiplier. If not input is set to 0.00363 (Lk496) | (ft) |

θ

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|------------------|--|--------------|
| θ_b | Achieved missile Euler angle pitch attitude (L5710) | (deg) |
| $\dot{\theta}_b$ | Achieved vehicle Euler angle pitch rate (L5760) | (deg/sec) |
| θ_{bo} | Input pitch orientation angle at the trajectory start time, $-180^\circ < \theta_{bo} \leq 180^\circ$ (L0034) | (deg) |
| θ_i | Input inertial elevation axis Euler angle relating the i and e_o systems (L0015) | (deg) |
| θ_g | Input generalized coordinate orientation for velocity steering. First rotation angle (about the X_e -axis) of the set θ_g , ψ_g , and ϕ_g (L0047) | (deg) |
| θ_m | Desired missile attitude Euler angle relating the m and i system (L5722) | (deg) |
| $\dot{\theta}_m$ | Desired vehicle pitch Euler angular rate (L5772) | (deg/sec) |

λ

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|----------------------|--|--------------|
| λ_{MT} | Angle of missile to target line projection on horizontal and firing azimuth (L5360) | (deg/sec) |
| $\dot{\lambda}_{MT}$ | Angular rate of missile to target line projection or horizontal and firing azimuth (L5361) | (deg/sec) |
| λ_i | Lagrange multiplier used in the simultaneous hunt (P2) for the i-th constraint function | (dbi) |
| λ_a | Apogee longitude | (deg) |
| λ_d | Nozzle half angle momentum correction coefficient | (dim) |

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|---|--------------|
| μ | Instantaneous vehicle longitude. Value is positive or negative west or east of Greenwich, England, respectively (L5362) | (deg) |
| μ' | Instantaneous vehicle change of longitude from launch longitude. Value is positive east (L5363) | (deg) |
| $\dot{\mu}$ | Vehicle longitude time rate change (L5364) | (deg/sec) |
| μ_a | Vehicle apogee longitude if powered flight and the atmosphere end at the time being printed (L5365) | (deg) |
| μ_f | Missile impact or intercept longitude if powered flight and the atmosphere end at the time being printed (L5366) | (deg) |
| μ_L | Input launcher longitude (L0012) | (deg) |
| μ'_0 | Initial change in longitude from launch longitude | (deg) |

E

Symbol

Definition

Units

E

Ratio of specific heats function constant used in
separated flow thrust equation

(dim)

ρ

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|---|------------------------|
| ρ | Instantaneous vehicle latitude positive north of the equator $-90^\circ \leq \rho \leq 90^\circ$ (L5367) | (deg) |
| $\dot{\rho}$ | Vehicle latitude time rate change (L5368) | (deg/sec) |
| ρ_a | Vehicle apogee latitude if powered flight and the atmosphere end at the time being printed (L5369) | (deg) |
| ρ_f | Missile impact or intercept latitude if powered flight and the atmosphere end at the time being printed (L5370) | (deg) |
| ρ_L | Input launch latitude, $-90^\circ \leq \rho \leq 90^\circ$ (L0017) | (deg) |
| ρ_p | Density of propellant used in internal ballistic evaluation is set to 0.065 if not input (Lk095) | (lb/in. ³) |
| ρ_o | Initial vehicle latitude | (deg) |

σ

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|----------------|---|--------------|
| σ_a | Input code which designates the dependent variable in the hunting procedure (P1) (L0078) | (dim) |
| σ_{Aj} | Input code which designates the integration tolerance parameters where $J = 1, 2, \dots$, or 7 (L0280, 283, etc) | (dbi) |
| σ_{Bj} | Input code which designates the quantities whose values at staging are to be available to the hunting procedure, $j = 1, 2, \dots, 5$ (L0271, 273, etc) | (dim) |
| σ_{BX1} | Values which are designated by input, at staging which are available to the hunting procedure (L5496-500) | (dbi) |
| σ_{BX2} | | |
| σ_{BX3} | | |
| σ_{BX4} | | |
| σ_{BX5} | | |
| σ_c | Input code which designates the quantity that determines the flight region when the orbital elements and impact determination are desired (L0041) | (dim) |
| σ_{Dj} | Input code which designates the quantity that determines when to print a discontinuity where $j = 1, 2, \dots, 8$ (L0252-259) | (dim) |
| σ_f | Standard of vacuum thrust to nominal vacuum thrust at any nominal time point | (dim) |
| σ_{fj} | Input code which designates the quantity that determines when the j -th type of flight ends where $j = 1, 2, \dots, 16$ (L0311, 318, etc) | (dim) |
| σ_{Fyj} | Input code which designates the quantity that determines when the j -th type of TMC ends (L0801, 811, etc) | (dim) |
| σ_{Gj} | Input code which designates attitude control system gain zone limits ($j = 1, 2$, or 3) (Lk457, 466) | (dim) |

σ

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------------|--|--------------|
| σ_{g1k} | Input code which designates the start of the acquisition zone for evaluation of the steering equations coefficients for the k-th stage, $k = 1, 2, 3$, or 4 (Lk397) | (dbi) |
| σ_{g2k} | Input quantity which designates the end of the acquisition zone for evaluation of the steering equation coefficient for the k-th stage, $k = 1, 2, 3$, or 4 (Lk399) | (dbi) |
| σ_{It} | Input standard deviation of the ratio of total impulse to nominal total impulse for the k-th stage (Lk383) | (dim) |
| σ_{Jj} | Input code which designates the quantity that determines when the W_{JT} weight is to be jettisoned where $j = 1, 2, \dots$, or 8 (L0050, 53, etc) | (dim) |
| σ_{MI} | Local flight path angle to estimated target, intercept (L5373) | (deg) |
| σ_{mj} | Input code which designates the quantity whose maximum value is to be printed following each stage time where $j = 1, 2, \dots, 5$ (L0261, 263, etc) | (dbi) |
| σ_{Mj} | Input code which designates the quantity that determines when the j-th mode type ends where $j = 1, 2, \dots, 10$ (L0601, 609, etc) | (dim) |
| σ_{MT} | Angle of missile to target line and local horizontal (L5371) | (deg) |
| $\dot{\sigma}_{MT}$ | Angular rate of missile to target line and local horizontal (L5372) | (deg/sec) |
| σ_{mx1} | Values which are designated by input, as quantity whose maximum value is to be printed following each stage time (L5491, 495) | (dbi) |
| σ_{mx2} | | |
| σ_{mx3} | | |
| σ_{mx4} | | |
| σ_{mx5} | | |

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|----------------|---|--------------|
| σ_{pj} | Input code designates the quantity to be printed in printline Z where $j = 1, 2, \dots, 8$ (L0209-219) | (sec) |
| σ_{Sk} | Input code which designates the quantity that determines when a stage is terminated where $k = 1, 2, 3, 4$ (Lk000) | (dim) |
| σ_{tb} | Input standard deviation of the ratio of web burntime to nominal burntime for the k-th stage (Lk384) | (dim) |
| σ_{tj} | Input code which designates the quantity that determines when to print a special time where $j = 1, 2, \dots, 8$ (L0236, 238, etc) | (dim) |
| σ_{Tto} | Input code designating start of target maneuvering (L0630) | (dim) |
| σ_X | Input code which designates the independent variable in the hunting procedure (P1) (L0077) | (dim) |
| σ_{xj} | Input code which designates the independent variables used in hunting procedure (P2) where $j = 1, 2, \dots, 7$ (L0091, 100, etc) | (dim) |
| σ_{yj} | Input code which designates the dependent variables used in hunting procedure (P2) where $j = 1, 2, \dots, 7$ (L0094, 103, etc) | (dim) |
| σ_z | Input code. The σ_z identifies the dependent variable being maximized or minimized. Used in hunt procedure (P2). If $\sigma_z < 0$, the values of x_1, x_2, \dots, x_{in} (L0085) | (dim) |

| <u>T</u> | | |
|-----------------|---|--------------|
| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
| τ_c | Input stage pitch and yaw control system's time constant for the thrust vector deflection first order transfer function (Lk435) | (sec) |
| τ_{cf} | First order lead constant which will be set proportional to equivalent first order lag of controllable motor used in the TMC command logic | (sec) |
| τ_{fk} | Input pitch flare-in time constant for k-th stage used in velocity steering type cf flight ($T_y = 4$) (Lk396) | (sec) |
| τ_{Fyj} | Input control system time constant of the j-th type TMC (L0805, 815, etc) | (sec) |
| τ_{HGj} | Input pitch and yaw flare-in factor used in the Homing Guidance ($T_y = 11$) (L0314, 321, etc) | (sec) |
| τ_{IGj} | Input pitch and yaw flare-in factor used in the intercept guidance ($T_y = 10$) (L0314, 321, etc) | (sec) |
| τ_{MIj} | Input guidance associated first order intercept guidance controller time constant used in type 10 flight where $j = 1, 2, \dots, \text{or } 13$ (L0313, 320, etc) | (sec) |
| τ_{RI} | Input stage roll control system time constant, for the first order transfer (Lk639, 649, 659) | (sec) |
| τ_w | Web fraction used in internal ballistic evaluation is set to 0.8 if not input (Lk096) | (dim) |
| τ_{yk} | Input time constant in the nontarget dependent yaw steering equation for the k-th stage (Lk402) | (sec) |
| $\tau_{\eta j}$ | Input flare-in time constant for constant load factor type of flight ($T_y = 9$) (L0315, 322, etc) | (g's) |

| <u>Symbol</u> | <u>T</u> <u>Definition</u> | <u>Units</u> |
|---------------|---|--------------|
| T_{MI} | Azimuthal angle to target intercept (L5374) | (deg) |

ϕ, ψ

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|----------------|--|--------------|
| ϕ | Instantaneous down range angle. Angle between the launch vertical and the local vertical on the down range azimuth point. Positive as shown in Figure 1.1, $-\infty < \phi < \infty$ (L5375) | (deg) |
| $\dot{\phi}$ | Instantaneous range angular rate. Positive down range (L5376) | (deg/sec) |
| ϕ_a | Glide range angle to the apogee vertical (L5378) | (deg) |
| ϕ_{a4} | Glide range angle to the apogee vertical (L5114) | (deg) |
| ϕ_b | Achieved missile Euler angle roll attitude (L5712) | (deg) |
| $\dot{\phi}_b$ | Achieved vehicle Euler angle roll rate (L5762) | (deg/sec) |
| ϕ_{bo} | Input roll orientation angle at the trajectory start time $-180^\circ < \phi_{bo} \leq 180^\circ$ (L0036) | (deg) |
| ϕ_f | Glide range angle to glide phase termination vertical used in Keplerian impact predictions (L5381) | (deg) |
| ϕ_g | Input generalized coordinate orientation angle. Final rotation angle (about the X_g axis) of the set θ_g, ψ_g , and ϕ_g | (deg) |
| ϕ_i | Input inertial meridional axis Euler angle relating the i and e_o systems (L0016) | (deg) |
| ϕ_m | Desired missile attitude Euler angle relating the m and i systems (L5724). | (deg) |
| $\dot{\phi}_m$ | Desired vehicle roll Euler angular rate (L5774) | (deg/sec) |
| ϕ_{mo} | Input initial commanded roll attitude (L0030) | (deg) |
| ϕ_{Ri} | Input bank angle location of the i -th raceway where $i = 1, 2$. As seen from the rear of the vehicle, a positive angle is measured clockwise from the Z_k axis direction (Lk669, 672) | (deg) |

| <u>Symbol</u> | <u>ϕ, ψ</u> <u>Definition</u> | <u>Units</u> |
|---------------|--|--------------|
| ϕ_s | Instantaneous slant range angle. Angle between the launch vertical and the local vertical (L5379) | (deg) |
| ϕ_v | Input bivariant consideration axis for the k-th stage (Lk385) | (deg) |
| ϕ_o | Initial down range angle | (deg) |
| ϕ | Local bank angle (L5380) | (deg) |
| ϕ_c | Commanded bank angle (L5377) | (deg) |
| ϕ_{cj} | Input command roll attitude used in the constant angle of attack and angle of side slip type of flight (Ty = 7) or the constant load factor type of flight where j = 1, 2, ..., or 13 (Ty = 9) (L0315, 322, etc) | (deg) |

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|----------------|--|---------------|
| ψ | Vehicle azimuth in the launch horizontal plane (L5382) | (deg) |
| ψ_b | Achieved missile Euler angle yaw attitude (L5711) | (deg) |
| $\dot{\psi}_b$ | Achieved vehicle Euler angle yaw rate (L5761) | (deg/sec) |
| ψ_{bo} | Input yaw orientation angle at the trajectory start time $-180^\circ < \psi_{bo} \leq 180^\circ$ (L0035) | (deg) |
| ψ_g | Input generalized coordinate orientation angle. Second rotation angle (about the resulting Z axis after rotating through θ_g , ψ_g , and ϕ_g) (L0046) | (deg) |
| ψ_i | Input flight plane azimuth angle. Angle measured north to the flight plane, $-180^\circ \leq \psi \leq 180^\circ$ (L0014) | (ft) |
| ψ_m | Desired missile attitude Euler angle relating the m and i systems (L5723) | (deg) |
| $\dot{\psi}_m$ | Desired vehicle yaw Euler angular rate (L5773) | (deg/sec) |
| ψ_{mo} | Input initial commanded yaw attitude (L0029) | (deg) |
| ψ_w | Instantaneous wind azimuth angles, measured in a plane parallel to the local tangent plane where $j = 1, 2, \dots, 30$. Angle measured clockwise from north to the direction from which the wind is coming (L5383) | (deg) |
| ψ_{wj} | Input instantaneous (with altitude h) wind azimuth angles, measured in a plane parallel to the local tangent plane where $j = 1, 2, \dots, 30$. Angle measured clockwise from north to the direction from which the wind is coming. (L0417, 415, etc) | (deg and dbi) |

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|--|--------------|
| ω | Input magnitude of the earth's angular velocity. If input greater than 0.5, set equal to 7.29211 E-5 (L0027) | (rad/sec) |
| ω_c | Input stage pitch control systems forcing frequency for the thrust vector deflection second-order transfer function (Lk437) | (rad/sec) |
| ω_c | Output slew frequency used in the TVC design stage slew rate calculations | (rad/sec) |
| ω_L | Input frequency of limit cycle for the k-th stage | (rad/sec) |
| ω_p | Pintle control frequency (L5083) | (rad/sec) |
| ω_s | Input slew frequency used in the TVC design stage slew rate calculations (L0674) | (rad/sec) |
| ω_v | Input vehicle controlled frequency for the k-th stage (Lk439) | (rad/sec) |
| ω_{zj} | Input attitude control frequency used in constant attitude type of flight where $j = 1, 2, \dots, 16$ ($Ty = 8$) (L0314, 321, etc) | (rad/sec) |
| Ω_d | Ratio of specific heats functional constant. Used in separated flow thrust equations | (dim) |

B. EQUATIONS OF MOTION

The equations and logic given in this section establish the trajectory program which simulates missile flight in three dimensions with an additional three degrees of freedom possible, i.e., the vehicle can pitch, yaw, and roll about its center of gravity. A spherical rotating earth mode is utilized for missile location; gravitational forces from an oblate earth can be included.

Differential equations requiring numerical integration are as follows:

1. Linear momenta equations
2. Angular momenta equations
3. Desired missile attitude angular velocities
4. Achieved missile attitude angular velocities
5. Thrust vectoring equations

To yield an essentially point mass solution, items 2, 4, and 5 are ignored if $M_y = 1$ or 4.

1. Linear Momenta Equations

The linear momenta equations which yield the three-dimensional missile acceleration components are computed from the real forces acting on the missile and the accelerations arising from the earth rotation. The equations are:

$$\begin{Bmatrix} \ddot{x}_{ee} \\ \ddot{y}_{ee} \\ \ddot{z}_{ee} \end{Bmatrix} = [D] \begin{Bmatrix} a_{xb} \bar{g}_e \\ a_{yb} \bar{g}_e \\ a_{zb} \bar{g}_e \end{Bmatrix} - \begin{Bmatrix} 2\omega \dot{y}_{ee} \sin \rho_L \\ -2\omega (\dot{x}_{ee} \sin \rho_L + \dot{z}_{ee} \cos \rho_L) \\ 2\omega \dot{y}_{ee} \cos \rho_L \end{Bmatrix} - \begin{Bmatrix} g_{xe} \\ g_{ye} \\ g_{ze} \end{Bmatrix}$$

The above parameters are defined as follows:

\ddot{X}_{ee} and \dot{X}_{ee} are the components of missile acceleration and velocity in a right handed Cartesian coordinate system whose origin is fixed at sea level at the input launch latitude, ρ_L . The X_e axis is positive north, Y_e -axis positive east, and Z_e , the vertical axis, is positive down.

a. Initial Condition

The initial condition position and velocity vector are as follows:

Down Range Angle

$$\phi_0 = (180/\pi) S_0/r_e$$

Cross Range Angle

$$\zeta_0 = (180/\pi) S_{co}/r_e$$

Radius From Center of Earth

$$r_{co} = h_0 + r_e$$

Launch Centered Coordinates

$$X_{ee0} = r_{co} (\cos \psi_i \cos \zeta_0 \sin \phi_0 - \sin \psi_i \sin \zeta_0)$$

$$Y_{ee0} = r_{co} (\sin \psi_i \cos \zeta_0 \sin \phi_0 + \cos \psi_i \sin \zeta_0)$$

$$Z_{ee0} = r_e - r_{co} \cos \zeta_0 \cos \phi_0$$

Initial Earth Geocentric Coordinates

$$X_{cco} = X_{ee0} \cos \rho_L - Z_{ee0} \sin \rho_L + r_e \sin \rho_L$$

$$Y_{cco} = Y_{ee0}$$

$$Z_{cco} = X_{ee0} \sin \rho_L + Z_{ee0} \cos \rho_L - r_e \cos \rho_L$$

Initial Latitude and Differential Lognitude

$$\sin \rho_0 = X_{cco}/r_{co}$$

$$\cos \rho_0 = (Y_{cco}^2 + Z_{cco}^2)^{1/2}/r_{co}$$

$$\sin \mu_0' = Y_{cco}/(Y_{cc}^2 + Z_{cc}^2)^{1/2}$$

$$\cos \mu_0' = -Z_{cc}/(Y_{cc}^2 + Z_{cc}^2)^{1/2}$$

Initial Launch Centered Velocity Coordinates

$$\begin{bmatrix} \dot{X}_{eeo} \\ \dot{Y}_{eeo} \\ \dot{Z}_{eeo} \end{bmatrix} = \begin{bmatrix} \cos \rho_L & 0 & \sin \rho_L \\ 0 & 1 & 0 \\ -\sin \rho_L & 0 & \cos \rho_L \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \mu_0' & -\sin \mu_0' \\ 0 & \sin \mu_0' & \cos \mu_0' \end{bmatrix}$$

$$\times \begin{bmatrix} \cos \rho_0 & 0 & -\sin \rho_0 \\ 0 & 1 & 0 \\ \sin \rho_0 & 0 & \cos \rho_0 \end{bmatrix} \begin{bmatrix} V_{eo} \cos \gamma_{10} \cos \gamma_{20} \\ V_{eo} \cos \gamma_{10} \sin \gamma_{20} \\ -V_e \sin \gamma_{10} \end{bmatrix}$$

b. D Matrix

The matrix [D], which rotates components from the b system to the e system, is computed from:

$$[D] = [A_{ec}][A_I][A_b]$$

where ω is input, $[A_r]$ rotates components from the b system to the i system, $[A_i]$ from the i system to the e_o system, and $[A_{eo}]$ from the eo system to the e system. The coordinate axes are discussed in Section A.2.c and shown in Figure 17. These rotation matrices are defined as follows:

$$[A_{eo}] = \begin{bmatrix} \cos \rho_L & 0 & \sin \rho_L \\ 0 & 1 & 0 \\ -\sin \rho_L & 0 & \cos \rho_L \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \omega t & \sin \omega t \\ 0 & -\sin \omega t & \cos \omega t \end{bmatrix} \begin{bmatrix} \cos \rho_L & 0 & -\sin \rho_L \\ 0 & 1 & 0 \\ \sin \rho_L & 0 & \cos \rho_L \end{bmatrix}$$

$$[A_i] = \begin{bmatrix} \cos \psi_i & -\sin \psi_i & 0 \\ \sin \psi_i & \cos \psi_i & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \cos \theta_i & 0 & \sin \theta_i \\ 0 & 1 & 0 \\ -\sin \theta_i & 0 & \cos \theta_i \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \phi_i & -\sin \phi_i \\ 0 & \sin \phi_i & \cos \phi_i \end{bmatrix}$$

with

$$[A_m] = \begin{bmatrix} \cos \theta_m & 0 & \sin \theta_m \\ 0 & 1 & 0 \\ -\sin \theta_m & 0 & \cos \theta_m \end{bmatrix} \begin{bmatrix} \cos \psi_m & -\sin \psi_m & 0 \\ \sin \psi_m & \cos \psi_m & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \phi_m & -\sin \phi_m \\ 0 & \sin \phi_m & \cos \phi_m \end{bmatrix}$$

$$[A_b] = \begin{bmatrix} \cos \theta_b & 0 & \sin \theta_b \\ 0 & 1 & 0 \\ -\sin \theta_b & 0 & \cos \theta_b \end{bmatrix} \begin{bmatrix} \cos \psi_b & -\sin \psi_b & 0 \\ \sin \psi_b & \cos \psi_b & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \phi_b & -\sin \phi_b \\ 0 & \sin \phi_b & \cos \phi_b \end{bmatrix}$$

where t is the instantaneous time, θ_i , ψ_i , ϕ_i the input Euler angles defining the relation between i and e_o systems, and the subscript m and b Euler angles are computed from the integration of their rate equations. The angles are shown in Figure 17 and Figure 18.

c. Inertial Acceleration Components

The components of acceleration arising from the thrust and aerodynamic forces acting on the missile are:

$$a_{xb} = \left[F_x - C - C_{\delta z} - D_{rl} \operatorname{sgn}(\dot{x}_{bb}) \right] / W$$

$$a_{yb} = (F_y + F_{JDy} + F_{TDy} + N_{Py} - N_Y + N_{\delta Y}) / W$$

$$a_{zb} = (F_z + F_{JDz} + F_{TDz} + N_{Pz} - N_Z + N_{\delta Z}) / W$$

where $F_{x,y,z}$ are the components of missile thrust, main and/or complementary; F_{JDy} and F_{JDz} are the jet damping forces in yaw and pitch respectively; N_{Py} and N_{Pz} are the aerodynamic damping forces in yaw and pitch respectively; F_{TDy} and F_{TDz} are the movable nozzle tail-wag-dog force in yaw and pitch respectively; and C , N_Y and N_Z are the aerodynamic force components. $N_{\delta Y}$ and $N_{\delta Z}$ are the control fins normal force in yaw and pitch respectively; and $C_{\delta z}$ is the control fin axial force. D_{rl} is the input rail drag. The mass conversion gravity value, \bar{g}_e , is input.

The second and third terms of the linear momenta equations result from Coriolis and gravitational accelerations.

Some of these forces are depicted on Figures 19 and 20.

d. Gravity

The gravitational force is specified by the two components shown in Figure 24; one directed down from the missile towards the earth center and the other perpendicular to the preceding component, directed towards the equatorial plane. Both components are functions of vehicle geocentric latitude and radial distances and include the accelerations due to mass attraction and centrifugal force.

The local components of gravity are:

$$g_{X1} = -(2r_e^4 g_e J/r_c^4 + \omega^2 r_c) \cos \rho \sin \rho$$

$$g_{Y1} = 0$$

$$g_{Z1} = r_e^2 g_e [1 - J r_c^2 (3 \sin^2 \rho - 1)/r_c^2 - \omega^2 r_c \cos^2 \rho]$$

where r_e , g_e , J , and ω are input and r_c and ρ are the instantaneous missile earth center distance and latitude, respectively.

The components in the e system are

$$\vec{g}_e = [A_1] \vec{g}_1$$

where the matrix $[A_1]$ is defined in Section F.2.b.

The energy per unit mass is:

$$E/m = g_e r_c - g_e r_e^2/r_c + v_1^2/2$$

2. Angular Momenta Equations

The angular momenta equations which yield the angular acceleration components about the vehicle center of gravity are defined as follows:

$$\begin{bmatrix} I_{XX} & -I_{XY} & -I_{XZ} \\ -I_{XZ} & I_{YY} & I_{YZ} \\ -I_{XZ} & -I_{YZ} & I_{ZZ} \end{bmatrix} \begin{Bmatrix} \dot{P}_b \\ \dot{Q}_b \\ \dot{R}_b \end{Bmatrix} + \begin{bmatrix} \dot{I}_{XX} & -\dot{I}_{XY} & -\dot{I}_{XZ} \\ -\dot{I}_{XY} & \dot{I}_{YY} & -\dot{I}_{YZ} \\ -\dot{I}_{XZ} & -\dot{I}_{YZ} & \dot{I}_{ZZ} \end{bmatrix} \begin{Bmatrix} P_b \\ Q_b \\ R_b \end{Bmatrix} \\
 + \begin{bmatrix} C & -R_b & Q_b \\ R_b & 0 & -P_b \\ -Q_b & P_b & 0 \end{bmatrix} \begin{bmatrix} I_{XX} & -I_{XY} & -I_{XZ} \\ -I_{XY} & I_{YY} & -I_{YZ} \\ -I_{XZ} & -I_{YZ} & I_{ZZ} \end{bmatrix} \begin{Bmatrix} P_b \\ Q_b \\ R_b \end{Bmatrix} = \begin{Bmatrix} M_{IP} \\ M_{IQ} \\ M_{IR} \end{Bmatrix}$$

where P_b , Q_b and R_b are the roll, pitch and yaw turning rates about the missile center of gravity (Figure 21), I_{XX} , I_{YY} and I_{ZZ} are the roll, pitch and yaw moments of inertia respectively; I_{XY} , I_{XZ} , and I_{YZ} are the products of inertia; and M_{IP} , M_{IQ} and M_{IR} are the roll, pitch, and yaw unbalance moments respectively.

a. Initial Conditions, Angles, and Angular Rates

Initial values of θ_b , ψ_b , and ϕ_b , at the trajectory start time, t_0 , are obtained from input and thereafter, at the initiation of the mode are equated to the values existing at the end of the previous mode segment. At staging, the input stage attitude reaction angular impulse, ΔQ_b is added to Q_b and ΔR_b is added to R_b .

b. Angular Moments

Angular moments are defined as follows.

Perturbing Pitching Moments

$$M_{DQ} = M_{NQ} + M_{FOQ} + M_{TDQ} + M_{JDQ}$$

where M_{NQ} is the aerodynamic pitching moment, M_{FOQ} is the thrust offset pitching moment, M_{TDQ} is the movable nozzle tail-wag-dog pitching moment, and M_{JDQ} is the jet damping pitching moment.

Controlling Pitching Moments

$$M_{CQ} = M_{FCQ} + M_{EQ}$$

where M_{FCQ} is the thrust vector control pitching moment and M_{EQ} is the movable pitch control fin moment.

Unbalance Pitching Moment

$$M_{IQ} = M_{DQ} + M_{CQ}$$

Perturbing Yaw Moments

$$M_{DR} = M_{NR} + M_{FOR} + M_{TDR} + M_{JDR}$$

where M_{NR} is the aerodynamic yawing moment, M_{FOR} is the thrust offset yawing moment, M_{TDR} is the movable nozzle tail-wag-dog yawing moment, and M_{JDR} is the jet damping yawing moment.

Controlling Yawing Moment

$$M_{CR} = M_{FCR} + M_{OR}$$

where M_{FCR} is the thrust vector control yawing moment and M_{OR} is the movable yaw control fin moment.

Unbalance Yawing Moment

$$M_{IR} = M_{DR} + M_{CR}$$

Perturbing Roll Moments

$$M_{DP} = M_{NP} + M_{FOP} + M_{FVP} + M_{RAP}$$

where M_{NP} is the aerodynamic normal force offset rolling moment, M_{FOP} is the thrust offset rolling moment, M_{FVP} is the thrust vortex rolling moment, and M_{RAP} the raceway aerodynamic rolling moment.

Controlling Rolling Moment

$$M_{CP} = M_{FCP} + M_{OR}$$

where M_{FCP} is the auxiliary roll control rolling moment and M_{OR} is the aerodynamic fin rolling control moment.

Unbalance Rolling Moment

$$M_{IP} = M_{DP} + M_{CP}$$

C. CONTROL TABLES

Three different control tables regulate the type of trajectory simulation. The mode control table stipulates the degrees of freedom to be simulated, the attitude control table dictates the type of flight, and the thrust modulation control table specifies the thrust control law.

1. Mode Control Table

The mode table controls the degree of sophistication that is obtained in the simulation of missile flight. Options such as rigid body with and without thrust vector control are controlled by the mode table. The desired option or mode is determined by the type of mode input M_y .

If the input σ_{M1} is zero, all of the logic given below is ignored and only the Mode 1 option of a rigid body without controls is applicable throughout the run.

The following logic applies to the mode regions:

Inputting a maximum of ten mode regions per trajectory is possible. Let σ_{Mj} ($j = 1, 2, \dots, 10$) be the achieved value of a parameter designated by code input and let K_{Mj} be the input of the parameter; then the j -th mode region will apply until $\sigma_{Mj} = K_{Mj}$, then mode is switched to next mode type.

The time when equality in the above occurs will be determined and is defined as t_{Mj} . The K_{Mj} criteria are checked monotonically with respect to the j index. The trajectory is terminated if the final t_{Mj} is reached. The applicable region at the beginning of a trajectory run is determined from

the region start flag, M'_{yj} , as follows:

1. The j -th ($j = 1, 2, \dots, 10$) region applies if
 $M'_{yj} = j \neq 0$
2. If $M'_{yj} = 0$, the first margin applies.

At the initiation of Mode 4, the initial thrust vector angles and rates are obtained from input unless they are not input; then, they are equated to the values at the end of the previous mode region.

The modes have the following meaning:

- a. Point mass simulation ($M_y = 4$)

Mode 4 simulates in three dimensions the vehicle motion as a rigid body without controls (point mass).

- b. Rigid body simulation ($M_y = 5$)

Mode 5 simulates in three dimensions the vehicle motion as a rigid body with controls.

The trajectory will be terminated with an error message and dump if any mode other than 4 or 5 is encountered.

2. Flight Control Table

Desired missile attitude (the relation between the m and i systems) as shown in Figure 18 will be computed by one of the many types of flight methods given below. The m system is the basic coordinates that the autopilot controls. The command m system is calculated for desired angles of attack, angle of sideslip and back angle for certain types of flight. The type of attitude control desired will be determined by the "type of flight" input T_y according to the following logic:

If $T_y = 1$

programmed flight is desired. Missile attitude is determined from the input turning rates.

If $T_y = 2$

stipulated angle of attack and angle of sideslip for a given back angle is desired. Commanded pitch, yaw, and roll attitudes are determined from the commanded relative attitude from achieved earth reference velocity vector.

If $T_y = 4$

nontarget dependent guided flight is desired. Missile attitude is determined from velocity steering equations.

If $T_y = 6$

rail launch dynamic is desired. Missile attitude is fixed in pitch and yaw but the roll attitude is allowed to be commanded from input roll rate.

If $T_y = 8$

constant attitude is specified. Missile attitude will be controlled from a command law specifying angle of attack and angle of side slip. Roll attitude will be specified from command back angle.

If $T_y = 9$

constant normal load factor flight is desired. Missile attitude will be controlled from command law specifying angle of attack, and angle of side slip. Roll attitude will be specified from command back angle.

If $T_y = 10$

intercept guidance flight is desired. Missile attitude is commanded so as to fly the missile on a collision course to intersect with the input moving target coordinates.

If $T_y = 11$

Homing Guidance flight is desired. Missile attitude is calculated to home on a target by so called proportional navigational steering.

The following logic applies to all types of flight:

A maximum of 13 types of flight per trajectory can be input. Let σ_{fj} ($j = 1, 2, \dots, 13$) be the achieved value of a parameter designated by code input and let K_{fj} be the input value of the parameter; then, the j -th type of flight will apply for as long as σ_{fj} does not equal K_{fj} .

An error will occur if σ_{fj} and K_{fj} are equal at the beginning of the j = the type of flight.

The j-th type of flight will end and the trajectory will be computed when equality occurs. Criterion for ending the (j+1)-type of flight is not checked until the j-th type of flight ends. Once the j-th type of flight ends, it cannot be re-entered during the trajectory.

a. Programmed Flight ($T_y = 1$)

When $T_y = 1$ during the j-th type of flight, the pitch, yaw and roll turning rates are obtained from input and the desired vehicle attitude is determined from:

$$\begin{aligned}\dot{\theta}_m &= (Q_{mj} \cos \phi_m - R_{mj} \sin \phi_m) / \cos \psi_m \\ \dot{\phi}_m &= Q_{mj} \sin \phi_m + R_{mj} \cos \phi_m \\ \dot{\psi}_m &= P_{mj} - \dot{\theta}_m \sin \psi_m\end{aligned}$$

where Q_{mj} , R_{mj} , and P_{mj} are the input turning rates in the attitude control table whose positive directions are shown in Figure 19.

The initial values of θ_m , ϕ_m , and ψ_m are obtained from input if $t = t_0$, or from the last computed values from the previous type of flight.

b. Constant Angle of Attack and Angle of Side Slip ($T_y = 2$)

When $T_y = 2$ during the j -th type of flight, the desired vehicle attitude is determined from:

$$\theta_m = \arctan [(-A_{m31})/(A_{m11})] \quad -180^\circ < \theta_m \leq 180^\circ$$

$$\psi_m = \arcsin [A_{m21}] \quad -90^\circ \leq \psi_m \leq 90^\circ$$

$$\phi_m = \arctan [(-A_{m23})/(A_{m22})] \quad -180^\circ < \phi_m \leq 180^\circ$$

where

$$[A_m] = [A_i]^{-1} [A_{eo}]^{-1} [A_1] [A_{\gamma_2}]^{-1} [A_{\gamma_1}]^{-1} [A_c]^{-1}$$

where

$$[A_c] = \begin{bmatrix} \cos \alpha_c & 0 & -\sin \alpha_c \\ 0 & 1 & 0 \\ \sin \alpha_c & 0 & \cos \alpha_c \end{bmatrix} \begin{bmatrix} \cos \beta'_c & -\sin \beta'_c & 0 \\ \sin \beta'_c & \cos \beta'_c & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \varphi_c & \sin \varphi_c \\ 0 & -\sin \varphi_c & \cos \varphi_c \end{bmatrix}$$

where

$$\beta_c' = \arctan [(\tan \beta_c) / (\sec \alpha_c)]$$

The values of α_c , β_c and φ_c are input in the flight control table in the Q_m , R_m , and P_m columns.

$$\begin{aligned} [\dot{A}_m]^{-1} = & [A_c] \{ [\dot{A}_{\gamma_1}] \quad [\dot{A}_{\gamma_2}] \quad [A_1]^{-1} \quad [\dot{A}_{eo}] \\ & + [\dot{A}_{\gamma_1}] \quad [\dot{A}_{\gamma_2}] \quad [A_1]^{-1} \quad [\dot{A}_{eo}] \\ & + [\dot{A}_{\gamma_1}] \quad [\dot{A}_{\gamma_2}] \quad [\dot{A}_1]^{-1} \quad [\dot{A}_{eo}] \\ & + [\dot{A}_{\gamma_1}] \quad [\dot{A}_{\gamma_2}] \quad [A_1]^{-1} \quad [\dot{A}_{eo}] \} [A_1] \end{aligned}$$

$$[\dot{A}_{eo}] = \omega \begin{bmatrix} 0 & -\sin \rho_L & 0 \\ \sin \rho_L & 0 & \cos \rho_L \\ 0 & -\cos \rho_L & 0 \end{bmatrix} [A_{eo}]$$

$$[A_E] = [\dot{A}_m]^{-1} [A_m]$$

$$P_m = A_{E23}$$

$$Q_m = A_{E31}$$

$$R_m = A_{E11}$$

and $\dot{\theta}_m$, $\dot{\psi}_m$, and $\dot{\phi}_m$ are determined as in $T_y = 1$.

c. Pitch Steering (Ty=4)

When Ty=4 during the j-th segment of flight, the vehicle attitude and rate are obtained from instantaneous missile position and velocity components as follows:

$$\theta_m = (180/\pi)[a_{1k} \dot{z}_{gg} + a_{0k} + b_{1k} \dot{x}_{gg} + b_{2k} \dot{x}_{gg}^2 + b_{3k} \dot{x}_{gg}^3 + \Delta_{ak}]$$

$$\dot{\theta}_m = (180/\pi)[a_{1k} \ddot{z}_{gg} + b_{1k} \ddot{x}_{gg} + 2b_{2k} \dot{x}_{gg} \ddot{x}_{gg} + 3b_{3k} \dot{x}_{gg}^2 \ddot{x}_{gg} + \dot{\Delta}_{ak}]$$

The constants a_{1k} , a_{0k} , b_{1k} , b_{2k} , b_{3k} ($k = 1, 2, 3$, or 4) are input per stage, computed under acquisition of coefficients for steering equation logic delineates in section L.3.a, or obtained from previous run if $\sigma_{gk} < 0$. Also,

$$\Delta_{ak} = \Delta'_{ak} \exp[(t_{Bf} - t)/\tau_{fk}]$$

$$\dot{\Delta}_{ak} = -(\Delta_{bk}/\tau_{fk}) \exp[(t_{Bf} - t)/\tau_{fk}]$$

$$\Delta'_{ak} = [(\pi/180)\theta_{mf} - a_{1k}\dot{z}_{gf} - a_{0k} - b_{1k}\dot{x}_{gf} - b_{2k}\dot{x}_{gf}^2 - b_{3k}\dot{x}_{gf}^3]$$

where values of the vehicle attitude angle and velocity components with subscript 'f' are determined at the beginning of this segment or at staging, whichever is the last occurring event, t is the time, t_{Bf} is the value of time when Ty=4 flight begins or is zero at staging, and τ_{fk} is the input pitch flare-in time constant for the k-th stage.

(1) Commanded Yaw Attitude

$$\dot{\psi}_m = - (180/\pi) K_{yk} [\tau_{yk} \dot{Y}_{gg} + Y_{gg}]$$

$$\ddot{\psi}_m = - (180/\pi) K_{yk} [\tau_{yk} \ddot{Y}_{gg} + \dot{Y}_{gg}]$$

(2) Command Roll Attitude

$$\phi_m = \dot{\phi}_m = 0$$

d. Rail Launch ($T_y = 6$)

When $T_y = 6$ during the j -th segment of flight, the vehicle flight path will simulate flying down a launcher rail or tube.

The linear momenta equations are set as

$$\begin{bmatrix} \ddot{X}_{ee} \\ \ddot{Y}_{ee} \\ \ddot{Z}_{ee} \end{bmatrix} = [D] \begin{bmatrix} A_{ax} \\ 0 \\ 0 \end{bmatrix}$$

where

$$A_{ax} = \text{MAX} \left[\begin{matrix} 0 \\ a_{xo} \bar{g}_e - 2\omega \dot{Y}_{ee} \sin \rho_L - g_{xe} \end{matrix} \right]$$

where the quantities are delineated in section B.1.

set

$$\theta_b = \theta_m$$

$$\psi_b = \psi_m$$

$$\begin{bmatrix} P_m \\ Q_m \\ R_m \end{bmatrix} = [D] \begin{bmatrix} * \\ 0 \\ 0 \end{bmatrix}$$

$$\dot{\phi}_m = \frac{(Q_m \cos \phi_m - R_m \sin \phi_m)}{\cos \psi_m}$$

$$\dot{\psi}_m = Q_m \sin \phi_m + R_m \cos \phi_m$$

$$\dot{\phi}_m = P_m - \dot{\theta}_m \sin \psi_m$$

The distance traveled along the rail is

$$l_{lr} = [(X_{ee} - X_{ee}^*)^2 + (Y_{ee} - Y_{ee}^*)^2 + (Z_{ee} - Z_{ee}^*)^2]^{\frac{1}{2}}$$

where l_{lr} is assigned a "p" number 5113 and

$$X_{ee}^* = X_{eeo} + \dot{X}_{eeo}(t - t_o)$$

$$Y_{ee}^* = Y_{eeo} + \dot{Y}_{eeo} (t - t_o)$$

$$Z_{ee}^* = Z_{eeo} + \dot{Z}_{eeo} (t - t_o)$$

where X_{eeo} , Y_{eeo} , Z_{eeo} , and t_o are the initial values of X_{ee} , Y_{ee} , Z_{ee} , and t at the beginning of the segment of flight.

e. Constant Altitude ($T_y = 8$)

The constant altitude type of flight will command the vehicle so as to fly the missile to a specified altitude and then maintain that altitude. The directed flight path azimuth will be down the generalized coordinates $X_{gg} - Z_{gg}$ plane. The transition of the vehicle initial altitude to the desired altitude is accomplished by a second order transfer function characterized by an input altitude control frequency and damping ratio.

When $T_y = 8$ during the j-th segment of flight, the vehicle attitude is obtained from instantaneous values of no-wind total angle of attack, roll angle of total angle of attack orientation, bank angle, altitude distance, rate, body angular attitude, and acceleration, as well as from input values, command altitude, altitude control frequency, and damping ratio.

The commanded angle of attack and angle of side slip is defined as follows:

(1) Commanded Angle of Attack

$$\alpha_c = \begin{cases} 45^\circ + \Delta_{ak} & \text{If } \alpha_c^* > 45^\circ \\ -45^\circ + \Delta_{ak} & \text{If } \alpha_c^* < -45^\circ \\ \alpha_c^* + \Delta_{ak} & \text{Otherwise} \end{cases}$$

where

$$\begin{aligned} \alpha_c^* = & \alpha_l + [(h_c - h) K_z - \dot{h} K_z^* - \ddot{h} K_z^*] \cos \varphi_c \\ & + [Y_{gg} K_z + \dot{Y}_{gg} K_z^* + \ddot{Y}_{gg} K_z^*] \sin \varphi_c \\ & - K_\theta Q_b \cos (\varphi - \varphi_c) - K_\psi \dot{R}_b \sin (\varphi - \varphi_c) \end{aligned}$$

and the angle of attack exponential flair-in factor is determined as follows:

$$\Delta_{ak} = \begin{cases} \Delta'_{ak} \exp \{ (t_{Bf} - t) [\omega_z / (2 \zeta_z)] \} & \text{If } \omega_z > 0 \\ 0 & \text{Otherwise} \end{cases}$$

where

$$\Delta'_{ak} = [\alpha_{cf}^* - \alpha_{lf}]$$

and the angle of attack rotated to the commanded vertical is

$$\alpha_\ell = \arctan \{ [\tan \tilde{\alpha}'] / [\sec (\varphi - \varphi_c + \bar{\epsilon})] \}$$

where the values of the vehicle trajectory parameters with subscript "f" are determined at the beginning of this segment of flight type control.

(2) Commanded Angle of Side Slip

$$\beta_c = \begin{cases} 45 + \Delta_{bk} & \text{If } \beta_c^* > 45^\circ \\ -45 + \Delta_{bk} & \text{If } \beta_c^* < -45 \\ \beta_c^* + \Delta_{bk} & \text{Otherwise} \end{cases}$$

where

$$\begin{aligned} \beta_c^* = & \beta_\ell + [Y_{gg} K_z + \dot{Y}_{gg} K_z + \ddot{Y}_{gg} K_z] \cos \varphi_c \\ & - [(h_c - h) K_z - \dot{h} K_z - \ddot{h} K_z] \sin \varphi_c \\ & + K_{\theta} Q_b \sin (\varphi - \varphi_c) - K_{\dot{\theta}} R_b \cos (\varphi - \varphi_c) \end{aligned}$$

and the angle of side slip exponential flare-in factor is determined as follows:

$$\Delta_{bk} = \begin{cases} \Delta'_{bk} \exp \{ (t_{Bf} - t) [\omega_z / (2 \zeta_z)] \} & \text{If } \omega_z > 0 \\ 0 & \text{Otherwise} \end{cases}$$

and the angle of sideslip in the horizontal is:

$$\beta_L = \arctan \{ [(\tan \bar{\alpha}')]/[\csc (\varphi - \varphi_c + \bar{\epsilon})] \}$$

where

$$\Delta'_{bk} = [\beta_{zf} - \beta_{cf}^*]$$

where the values of the vehicle trajectory parameters with subscript "f" are determined at the beginning of this segment of flight type control.

The above gain are defined as:

$$K_z = \omega_z^2 / G_z$$

$$K_{\dot{z}} = 2\zeta_z |\omega_z| G_z$$

$$K_{\ddot{z}} = 1/G_z$$

where the values of h_c , ω_z , and ζ_z are input in the attitude control table in the locations of Q_{mj} , R_{mj} , and P_{mj} , respectively for the j -th type of flight row and the variable gain factor is determined as:

$$G_z = (\pi/180) [\ddot{a}_{xb} \bar{g}_e + N_{PEA} g_e / W]$$

$$K_{\ddot{\theta}} = \begin{cases} 0 & \text{if } M_y = 1 \text{ or } 4 \\ N_{PCD} I_{YY} / (N_{NVA} M_{PCD} + N_{PCD} \cdot M_{PDA}) & \text{Otherwise} \end{cases}$$

Pitch aerodynamic control normal force per radian fin deflection angle

$$N_{PAC} = (180/\pi) C_{Lz} q S_{Fz}$$

Pitch aerodynamic disturbing normal force per radian angle of attack

$$N_{PAD} = (180/\pi) C_{N1} q S_{RN} \bar{N}$$

Pitch total thrust control moment per radian TVC deflection angle

$$M_{PTC} = F \ell_e$$

Pitch main thrust control moment per radian TVC deflection angle

$$M_{PMC} = F_H \ell_e$$

Pitch aerodynamic control moment per radian fin deflection angle

$$M_{PAC} = N_{PAC} \cdot l_6$$

Pitch aerodynamic disturbing moment per radian angle of attack

$$M_{PAD} = N_{PAD} \cdot l_{cp}$$

Total pitch control moment per radian deflection angle

$$M_{PCD} = \begin{cases} K_{cf} \cdot M_{PAC} + M_{PTC} & \text{if } K_0 = 0 \text{ or } K_0 > 2 \\ K_{cf} \cdot M_{PAC} + M_{PMC} & \text{if } K_0 = 1 \\ M_{PAC} & \text{if } K_0 = 2 \end{cases}$$

Total pitch disturbing moment per radian angle of attack

$$M_{PDA} = M_{PAD} - M_{PAC}$$

Total pitch control normal force per radian deflection angle

$$N_{PCD} = \begin{cases} K_{cf} N_{PAC} + F & \text{if } K_0 = 0 \\ K_{cf} N_{PAC} + F_M & \text{if } K_0 = 1 \\ N_{PAC} & \text{if } K_0 = 2 \end{cases}$$

Total pitch disturbing normal force per radian angle of attack

$$N_{PDA} = N_{PAD} + N_{PAC}$$

Pitch trim normal force per radian angle of attack

$$N_{PEA} = \begin{cases} N_{PDA} & \text{if } M_y = 1 \text{ or } 4 \\ N_{PDA} + (M_{PDA}/M_{PCD})N_{PCD} & \text{Otherwise} \end{cases}$$

Force normal to velocity vector per radian angle of attack

$$N_{NVA} = a_{xb} W + N_{PDA}$$

$$K_{\dot{\theta}} = \left(I_{zz} / I_{yy} \right) K_{\ddot{\theta}}$$

Commanded bank angle

$$\varphi_c = 0$$

f. Constant Normal Load Factor ($T_y = 9$)

The programmed normal load factor type of flight will command the vehicle attitude so as to fly the missile with a specified acceleration in g's normal to the earth reference velocity vector. The transition from the initial load factor to the desired load factor is accomplished by a first order transfer function characterized by an input load factor flare-in constant.

The values of η_{cn} , η_{ct} , and φ_c are input in the attitude control table in the Q_{mj} , R_{mj} , and P_{mj} locations.

Defining the achieved load factor along the velocity vector is:

$$\begin{pmatrix} \eta_{ba} \\ -\eta_{bt} \\ -\eta_{bn} \end{pmatrix} = [A_\beta]^{-1} [A_\alpha]^{-1} \{\ddot{\vec{X}}_b\} \quad 1/\bar{g}_e$$

where η_{ba} is the acceleration along the velocity vector, η_{bt} is the acceleration transverse to the velocity vector, and η_{bn} is the acceleration normal to the velocity vector.

The achieved load factor along the velocity vector is:
(in commanded local roll coordinates).

$$\eta_{lt} = \eta_{bt} \cos (\varphi - \varphi_c) - \eta_{bn} \sin (\varphi - \varphi_c)$$

$$\eta_{ln} = \eta_{bt} \sin (\varphi - \varphi_c) + \eta_{bn} \cos (\varphi - \varphi_c)$$

The commanded angle of attack

$$\alpha_c = \begin{cases} 45^\circ + \Delta_{ak} & \text{If } \alpha_c^* > 45^\circ \\ -45^\circ + \Delta_{ak} & \text{If } \alpha_c^* < -45^\circ \\ \alpha_c^* + \Delta_{ak} & \text{Otherwise} \end{cases}$$

where

$$\alpha_c^* = \alpha_z + (\eta_{cn} - \eta_{zn}) K_\eta - K_\theta Q_b \cos(\varphi - \varphi_c) - K_\psi R_b \sin(\varphi - \varphi_c)$$

and the angle of attack experimental flare-in factor is determined as follows:

$$\Delta_{ak} = \begin{cases} 0 & \text{If } \tau_f = 0 \\ \Delta'_{ak} \exp[(t_{BF} - t)/\tau_f] & \text{Otherwise} \end{cases}$$

$$\Delta'_{ak} = \begin{cases} 0 & \text{If } \tau_f = 0 \\ [\alpha_{zf} - \alpha_{cf}^*] & \text{Otherwise} \end{cases}$$

The commanded angle of sideslip

$$\beta_c = \begin{cases} 45^\circ + \Delta_{bk} & \text{If } \beta_c^* > 45^\circ \\ -45^\circ + \Delta_{bk} & \text{If } \beta_c^* < -45^\circ \\ \beta_c^* + \Delta_{bk} & \text{Otherwise} \end{cases}$$

where

$$\beta_c^* = \beta_z - (\eta_{ct} - \eta_{zn}) K_\eta + K_\theta Q_b \sin(\varphi - \varphi_c) + K_\psi R_b \cos(\varphi - \varphi_c)$$

and the angle of side slip exponential flare-in factor is determined as follows:

$$\Delta_{bk} = \begin{cases} 0 & \text{If } \tau_f = 0 \\ \Delta'_{bk} \exp (t'_{bf} - t) & \text{Otherwise} \end{cases}$$

$$\Delta'_{bk} = \begin{cases} 0 & \text{If } \tau_f = 0 \\ (\beta_{bf} - \beta_{cf}^*) & \text{Otherwise} \end{cases}$$

g. Intercept Guidance ($T_y = 10$)

The intercept guidance type of flight will command the vehicle so as to fly the missile on a collision course to intersect with the input moving target coordinates. This type of flight represents a radio command guidance system where the signals are generated by an external facility which keeps track of the missile and target dynamical characteristics.

When $T_y = 10$ during the j -th segment of flight, the vehicle attitude is obtained from instantaneous values of flight path angle (γ_1), the flight path error to intercept angle (ϵ_{MI}), the flight path azimuth error to intercept (δ_{MI}), the partial derivative of the linear inertial acceleration normal to the velocity vector to the vehicle angle of attack (G_Z), the earth gravity and rotation acceleration (g_{Z1}), and vehicle velocity (V_e) as well as the guidance associated first order intercept guidance controller time constant (τ_{MI}), and maximum angle of attack (α_{max}) input in the attitude control table in the Q_{mj} and R_{mj} locations.

The command angles of attack angle of sideslip are defined as follows:

$$\alpha_c = \begin{cases} \alpha'_{IG} + \Delta_{ak} & \text{If } -\alpha_{max} < \alpha'_{IG} < \alpha_{max} \text{ or } \alpha_{max} = 0 \\ \alpha_{max} + \Delta_{ak} & \text{If } \alpha'_{IG} > \alpha_{max} \\ -\alpha_{max} + \Delta_{ak} & \text{If } \alpha'_{IG} < -\alpha_{max} \end{cases}$$

where

Commanded angle of attack

$$\alpha_c^* = \begin{cases} 0 & \text{if } G_Z = 0 \\ \epsilon_{MI} + \frac{g_{Z1} \cos \gamma_1}{G_Z} & \text{if } \tau_{MI} = 0 \\ \frac{(\pi/180) V_e \left(\frac{\epsilon_{MI}}{\tau_{MI}} + \dot{\sigma}_{MT} \right) + g_{Z1} \cos \gamma_1}{G_Z} & \text{if } \tau_{MI} \neq 0 \end{cases}$$

$$\beta_c = \begin{cases} \beta_{IG}^* + \Delta_{bk} & \text{If } -\alpha_{\max} < \beta_{IG}^* < \alpha_{\max} \text{ or } \alpha_{\max} = 0 \\ \alpha_{\max} + \Delta_{bk} & \text{If } \beta_{IG}^* > \alpha_{\max} \\ -\alpha_{\max} + \Delta_{bk} & \text{If } -\alpha_{\max} > \beta_{IG}^* \end{cases}$$

Commanded angle of side slip

$$\beta_c^* = \begin{cases} 0 & \text{if } G_Z = 0 \\ -\delta_{MI} & \text{if } \tau_{MI} = 0 \\ -\frac{(\pi/180) V_e \left(\frac{\delta_{MI}}{\tau_{MI}} + \dot{\lambda}_{MI} \right)}{G_Z} & \text{if } \tau_{MI} \neq 0 \end{cases}$$

where

G_Z is formulated in section C.2.e (Type 8 flight), ϵ_{MI} , $\dot{\sigma}_{MI}$, δ_{MI} , and λ_{MI} are formulated in section J.4.c, "Missile Target Coordinates"

The exponential flare-in factor is determined as follows:

$$\Delta_{ak} = \begin{cases} 0 & \text{If } \tau_{IG} = 0 \\ \Delta_{ak}^* \exp [(t_{Bf} - t)/\tau_{IG}] & \text{Otherwise} \end{cases}$$

where

$$\Delta_{ak}^* = \begin{cases} 0 & \text{If } \tau_f = 0 \\ [\alpha_{IGf}^* - \alpha_{zf}] & \text{Otherwise} \end{cases}$$

$$\Delta_{bk}^* = \begin{cases} 0 & \text{If } \tau_f = 0 \\ \Delta_{bk} \exp [(t_{Bf} - t)/\tau_{IG}] & \text{Otherwise} \end{cases}$$

$$\Delta_{bk}^i = \begin{cases} 0 & \text{If } \tau_f = 0 \\ (\beta_{lf} - \beta_{cf}^*) & \text{Otherwise} \end{cases}$$

where the values of the vehicle trajectory parameters with subscript "f" are determined at the beginning of the segment of flight type control.

h. Homing Guidance ($T_y = 11$)

The homing guidance type of flight will command the vehicle so as to fly the missile to a specified moving target. This type of flight is also called proportional navigation steering which commands the time rate change of the missile flight path angle proportional to the turning rate of the look angle between the missile seeker and the target.

When $T_y = 11$ during the j -th segment of flight the vehicle attitude is obtained from instantaneous values of flight path angle (γ_1); time rate change of the angle to target in pitch ($\dot{\alpha}_{MT}$), time rate change of the angle to target in yaw ($\dot{\lambda}_{MT}$) partial derivative of the linear inertial acceleration normal to the velocity vector to the vehicle angle of attack (G_z), the earth gravity and rotation acceleration (R_1), and vehicle velocity (V_e) as well as the navigation constant (K_{HG}), flare-in time factor (τ_{HG}), and maximum angle of attack (α_{max}) input in the attitude control table in the Q_{mj} , R_{mj} , and P_{mj} locations.

Commanded Angle of Attack

$$\alpha_c = \begin{cases} \alpha_{HG} + \Delta_{ak} & \text{If } -\alpha_{max} < \alpha_c^* < \alpha_{max} \text{ or } \alpha_{max} = 0 \\ \alpha_{max} + \Delta_{ak} & \text{If } \alpha_c^* > \alpha_{max} \\ -\alpha_{max} + \Delta_{ak} & \text{If } \alpha_c^* < -\alpha_{max} \end{cases}$$

where

$$\alpha_c^* = \begin{cases} 0 & \text{If } G_z = 0 \\ [K_{HG} (\pi/180) \dot{\alpha}_{MT} V_e + (g_{Z_1} \cos \gamma_1)] / G_z & \end{cases}$$

$$\beta_c = \begin{cases} \beta_c^* + \Delta_{ck} & \text{If } -\alpha_{\max} < \beta_c^* < \alpha_{\max} \text{ or } \alpha_{\max} = 0 \\ \alpha_{\max} + \Delta_{ck} & \text{If } \beta_c^* > \alpha_{\max} \\ -\alpha_{\max} + \Delta_{ck} & \text{If } \alpha_{\max} > \beta_c^* \end{cases}$$

$$\beta_c^* = \begin{cases} 0 & \text{If } G_z = 0 \\ -[K_{HG} (\pi/180) \dot{\lambda}_{MT} V_e / G_z] & \text{Otherwise} \end{cases}$$

where

G_z is formulated in paragraph C.2.e, $\dot{\alpha}_{MT}$ and $\dot{\lambda}_{MT}$ are formulated in section J.4.c, "Missile to Target Angles."

The exponential flare-in factor is determined as follows:

$$\Delta_{ak} = \begin{cases} 0 & \text{If } \tau_f = 0 \\ \Delta_{ak}' \exp [(t_{Bf} - t) / \tau_f] & \text{Otherwise} \end{cases}$$

where

$$\Delta_{ak}' = \begin{cases} 0 & \text{If } \tau_{HG} = 0 \\ (\alpha_{HGF}' - \alpha_{LF}) & \text{Otherwise} \end{cases}$$

$$\Delta_{bk} = \begin{cases} 0 & \text{If } \tau_f = 0 \\ \Delta_{bk}' \exp [(t_{Bf} - t) / \tau_f] & \text{Otherwise} \end{cases}$$

where

$$\Delta_{bk}' = \begin{cases} 0 & \text{If } \tau_f = 0 \\ (\beta_c^* - \beta_{LF}) & \text{Otherwise} \end{cases}$$

where the values of the vehicle trajectory parameters with subscript "f" are determined at the beginning of the segment of flight type control.

3. Thrust Modulation Control Table

The control law type shall be determined from a sequential input table. Each row in this table contains the following ten control variables.

| | | | |
|----|-------------|---|--------------------|
| 1. | F_y | thrust control law mode - dim | |
| | $F_y = 1$ | Specific velocity-time profile | |
| | $F_y = 2$ | Constant Mach number-time profile | |
| | $F_y = 3$ | Proportional-to-commanded turning rate profile | |
| | $F_y = 4$ | Minimum velocity during commanded turn profile | |
| | $F_y = 5$ | Constrained dynamic pressure profile | |
| | $F_y = 6$ | Axial acceleration proportional to line-of-sight rate | |
| 2. | q_{Fy} | Code which designates the quantity that determines when the j-th type of TMC ends | dim |
| 3. | K_{Fy} | Limit of the j-th type of TMC | dbi |
| 4. | TMC | Thrust dynamics mode | dim |
| | TMC = 0. | Achieved thrust equals commanded thrust | |
| | TMC = 1. | First order response system (solve \dot{P}_c equation) | |
| 5. | C_{Fy} | Thrust system proportionality system gain | dim |
| 6. | τ_{Fy} | Control system time constant | sec |
| 7. | MIN | Minimum velocity or constant Mach number | dim/ft/sec |
| 8. | q_{max} | Maximum allowable dynamic pressure | lb/ft ² |

9. q_{\min} Minimum allowable dynamic pressure lb/ft²

10. Open

Inputting a maximum of seven segments of thrust mode control per trajectory is possible. Let a_{Fyj} ($j = 1, 2, \dots, 7$) be the achieved value of a parameter designated by input and let K_{Fy} , be the input value of the parameter, then the j -th segment of thrust modulation control will apply for:

$$a_{Fyj} \neq K_{Fyj}$$

The time when equality in the above occurs will be determined and is defined as t_{Fyj} . When the criteria for leaving a segment has been satisfied, that segment is not re-entered during the trajectory.

The K_{Fyj} criteria are checked monotonically with respect to the j -index. The table is input in the L800-L869 region.

The following discussion provides a description of the control laws which will be used to determine the control thrust command, \hat{F}_c . These control laws are based upon the commanded thrust being proportional to the error in the control variable modified with a signal proportional to the control variable rate of change. The control gains will be determined internally within the program unless input by the program user.

a. Specific Velocity-Time Profile

If $F_y = 1$, the flight for a preprogrammed velocity-time profile will be established from specifying the command velocity history in tabular form. This tabular input will be in the L-number region L870-L899. The time coordinate t_{vpj} will be input in L870, L872, ..., L898 and the velocity V_{pj} in L871, L873, ..., L899. This corresponds to a maximum of 15 points. If the time is less than or greater than the first or last points in the table, the corresponding end point velocity are used. The points in the input velocity-time table are fit with a third order quadratic function, and the velocity and its time derivative are evaluated as V_{ccv} and \dot{V}_{ccv} respectively.

To minimize the collective system error and provide the desired velocity history, the following control equation for the thrust required to provide the desired acceleration is:

$$F_c = \hat{F}_c + K_{cv} (V_{ccv} - V_c) + m \ddot{V}_{ccv}$$

where V_{ecv} is the command velocity, V_e is the achieved velocity, K_{cv} is a velocity error gain, \hat{F}_c is the thrust required to maintain V_e a constant value, m is the missile mass and \dot{V}_{ecv} is the time rate change of the command velocity. The vehicle mass divided by the velocity error gain magnitude represents the time required to eliminate the accumulated velocity error. The automatic control of this gain will be

$$K_{cv} = m/\tau_{CF}$$

where m is the missile mass and τ_{CF} represents the first order lead constant which will be set proportional to the equivalent first order lag of the controllable motor or to the input value.

$$\tau_{CF} = \begin{cases} 5/\omega_p & \text{If } \tau_{Fy} = 0 \\ \tau_{Fy} & \text{Otherwise} \end{cases}$$

where ω_p is the pintle control frequency and τ_{Fy} is control system time constant input in the thrust modulation control table.

The thrust required to maintain V_e , i.e., retarding force is:

$$\begin{aligned} \hat{F}_c = & C + C_{\delta z} - (N_{py} - N_y - N_{\delta y}) \sin \bar{\beta} / \cos \bar{\alpha}' \\ & - (N_{pz} - N_z - N_{\delta z}) \sin \bar{\alpha} / \cos \bar{\alpha}' \\ & + g_{z1} \sin \gamma_1 m / \cos \bar{\alpha}' \end{aligned}$$

where C , N_Y and N_Z are the aerodynamic force components, $N_{\delta Y}$ and $N_{\delta Z}$ are the control fins normal force in yaw and pitch respectively. $C_{\delta Z}$ is the control fin axial force, $\tilde{\alpha}$ is the still-wind angle of attack, $\tilde{\beta}$ is the still wind angle of yaw, and $\tilde{\alpha}'$ is the still wind total angle of attack. N_{Py} and N_{Pz} are the aerodynamic normal forces due to yaw and pitch damping.

b. Constant Mach Number Flight

If $F_y = 2$, a constant Mach number flight path is utilized in a cruise-type vehicle such as SRAM. Flying constant Mach number can be used to maximize the vehicle lift to drag for a maximum range glide trajectory.

The command acceleration for constant Mach number flight is:

$$\dot{V}_{ecm} = V_e M \frac{d C_a}{dh} \sin \gamma_1$$

where V_e is the achieved missile velocity, M is the achieved missile Mach number, $d C_a/dh$ is the rate change of the speed of sound with change in altitude, and γ_1 is the flight path angle. The command velocity is:

$$V_{ecm} = M_c C_a$$

where M_c is the command Mach number input in the thrust modulation control table as MIN and C_a is the instantaneous speed of sound.

To provide the transition to achieve initially required steady state Mach number and to minimize the collective system error, the control law presented in $F_y = 1$ is used, i.e.,

$$F_c = \hat{F}_c + K_{cv} (V_{ecm} - V_e) + m \dot{V}_{ecm}$$

c. Proportional-to-Commanded Turning Rate

If $F_y = 3$, the thrust level will be commanded proportional to the attitude command turning rate. For air-to-air missiles, the guidance and control logic is benefited by a propulsion system in which the time rate change of flight path is proportional to the seeker look angle rate. The trajectory control forces to provide the time rate change of flight path angle are those normal to the missile flight path angle. Current air-to-air missile control the angular rate change by pulling angle of attack, which provides an aerodynamic lift force.

A different, and possibly more desirable, method of providing the forces to change the flight path angle is by TVC system and propulsion thrust, or a combination of lift and TVC. The thrust magnitude proportional-to-commanded turning rate can be used in simulation of advanced air-to-air missile TVC and TMC propulsion systems.

The control equation is as follows:

$$F_c = (\pi/180) K_{CPR} F_N (\dot{\theta}_m^2 + \dot{\psi}_m^2)^{1/2}$$

where $\dot{\theta}_m$ is the commanded pitch rate, $\dot{\psi}_m$ is the commanded yaw rate, F_N is the nominal delivered thrust and K_{CPR} is the thrust magnitude proportional to commanded turning rate system gain. This gain will be input in the thrust mode control table as C_{Fyj} .

d. Minimum Velocity

If $F_y = 4$, the trajectory will use the thrust time history input into the trajectory program when the value of velocity is greater than the minimum specified value; if the input thrust produces velocity less than the specified value, the thrust will be modulated to a value adequate to maintain the missile specified minimum velocity. The following logic will be used to perform this control. The command thrust is

$$F_c = \begin{cases} F_N & \text{If } V_{cv} < V_e \\ \hat{F}_c + K_{cv} (V_{cv} - V_e) & \text{If } V_{cv} \geq V_e \end{cases}$$

The control law presented in $F_y = 1$ is that used for $V_{cv} \geq V_e$, and V_{cv} is the input minimum velocity value set in the TMC table as MIN. F_N is the nominal thrust.

e. Constrained Dynamic Pressure Profile

If $F_y = 5$, the thrust shall be commanded to constrain the dynamic pressure between an upper and lower value input in the TMC cable as q_{\min} and q_{\max} . The missile structural loads are established by the forces and moment on the body during flight in the atmosphere. These forces result from thrust and aerodynamics. One of the severest structural loads is the bending moments caused by aerodynamic lift which is proportional to the dynamic pressure, and the angle of attack. Thus, if the dynamic pressure were to be constrained to be less than some specified value by using thrust magnitude controls, the missile critical loads could be controlled. For air-to-air missiles depending on aerodynamic surfaces for lift and for control; a desirable property of the propulsion system is that it be capable of providing enough thrust to keep the vehicle from "stalling out". A thrust magnitude control to guarantee a minimum dynamic pressure will prevent this stall condition. The control equations for the specified thrust for a constrained dynamic pressure are:

$$F_{cqmin} = \hat{F}_c + K_{cq} (q_{\min} - q) + r \dot{V}_{ccq}$$

$$F_{cqmax} = \hat{F}_c + K_{cq} (q_{\max} - q) + m \dot{V}_{ccq}$$

$$F_c = \begin{cases} F_N & \text{If } q_{\min} \leq q \text{ and } F_N \geq F_{cqmin} \\ & \text{or } q_{\max} \geq q \text{ and } F_N \leq F_{cqmax} \\ F_{cqmin} & \text{If } q < q_{\min} \text{ or } F_N < F_{cqmin} \\ F_{cqmax} & \text{If } q > q_{\max} \text{ or } F_N > F_{cqmax} \end{cases}$$

The command acceleration to constrain dynamic pressure is:

$$\dot{V}_{ecq} = \left(\frac{d C_a}{dh} M - \frac{d P_a}{dh} \frac{V_c}{2 P_a} \right) V_c \sin \gamma_1$$

where $d C_a/dh$ is the change in the speed of sound with change in altitude,

$d P_a/dh$ is the change in atmospheric pressure with change in altitude;

both are a function of altitude and are evaluated in the Atmosphere

Parameter (F-1) routine. M is the instantaneous Mach number, P_a is

the instantaneous atmospheric pressure, V_c is the instantaneous velocity and

γ_1 is the instantaneous flight path angle, where \hat{F}_c is the thrust required

to maintain V_c delineated in $F_y = 1$ logic, F_N is the nominal delivered

thrust and K_{cq} is the dynamic pressure error gain.

This gain error term will null the residual dynamic pressure error.

The dynamic pressure error gain is:

$$K_{cq} = \frac{V_c^2}{2 q \tau_{cq}}$$

the time constant is:

$$\tau_{cq} = \begin{cases} 5/\omega_p & \text{If } \tau_{Fy} = 0 \\ \tau_{Fy} & \text{Otherwise} \end{cases}$$

ω_p is the control frequency of the controllable motor and τ_{Fy} is the control system gain input in the TMC table.

f. Axial Acceleration Proportional to Line-of-Sight Rate

If $F_y = 6$, the thrust shall be commanded so that the axial acceleration is proportional to the line-of-sight rate between the attacking missile and its target. In addition, the missile-to-target distance rate shall be maintained less than a specified value. For an air-to-air missile, complex guidance and control logic is greatly enhanced by a propulsion system in which the axial acceleration is proportional to the line-of-sight rate between the missile and the target, subject to the constraint of minimum closing rate and constrained dynamic pressure band.

The basic philosophy of this mode of TMC is that the flight path changes are needed only when changes in the missile-target collision flight path are needed. Thus, if the missile is coasting towards the target, no thrust is needed except that to maintain closing rate. The trajectory control forces that provide time rate change of flight path angle are those normal to the missile flight path angle. Thus, when the target performs evasive maneuvers, power must be applied to change the missile flight path. Current air-to-air missiles control the angular rate change by pulling angle of attack, which provides an aerodynamic lift force. Advanced systems will provide the side force by attitude changes with TVC systems. Both systems are greatly improved by increased thrust during the turn. The constraint of dynamic pressure will assure, on the lower limit, that enough aerodynamic control force is available to provide control and the upper limit, that the aerodynamic bias on the vehicle will not cause structural failure. This type of thrust modulation control is essentially a mixture of (3) proportional-to-commanded rate profile, (4) minimum velocity during command turn profile, and (5) constrained dynamic pressure profile.

The commanded thrust to provide acceleration proportional to LOS rate is

$$F_{cALOS} = V_c m (\pi/180) (\dot{\sigma}_{MT}^2 + \dot{\lambda}_{MT}^2)^{1/2} + \hat{F}_c$$

where K_{ALOS} is the system gain set equal to C_{Fyj} in the thrust modulation control table. V_c is the instantaneous missile velocity, m is the missile mass, $\dot{\sigma}_{MT}$ and $\dot{\lambda}_{MT}$ are the LOS rates in pitch and yaw respectively, and \hat{F}_c is the thrust required to maintain constant velocity delineated in $Fy = 1$.

The command thrust to provide a minimum missile to target closing rate is:

$$F_{cclos} = \hat{F}_c + K_{cv} (\dot{R}_{MTmin} - \dot{R}_{MT})$$

where K_{cv} is the velocity error gain delineated in $Fy = 1$, \dot{R}_{MTmin} is the minimum closing velocity input in the thrust modulation control table as MIN, and \dot{R}_{MT} is the time rate change of the missile to target distance.

The commanded thrust to maintain the dynamic pressure is:

$$F_{ccqmin} = \hat{F}_c + K_{cq} (q_{min} - q) + m \dot{V}_{ccq}$$

and the commanded thrust to maintain the dynamic pressure below the upper constraint is:

$$F_{ccqmax} = \hat{F}_c + K_{cq} (q_{max} - q) + m \dot{V}_{ccq}$$

where the control laws and therms are the same as those given in $F_y = 5$, constrained dynamic pressure thrust profile.

The commanded thrust for $F_y = 6$ is as follows:

$$F_{c\text{clos}} = \begin{cases} F_{c\text{ALOS}} & \text{If } F_{c\text{ALOS}} > F_{c\text{clos}} \\ F_{c\text{clos}} & \text{Otherwise} \end{cases}$$

$$F_c = \begin{cases} F_{c\text{qmin}} & \text{If } F_{c\text{qmin}} > F_{c\text{clos}} \\ F_{c\text{qmax}} & \text{If } F_{c\text{qmax}} < F_{c\text{clos}} \\ F_{c\text{clos}} & \text{Otherwise} \end{cases}$$

D. ATTITUDE CONTROL SYSTEM

For point mass systems ($My = 1$ or 4) the achieved attitude is identical to the commanded attitude, or

$$\theta_b = \theta_m$$

$$\psi_b = \psi_m$$

$$\phi_b = \phi_m$$

and all other attitude control system calculations are ignored.

For finite-mass systems ($My = 2$ or 5), the achieved missile attitude (the relation between the b and i systems as shown in Figure 18) is a function of the angular velocities about the missile center-of-gravity:

$$\dot{\theta}_b = (Q_b \cos \phi_b - R_b \sin \phi_b) / \cos \psi_b$$

$$\dot{\psi}_b = Q_b \sin \phi_b + R_b \cos \phi_b$$

$$\dot{\phi}_b = P_b - \dot{\theta}_b \sin \psi_b$$

Initial values of θ_b , ψ_b and ϕ_b are obtained from input.

If My equals 1 or 4 and $Ty = 8, 9, 10$, or 11 at the end of the compute interval, set:

$$\dot{\theta}_m = (\theta_{m(j+1)} - \theta_{mj}) / \Delta t_{cj}$$

$$\dot{\psi}_m = (\psi_{m(j+1)} - \psi_{mj}) / \Delta t_{cj}$$

$$\dot{\phi}_m = (\phi_{m(j+1)} - \phi_{mj}) / \Delta t_{cj}$$

where Δt_{cj} is the compute interval

$$P_m = \dot{\phi}_m + \dot{\theta}_m \sin \psi_m$$

$$Q_m = \dot{\theta}_m \cos \psi_m \cos \phi_m + \dot{\psi}_m \sin \phi_m$$

$$R_m = \dot{\psi}_m \cos \phi_m - \dot{\theta}_m \cos \psi_m \sin \phi_m$$

$$P_b = P_m$$

$$Q_b = Q_m$$

$$R_b = R_m$$

1. PITCH AND YAW THRUST DEFLECTIONS

Thrust deflections are functions of missile attitude errors, angular velocities, and steady state errors and whether the simulated thrust vector control system is for a first or second order transfer function.

a. Attitude Error Angles--The pitch ($\Delta \theta_b$) and yaw ($\Delta \psi_b$) attitude errors shown in Figure 23 are the difference between the achieved and desired vehicle attitude and are formulated as follows:

$$\Delta \theta_b = \arcsin (-K_{13})$$

$$\Delta \psi_b = \arcsin K_{12}$$

with

$$-90^\circ \leq \Delta \theta_b, \Delta \psi_b \leq 90^\circ$$

where K_{13} and K_{12} are the elements of the K-matrix defined by:

$$[K] = [A_m]^{-1} [A_c]$$

b. Autopilot Control Law--The control loop diagram depicting those control laws are shown on Figure 22.

The command deflection signals are determined from

$$\delta_{Pc} = K_{DP} \Delta\theta_b - K_{RP} Q_b - K_{IP} \alpha$$

and

$$\delta_{Yc} = -K_{DY} \Delta\psi_b + K_{RY} R_b + K_{IY} \beta$$

where $K_{DP, Y}$ and $K_{RP, Y}$ are the attitude error and rate gains, respectively.

c. TVC Deflection Angle Achieved to Commanded Transfer Function--The thrust vector control system can be represented by a zero order, first order, or a second order transfer function. The second order transfer function is needed if the tail-wag-dog effect of a gimbal nozzle is to be simulated. If $\bar{I}_y = 0$ or $\bar{I}_z = 0$, quasi-finite mass calculations are used for δ_P and δ_Y respectively.

The following differential equations and logic are employed

1. Zero order

$$(\omega_c = \tau_c = 0)$$

$$\delta_P = \delta_{Pc}, \ddot{\delta}_P = 0 \quad (\bar{I}_Y \neq 0)$$

$$\delta_Y = \delta_{Yc}, \ddot{\delta}_Y = 0 \quad (\bar{I}_Z \neq 0)$$

$\dot{\delta}_P$ and $\dot{\delta}_Y$ are obtained by numerically differentiating δ_P and δ_Y

2. First order

$$(\omega_c = 0 \text{ and } \tau_c \neq 0)$$

$$\tau_c \dot{\delta}_P + \delta_P = \delta_{Pc}, \text{ and } \ddot{\delta}_P = 0 \quad (\bar{I}_Y \neq 0)$$

$$\tau_c \dot{\delta}_Y + \delta_Y = \delta_{Yc}, \text{ and } \ddot{\delta}_Y = 0 \quad (\bar{I}_Z \neq 0)$$

3. Second order

$$(\omega_c \neq 0 \text{ and } I_n = 0)$$

$$\ddot{\delta}_P + 2.0 \xi_c \omega_c \dot{\delta}_P + \omega_c^2 \delta_P = \omega_c^2 \delta_{Pc} (\bar{I}_Y \neq 0)$$

$$\ddot{\delta}_Y + 2.0 \xi_c \omega_c \dot{\delta}_Y + \omega_c^2 \delta_Y = \omega_c^2 \delta_{Yc} (\bar{I}_Z \neq 0)$$

4. Second order, including tail-wag-dog effect ($\omega_c \neq 0, I_n \neq 0$)

$$\ddot{\delta}_P + 2.0 \xi_c \omega_c \dot{\delta}_P + \omega_c^2 \delta_P = \omega_c^2 \delta_{Pc} + Q_b \left[1.0 + [W_n \iota_e \iota_n / (I_n \bar{g}_e)] \right] + W_n \iota_n Z_{bb} (180/\pi) / (g_e I_n) (\bar{I}_Y \neq 0)$$

$$\ddot{\delta}_Y + 2.0 \xi_c \omega_c \dot{\delta}_Y + \omega_c^2 \delta_Y = \omega_c^2 \delta_{Yc} + \dot{R}_b \left[1.0 + [W_n \iota_e \iota_n / (I_n \bar{g}_e)] \right] + W_n \iota_n \ddot{Y}_{bb} (180/\pi) / (g_e I_n) (\bar{I}_Z \neq 0)$$

Values of δ_{P0} and δ_{Y0} and $\dot{\delta}_{P0}$ and $\dot{\delta}_{Y0}$, the initial values of the pitch and yaw thrust vector deflection angles and angular rates, are obtained from input per stage or equated to the values existing at the end of the previous mode segment.

If $\bar{I}_Y = 0$, the logic and equations used to determine δ_P are:

$$\ddot{\delta}_P = 0$$

$$\dot{\delta}_P = 0$$

| | | |
|--|--|--|
| $\delta_P = (-\delta_{MP}) + (180/\pi) \left[\begin{array}{l} M_{DQ}/M_{PTC} \\ M_{DQ}/M_{PMC} \\ 0 \\ M_{DQ}/(M_{PTC} + M_{FAC} \cdot K_{Pcf}) \\ M_{DQ}/(M_{PMC} + M_{PAC} \cdot K_{Pcf}) \\ M_{DQ}/M_{PAC} \\ 0 \end{array} \right]$ | M_{DQ}/M_{PTC} | If $K_\delta = 0$ and $K_{Pcf} = 0$ |
| | M_{DQ}/M_{PMC} | If $K_\delta = 1$ and $K_{Pcf} = 0$ |
| | 0 | If $K_\delta = 2$ and $K_{Pcf} = 0$ |
| | $M_{DQ}/(M_{PTC} + M_{FAC} \cdot K_{Pcf})$ | If $K_\delta = 0$ and $K_{Pcf} \neq 0$ |
| | $M_{DQ}/(M_{PMC} + M_{PAC} \cdot K_{Pcf})$ | If $K_\delta = 1$ and $K_{Pcf} \neq 0$ |
| | M_{DQ}/M_{PAC} | If $K_\delta = 2$ and $K_{Pcf} \neq 0$ |
| | 0 | If $K_\delta = 2$ and $K_{Pcf} \neq 0$ |

and outside the atmosphere

If $\bar{I}_Z = 0$ and $M_Y = 5$, the logic and equations used for δ_Y are:

$$\ddot{\delta}_Y = 0, \quad \dot{\delta}_Y = 0$$

$$\delta_Y = (-\delta_{MY}) + (180/\pi) \left[\begin{array}{ll} M_{DR}/M_{PTC} & \text{If } K_\delta = 0 \text{ and } K_{Ycf} = 0 \\ M_{DR}/M_{PMC} & \text{If } K_\delta = 1 \text{ and } K_{Ycf} = 0 \\ G & \text{If } K_\delta = 2 \text{ and } K_{Ycf} = 0 \\ M_{DR}/(M_{PTC} + M_{YAC} \cdot K_{Ycf}) & \text{If } K_\delta = 0 \text{ and } K_{Ycf} \neq 0 \\ M_{DR}/(M_{PMC} + M_{YAC} \cdot K_{Ycf}) & \text{If } K_\delta = 1 \text{ and } K_{Ycf} \neq 0 \\ M_{DR}/M_{YAC} & \text{If } K_\delta = 2 \text{ and } K_{Ycf} \neq 0 \\ & \text{and } h \leq h_E \text{ and } h_E \neq -1 \\ 0 & \text{If } K_\delta = 2 \text{ and } K_{Ycf} \neq 0 \\ & \text{and outside the atmosphere} \end{array} \right]$$

Where ω_c is the input stage control system forcing frequency for the thrust vector deflection second order transfer function, τ_c is the input stage control system time constant for the thrust vector deflection first-order transfer function, ζ_c is the input stage control system damping ratio for the thrust vector deflection second order transfer function, δ_{pc} and δ_{yc} are the pitch and yaw thrust deflection angle commands, δ_p & δ_y , $\dot{\delta}_p$ & $\dot{\delta}_y$, and $\ddot{\delta}_p$ & $\ddot{\delta}_y$ are the pitch and yaw thrust deflection angles, angular rates, and angular accelerations, respectively, W_n is the input stage movable portion nozzle weight, l_n is the movable portion nozzle center of gravity gimbal point distance, I_n is the input stage movable portion nozzle moment of inertia about the gimbal point, \dot{Q}_b and \dot{R}_b are the pitch and yaw missile attitude angular acceleration, \ddot{Y}_{bb} and \ddot{Z}_{bb} are the inertial missile acceleration positive along the pitch axis and yaw axis, l the missile gimbal point to center of gravity distance.

d. Autopilot Gains--Three gain zones are available for the control system of each stage. Zone durations are as follows:

| | |
|--|--------|
| from stage initiation until $\sigma_{G1} = K_{G1}$ | Zone 1 |
| until $\sigma_{G2} = K_{G2}$ | Zone 2 |
| thereafter to stage termination | Zone 3 |

where σ_{Gi} ($i = 1, 2$) are the achieved values of quantities designated by code input and K_{Gi} ($i = 1, 2$) are the input zone limits. The time when equality occurs is always computed.

The control system gains per gain zone and stage are as follows:

Pitch Rotation Reaction Moment

$$M_{PRR} = I_{YY} \omega_v^2 + |M_{PAD} - M_{PAC}|$$

Yaw Rotation Reaction Moment

$$M_{YRR} = I_{ZZ} \omega_v^2 + |M_{YAD} - M_{YAC}|$$

Pitch Rotation Damping Moment Integral

$$I_{PRD} = 2 \zeta_v I_{YY} \omega_v$$

Yaw Rotation Damping Moment Integral

$$I_{YRD} = 2 \zeta_v I_{ZZ} \omega_v$$

Pitch and Yaw Total Thrust Control Moment per Radian TVC Deflection Angle

$$M_{PTC} = F \ell_e$$

Pitch and Yaw Main Thrust Control Moment per Radian TVC Deflection Angle

$$M_{PMC} = F_M \ell_e$$

Pitch Aerodynamic Control Moment per Radian Fin Deflection Angle

$$M_{PAC} = (180/\pi) C_{Lz} q S_{Fz} \ell_\delta$$

Yaw Aerodynamic Control Moment per Radian Fin Deflection Angle

$$M_{YAC} = M_{PAC}$$

Pitch Aerodynamic Disturbing Moment per Radian Angle of Attack

$$M_{PAD} = (180/\pi) C_{Nl} q S_{RN} \bar{N} \ell_{cp}$$

Yaw Aerodynamic Disturbing Moment per Radian Angle of Attack

$$M_{YAD} = M_{PAD}$$

Pitch Attitude Error Gain

$$K_{DP} = \begin{cases} 0 & \text{If } \bar{I}_Y = 0 \\ M_{PRR}/M_{PTC} & \text{If } f_{Gi} \neq 0 \text{ and } K_\delta = 0 \text{ and } K_{Pcf} = 0 \\ M_{PRR}/M_{PMC} & \text{If } f_{Gi} \neq 0 \text{ and } K_\delta = 1 \text{ and } K_{Pcf} = 0 \\ 0 & \text{If } f_{Gi} \neq 0 \text{ and } K_\delta = 2 \text{ and } K_{Pcf} = 0 \\ M_{PRR}/(M_{PTC} + M_{PAC} \cdot K_{Pcf}) & \text{If } f_{Gi} \neq 0 \text{ and } K_\delta = 0 \text{ and } K_{Pcf} \neq 0 \\ M_{PRR}/(M_{PMC} + M_{PAC} \cdot K_{Pcf}) & \text{If } f_{Gi} \neq 0 \text{ and } K_\delta = 1 \text{ and } K_{Pcf} \neq 0 \\ M_{PRR}/M_{PAC} & \text{If } f_{Gi} \neq 0 \text{ and } K_\delta = 2 \text{ and } K_{Pcf} \neq 0 \\ 0 & \text{If } f_{Gi} \neq 0 \text{ and } K_\delta = 2 \text{ and } K_{Pcf} \neq 0 \\ & \text{and } V_a = 0 \\ K'_{DPi} & \text{Otherwise} \end{cases}$$

Yaw Attitude Error Gain

$$K_{DY} = \begin{cases} 0 & \text{If } \bar{I}_Z = 0 \\ M_{YRR}/M_{PTC} & \text{If } f_{Gi} \neq 0 \text{ and } K_\delta = 0 \text{ and } K_{Ycf} = 0 \\ M_{YRR}/M_{PMC} & \text{If } f_{Gi} \neq 0 \text{ and } K_\delta = 1 \text{ and } K_{Ycf} = 0 \\ 0 & \text{If } f_{Gi} \neq 0 \text{ and } K_\delta = 2 \text{ and } K_{Ycf} = 0 \\ M_{YRR}/(M_{PTC} + M_{YAC} \cdot K_{Ycf}) & \text{If } f_{Gi} \neq 0 \text{ and } K_\delta = 0 \text{ and } K_{Ycf} \neq 0 \\ M_{YRR}/(M_{PMC} + M_{YAC} \cdot K_{Ycf}) & \text{If } f_{Gi} \neq 0 \text{ and } K_\delta = 1 \text{ and } K_{Ycf} \neq 0 \\ 0 & \text{If } f_{Gi} \neq 0 \text{ and } K_\delta = 2 \text{ and } K_{Ycf} \neq 0 \\ & \text{and } V_a = 0 \\ M_{YRR}/M_{YAC} & \text{If } f_{Gi} \neq 0 \text{ and } K_\delta = 2 \text{ and } K_{Ycf} \neq 0 \\ K'_{DYi} & \text{Otherwise} \end{cases}$$

Pitch Angle of Attack Gain

$$K_{IP} = \begin{cases} 0 & \text{If } \bar{I}_Y = 0 \text{ or } f_{Gi} = 1 \\ (M_{PAD} - M_{PAC}) / (M_{PTC} + M_{PAC} \cdot K_{Pcf}) & \text{If } f_{Gi} = 2 \text{ and } K_\delta = 0 \\ (M_{PAD} - M_{PAC}) / (M_{PMC} + M_{PAC} \cdot K_{Pcf}) & \text{If } f_{Gi} = 2 \text{ and } K_\delta = 1 \\ 0 & \text{If } f_{Gi} = 2 \text{ and } K_\delta = 2 \text{ and } \gamma_a = 0 \\ (M_{PAD} - M_{PAC}) / (M_{PAC}) & \text{If } f_{Gi} = 2 \text{ and } K_\delta = 2 \\ K'_{IPi} & \text{If } f_{Gi} = 0 \end{cases}$$

Yaw Angle of Side Slip Gain

$$K_{IY} = \begin{cases} 0 & \text{If } \bar{I}_z = 0 \text{ or } f_{Gi} = 1 \\ (M_{YAD} - M_{YAC}) / (M_{PTC} + M_{YAC} \cdot K_{Ycf}) & \text{If } f_{Gi} = 2 \text{ and } K_\delta = 0 \\ (M_{YAD} - M_{YAC}) / (M_{PMC} + M_{YAC} \cdot K_{Ycf}) & \text{If } f_{Gi} = 2 \text{ and } K_\delta = 1 \\ 0 & \text{If } f_{Gi} = 2 \text{ and } K_\delta = 2 \text{ and } V_a = 0 \\ (M_{YAD} - M_{YAC}) / (M_{YAC}) & \text{If } f_{Gi} = 2 \text{ and } K_\delta = 2 \\ K'_{IYi} & \text{If } f_{Gi} = 0 \end{cases}$$

Pitch Attitude Rate Gain

$$K_{RP} = \begin{bmatrix} 0 \\ I_{PRD}/M_{PTC} \\ I_{PRD}/M_{PMC} \\ 0 \\ I_{PRD}/(M_{PTC} + M_{PAC} \cdot K_{Pcf}) \\ I_{PRD}/(M_{PMC} + M_{PAC} \cdot K_{Pcf}) \\ 0 \\ I_{PRD}/M_{PAC} \\ K'_{RPI} \end{bmatrix}$$

If $\bar{I}_Y = 0$

If $f_{Gi} \neq 0$ and $K_\delta = 0$ and $K_{Pcf} = 0$

If $f_{Gi} \neq 0$ and $K_\delta = 1$ and $K_{Pcf} = 0$

If $f_{Gi} \neq 0$ and $K_\delta = 2$ and $K_{Pcf} = 0$

If $f_{Gi} \neq 0$ and $K_\delta = 0$ and $K_{Pcf} \neq 0$

If $f_{Gi} \neq 0$ and $K_\delta = 1$ and $K_{Pcf} \neq 0$

If $f_{Gi} \neq 0$ and $K_\delta = 2$ and $K_{Pcf} \neq 0$
and $V_a = 0$

If $f_{Gi} \neq 0$ and $K_\delta = 2$ and $K_{Pcf} \neq 0$

Otherwise

Yaw Attitude Rate Gain

$$K_{RY} = \begin{bmatrix} 0 \\ I_{YRD}/M_{PTC} \\ I_{YRD}/M_{PMC} \\ 0 \\ I_{YRD}/(M_{PTC} + M_{YAC} \cdot K_{Ycf}) \\ I_{YRD}/(M_{PMC} + M_{YAC} \cdot K_{Ycf}) \\ 0 \\ I_{YRD}/M_{YAC} \\ K'_{RYI} \end{bmatrix}$$

If $\bar{I}_Z = 0$

If $f_{Gi} \neq 0$ and $K_\delta = 0$ and $K_{Ycf} = 0$

If $f_{Gi} \neq 0$ and $K_\delta = 1$ and $K_{Ycf} = 0$

If $f_{Gi} \neq 0$ and $K_\delta = 2$ and $K_{Ycf} = 0$

If $f_{Gi} \neq 0$ and $K_\delta = 0$ and $K_{Ycf} \neq 0$

If $f_{Gi} \neq 0$ and $K_\delta = 1$ and $K_{Ycf} \neq 0$

If $f_{Gi} \neq 0$ and $K_\delta = 2$ and $K_{Ycf} \neq 0$
and $V_a = 0$

If $f_{Gi} \neq 0$ and $K_\delta = 2$ and $K_{Ycf} \neq 0$

Otherwise

where the criteria for evaluating vehicle damping ratio and the vehicle control frequency are given in section D.1.e.

The following parameters are limited by input:

$$\begin{array}{ll}
 |K_{DP}\Delta\theta_b| \leq L_1 & |K_{DY}\Delta\theta_b| \leq L_6 \\
 |\delta_{Pc}| \leq L_2 & |\delta_{Yc}| \leq L_7 \\
 |\delta_p| \leq L_3 & |\delta_y| \leq L_8 \\
 |\dot{\delta}_p| \leq L_4 & |\dot{\delta}_y| \leq L_9 \\
 |\ddot{\delta}_p| \leq L_5 & |\ddot{\delta}_y| \leq L_{10}
 \end{array}$$

where L_j ($j = 1, 2, \dots, 10$) are input for each stage. If a limit is zero, then no limit of the parameter will be made.

The angular velocities, $\dot{\delta}_p$ and $\dot{\delta}_y$ are further limited by the following:

If

$$\delta_p = L_3, \text{ then } \dot{\delta}_p = 0$$

or

$$\delta_y = L_8, \text{ then } \dot{\delta}_y = 0$$

e. Vehicle Control Frequency and Damping Ratio

$$\zeta_v = \begin{cases} \zeta'_v & \text{If } \zeta'_v \neq 0 \\ 0.7 & \text{Otherwise} \end{cases}$$

$$\omega_v = \begin{cases} \omega'_v & \text{If } \omega'_v \neq 0 \\ \text{anti } \ell_n [10.132079 - 1.382972 (\ell_n W_{01}) \\ + 0.0624466 (\ell_n W_{01})^2 - 0.00093655891 (\ell_n W_{01})^3] & \end{cases}$$

where ζ'_v and ω'_v are input per stage

where the liftoff weight is

The stage I liftoff weight is determined as follows:

$$W_{01} = \begin{cases} W_{01}' & \text{If } W_{01}' > 0 \\ 1 \times \hat{W}_{01} & \text{If } K_k < 2 \\ 3 \times \hat{W}_{02} & \text{If } K_k = 2 \\ 7 \times \hat{W}_{03} & \text{If } K_k = 3 \\ 11 \times \hat{W}_{04} & \text{If } K_k = 4 \end{cases}$$

where \hat{W}_{0k} is the vehicle initial weight of the K_k -th stage.

2. ROLL CONTROL

The simulated roll control system discussed below assumes either a power source from the main propulsive one (Figure 19), or aerodynamic control fins. If $K_{RC} = 0$, a roll system does not exist. If $K_{RC} = 1$, an auxiliary thrust control system is operating and if $K_{RC} = 2$ aerodynamic fins provide roll control. A bang-bang system with dead band is simulated if K_{DR} is zero and a proportional system is simulated if K_{DR} is non-zero. The force signal is a function of vehicle roll attitude error, angular velocity, and steady state error. The roll control equations are ignored if either $M_y \neq 5$ or I_x is zero

a. Roll Attitude Error Angle

The roll attitude error shown in Figure 23 is determined from

$$\Delta\phi_b = \arctan (K_{23} - K_{32}) / (K_{22} + K_{33})$$

with

$$-180^\circ < \Delta\phi_b \leq 180^\circ$$

and the roll attitude error rate (not integrated) is

$$\dot{\Delta\phi}_b = P_m - P_b + (Q_m K_{21} + R_m K_{31} - Q_b K_{12} - R_b K_{13}) / (1 + K_{11})$$

where K_{DR} and K_{IR} are the attitude error and bias gains determined from input, K_{ij} 's are the elements of the K matrix and P_m , Q_m , and R_m are the current input roll, pitch, and yaw commands, respectively.

b. Auxiliary Roll Thrusters

The roll command signal is determined from one of the following if

$$K_{RC} = 1$$

Zero Order Thrusters

$$\text{If } K_{DR} \neq 0 \text{ and } K_{IR} = 0, \text{ then } F_c = K_{DR} \Delta\phi_b - K_{RR} P_b$$

First Order Thrusters

If $K_{DR} \neq 0$ and $K_{IR} \neq 0$, then $\dot{F}_c = K_{DR} \Delta\phi_b - K_{RR} \dot{P}_b + K_{IR} \Delta\phi_b$

and F_c is the integral of \dot{F}_c .

Bang-Bang Thrusters ($K_{DR} = 0$)

$$F_c = \frac{L_{Rc}}{2} \left[1 \cdot \text{sign} \left[F_D - F_\Delta \left[1 - D (1 + 1 \cdot \text{sign} \dot{F}_D)/2 \right] \right] \right. \\ \left. + 1 \cdot \text{sign} \left[F_D + F_\Delta \left[1 + D (1 + 1 \cdot \text{sign} \dot{F}_D)/2 \right] \right] \right]$$

where the rate gain, K_{RR} , the dead band control quantity, F_Δ , and the hysteresis, D , are determined from input and if F_c is integrated to obtain F_c , then its initial value at stage initiation is obtained from input. The phase plane signal and derivative (not integrated) are

$$F_D = \Delta\phi_b - K_{RR} P_b$$

$$\dot{F}_D = \Delta\dot{\phi}_b - K_{RR} \dot{P}_b$$

The roll command signal is limited if $L_{Rc} \neq 0$ such that

$$|F_c| \leq L_{Rc}$$

where L_{Rc} is determined from input.

The achieved roll thrust level is computed from

$$\dot{F}_R = (F_c - F_R)/\tau_R$$

where the roll control time constant, τ_R is determined from input and the initial value at stage initiation is obtained from input.

Three sets of roll control system parameters can be input for each stage. Values are determined as follows:

$$\begin{array}{ll} \tau_{R1} & \dots \text{ if } t_B \leq t'_{R2} \\ \tau_R, F_{\Delta}, D, L_{Rc}, K'_{PR_i}, K'_{RR_i}, K'_{IR_i} & \tau_{R2} \dots \text{ if } t'_{R2} \leq t_B \leq t'_{R3} \\ \tau_{R3} & \dots \text{ if } t_B \geq t'_{R3} \end{array}$$

where τ_{Rj} , $F_{\Delta j}$, D_j , L_{Rcj} , $K'_{D,R,IRj}$, and l_{Rj} and $t'_{R2,3}$ are input for each stage and where l_R is the roll control motor lever arm shown in Figure 1.5 and used in the angular momenta equation.

Thrust Control Moment

$$M_{FCP} = F_R l_R$$

c. Roll Control Aerodynamic Fins

The roll command signal for aerodynamic control fins is as follows:

If $\bar{I}_R \neq 0$ and $K_{Rc} = 2$ the following differential equations and logic are employed:

1. Zero Order ($\omega_c = \tau_c = 0$)

$$\delta_R = \delta_{Rc}, \dot{\delta}_R = \dot{\delta}_{Rc} \text{ and } \ddot{\delta}_R = 0$$

2. First Order ($\omega_c = 0$ and $\tau_c \neq 0$)

$$\tau_c \dot{\delta}_R + \delta_R = \delta_{Rc}, \text{ and } \ddot{\delta}_R = 0$$

3. Second Order ($\omega_c \neq 0$)

$$\ddot{\delta}_R + 2.0 \zeta_c \omega_c \dot{\delta}_R + \omega_c^2 \delta_R = \omega_c^2 \delta_{RC}$$

If $\bar{I}_R = 0$, quasi-finite mass equations are used:

$$\ddot{\delta}_R = 0, \dot{\delta}_R = 0 \text{ and}$$

$$\delta_R = (-\delta_{MR}) + (180/\pi) M_{DP}/M_{RAC}$$

d. Roll Control Gains

Roll Aerodynamic Control Moment per Radian Fin Deflection Angle

$$M_{RAC} = 2 (180/\pi) q S_{Fz} C_{Lz} l_{\delta r}$$

Roll Rotation Reaction Moment

$$M_{RRR} = I_{xx} \omega_v^2$$

Roll Rotation Damping Moment Integral

$$I_{RRD} = 2 \zeta_v I_{xx} \omega_v$$

Roll Attitude Error Gain

$$K_{DR} = \begin{cases} 0 & \text{If } \bar{I}_X = 0 \\ M_{RRR}/M_{RAC} & \text{If } K'_{DR1} = 0 \text{ \& } K_{RC} \neq 0 \\ K'_{DR1} & \text{Otherwise} \end{cases}$$

Roll Attitude Rate Gain

$$K_{RR} = \begin{cases} 0 & \text{If } \bar{I}_X = 0 \\ I_{RRD}/M_{RAC} & \text{If } K'_{RRi} = 0 \text{ and } K_{RC} \neq 0 \\ K'_{RRi} & \text{Otherwise} \end{cases}$$

$$K_{IR} = K'_{IRi}$$

Roll control commanded Aerodynamic Fin Angle

$$\delta_{RC} = K_{DR} \Delta\phi_b - K_{RR} P_b$$

2. MISSILE LOCATION

The vehicle location with respect to a spherical earth is defined. Parameters are shown in Figure 24.

1. Altitude and Earth Centered Coordinates

Vehicle altitude and rate change are determined from position components defined in an earth geocentric coordinate system as follows:

$$X_{cc} = X_{ee} \cos \rho_L - Z_{ee} \sin \rho_L + r_e \sin \rho_L$$

$$Y_{cc} = Y_{ee}$$

$$Z_{cc} = X_{ee} \sin \rho_L + Z_{ee} \cos \rho_L - r_e \cos \rho_L$$

$$\dot{X}_{cc} = \dot{X}_{ee} \cos \rho_L - \dot{Z}_{ee} \sin \rho_L$$

$$\dot{Y}_{cc} = \dot{Y}_{ee}$$

$$\dot{Z}_{cc} = \dot{X}_{ee} \sin \rho_L + \dot{Z}_{ee} \cos \rho_L$$

where the launch latitude, ρ_L , and the earth radius, r_e , are input and position components X_{ee} , Y_{ee} , and Z_{ee} are obtained from the integration of the linear momenta equations.

Vehicle distance from the earth center is

$$r_c = (X_{cc}^2 + Y_{cc}^2 + Z_{cc}^2)^{\frac{1}{2}}$$

$$\dot{r}_c = (\dot{X}_{cc} X_{cc} + \dot{Y}_{cc} Y_{cc} + \dot{Z}_{cc} Z_{cc})/r_c$$

and the vehicle altitude and rate change are

$$h = r_c - r_e$$

$$\dot{h} = \dot{r}_c$$

2. Heading Azimuth, Latitude and Longitude

Vehicle azimuth in the launch horizontal plane is

$$\psi = \begin{cases} \psi_1 & \text{If } \dot{Y}_{ee} = \dot{X}_{ee} = 0 \\ \arctan \dot{Y}_{ee} / \dot{X}_{ee} & \text{Otherwise} \end{cases}$$

with

$$0 \leq \psi < 360^\circ$$

Latitude and Longitude

The vehicle latitude is

$$\rho = \arcsin X_{cc}/r_c$$

with

$$-90^\circ \leq \rho \leq 90^\circ$$

and the change in longitude from launch is

$$\mu' = \arctan Y_{cc}/-Z_{cc}$$

with

$$0 \leq \mu' < 360^\circ$$

The longitude is defined so that west of Greenwich, England is positive and east is negative. The longitude is

$$\mu = \begin{cases} \mu_L - \mu' & \text{If } -180^\circ < \mu_L - \mu' \\ 360^\circ + \mu_L - \mu' & \text{Otherwise} \end{cases}$$

where the launch longitude, μ_L , is input.

3. Ground and Slant Ranges

The down range-cross range coordinates are shown in Figure 25.

The range angle is

$$\phi_s = \begin{cases} \arcsin (X_{ee}^2 + Y_{ee}^2)^{1/2} / r_c & \text{If } \sin \phi \leq 0.7 \\ \arccos (r_e - Z_{ee}) / r_c & \text{Otherwise} \end{cases}$$

with

$$0 \leq \phi_s < 180^\circ$$

and the ground range is

$$S_s = (\pi/180) r_e \phi_s$$

The cross range angle is

$$\zeta = \arcsin [(Y_{ee} \cos \phi_i - X_{ee} \sin \phi_i) / r_c]$$

$$\dot{\zeta} = \frac{(180/\pi)(\dot{Y}_{ee} \cos \phi_i - \dot{X}_{ee} \sin \phi_i - \dot{r}_c \sin \zeta)}{r_c \cos \zeta}$$

where

$$-90^\circ < \zeta \leq 90^\circ$$

the cross range is

$$S_c = (\pi/180) r_e \zeta$$

$$\dot{S}_c = (\pi/180) r_e \dot{\zeta}$$

the down range angle is

$$\phi = \arctan [(X_{ee} \cos \phi_i + Y_{ee} \sin \phi_i) / (r_e - Z_{ee})]$$

$$\dot{\phi} = (180/\pi) [(\dot{X}_{ee} \cos \psi_1 + \dot{Y}_{ee} \sin \psi_1) \cos^2 \phi + \dot{Z}_{cc} \sin \phi \cos \phi] / (r_e - z_{ee})$$

where

$$- 180^\circ < \phi \leq 180^\circ$$

the down range is

$$S = (\pi/180) r_e \phi$$

$$\dot{S} = (\pi/180) r_e \dot{\phi}$$

F. FLIGHT ENVIRONMENT AND FORCES

Parameters which define the vehicle flight environment and aerodynamic forces are given below.

1. Atmospheric Parameters

The ambient pressure, P_a , the speed of sound, C_a , the partial derivative of ambient pressure with altitude, $\partial P_a / \partial h$, and, the partial derivative of the speed of sound with altitude, $\partial C_a / \partial h$, are functions of the missile altitude, h , and the formulas and constants contained in National Aeronautics and Space Administration, "U.S. Standard Atmosphere, 1962".

a. Speed of Sound, ft/sec

$$C_a = \begin{cases} 1,177.7301 & \text{If } h \leq -16,391.307 \\ 3,417.9390 & \text{If } h \geq 2,296,587.9 \\ \sqrt{G_{RZ} T_M} & \text{Otherwise} \end{cases}$$

where

$$G_{RZ} = 2403.1756$$

Temperature Gradient, °R/ft

$$S_B = \begin{cases} 0.0 & \text{If } h \leq -16,391.307 \\ 0.0 & \text{If } h \geq 2,296,587.9 \\ \frac{T_{MB(i+1)} - T_{MBi}}{h_{B(i+1)} - h_{Bi}} & \text{Otherwise} \end{cases}$$

Temperature, °R

$$T_M = T_{MBi} + S_B (h - h_{Bi})$$

The values of T_{MB} and h_B are given in the table at the end of this section. The index value i is set such that $h_{Bi} \leq h < h_{B(i+1)}$.

b. Partial Derivative of the Speed of Sound with Altitude, (1/sec)

$$\frac{\partial c_a}{\partial h} = \begin{cases} 0.0 & \text{If } h \leq -16,391.307 \\ 0.0 & \text{If } h \geq 2,296,587.9 \\ \frac{G_{RZ} S_B}{2 C_a} & \text{Otherwise} \end{cases}$$

c. Ambient Pressure, lb/ft²

$$P_a = \begin{cases} 3711.0756 & \text{If } h \leq -16,391.307 \\ 2.4891 \times 10^{-9} & \text{If } h \geq 2,296,587.9 \\ P_B e^{-\frac{Z_{MGM} (h_B - h)}{R^* (S_B R_B - T_{MB}) R R_B}} \times \left[\frac{R_B S_B (h - h_B) + T_{MB}}{R T_{MB}} \right]^{-\frac{Z_{MGM} S_B}{R^* (S_B R_B - T_{MB})^2}} \end{cases}$$

where

$$R = h + R_Z$$

$$R_B = h_B + R_Z$$

$$Z_{MXGM} = 40.80696 \times 10^{16}$$

$$R_Z = 20,925,780.$$

$$R^* = 49718.9585$$

and

$$Z_{MGM} = Z_{MXGM} \times Z_K$$

d. Partial Derivative of Ambient Pressure with Altitude (lb/ft³)

$$\frac{\partial P_a}{\partial h} = \begin{cases} 0.0 & \text{If } h \leq -16,391.307 \\ 0.0 & \text{If } h \geq 2,296,587.9 \\ P_a \left[\frac{Z_{MGM}}{R^* (S_B R_B - T_{MB}) R^*} - \frac{Z_{MGM}}{R^* (S_B R_B - T_{MB}) R^*} \left(\frac{S_B}{S_B (h - h_B) + T_{MB}} - \frac{1}{R} \right) \right] & \text{Otherwise} \end{cases}$$

e. U. S. Standard Atmosphere Altitude - Temperature - Pressure Table

| Altitude, h_B , ft | Temperature T_{MB} , °R | Pressure, P_B , lb/ft ² | Correction Z_K , dim |
|-------------------------|------------------------------|---|---------------------------|
| -16,391.307 | 577.17 | 3711.0756 | 1.00000969 |
| 0.0 | 518.67 | 2116.22 | 1.00006922 |
| 36,151.798 | 389.97 | 472.68122 | 0.99997683 |
| 65,823.897 | 389.97 | 114.3456 | 0.99994851 |
| 105,518.46 | 411.57 | 18.12897 | 0.99988460 |
| 155,348.08 | 487.17 | 2.3163292 | 0.99994118 |
| 172,010.76 | 487.17 | 1.2322622 | 0.99994953 |
| 202,070.31 | 454.77 | 0.38032587 | 1.00007811 |
| 262,447.98 | 325.17 | 2.1673089×10^{-2} | 0.99990452 |
| 295,275.59 | 325.17 | 3.433025×10^{-3} | 0.99988145 |
| 328,083.99 | 379.17 | 6.28115×10^{-4} | 0.99987195 |
| 360,892.39 | 469.17 | 1.5360×10^{-4} | 0.99984532 |
| 393,700.79 | 649.17 | 5.2667×10^{-5} | 0.99983723 |
| 492,125.98 | 1729.17 | 1.0572×10^{-5} | 0.99994038 |
| 524,934.38 | 1999.17 | 7.7157×10^{-6} | 0.99979481 |
| 557,742.78 | 2179.17 | 5.8325×10^{-6} | 0.99978217 |
| 623,359.58 | 2431.17 | 3.5197×10^{-6} | 0.99978447 |
| 754,593.18 | 2791.17 | 1.4537×10^{-6} | 0.99968987 |
| 984,251.97 | 3295.17 | 3.9345×10^{-7} | 0.99959327 |
| 1,312,336.0 | 3889.17 | 8.4177×10^{-8} | 0.99944931 |
| 1,640,419.9 | 4357.17 | 2.2885×10^{-8} | 0.99941075 |
| 1,968,503.9 | 4663.17 | 7.2059×10^{-9} | 0.99921789 |
| 2,296,587.9 | 4861.17 | 2.4891×10^{-9} | |

2. Winds

a. Wind Speed and Azimuth

The wind velocity is a function of vehicle altitude and input wind speed, v_w , and azimuth ψ_w . The wind direction is directed parallel to the local horizontal with ψ_w being the clockwise angle from north to the direction the wind is coming from.

If the input altitude multiplier, K_a , is zero, or the vehicle is outside the atmosphere

$$v_w = \dot{v}_w = \psi_w = \dot{\psi}_w = 0 \text{ and}$$

$$\dot{\vec{x}}_{aee} = \dot{\vec{x}}_{ee}$$

where $\dot{\vec{x}}_{aee}$ are the vehicle velocity components with respect to the air as measured in the 3-system and $\dot{\vec{x}}_{ee}$ the still air components.

For

$$K_h \neq 0 \text{ and } K_h h_j \leq h \leq K_h h_{j+1}$$

$$v_w = K_v [K_h (h_j v_{w(j+1)} - h_{j+1} v_{wj}) + h(v_{wj} - v_{w(j+1)})] / (h_j - h_{j+1}) K_h$$

$$\dot{\psi}_w = K[\dot{\psi}_w] [K_h (h_j \dot{\psi}_{w(j+1)} - h_{j+1} \dot{\psi}_{wj}) + h(\dot{\psi}_{wj} - \dot{\psi}_{w(j+1)})] / (h_j - h_{j+1}) K_h$$

If $h > K_h h_J$ (J denoting the last input where $J = 1, 2, \dots, 32$),

$$\text{then } v_w = K_v v_{wJ} \text{ and } \dot{\psi}_w = K_{\dot{\psi}} \dot{\psi}_{wJ}$$

$$\text{If } h < K_h h_1, \text{ then } v_w = K_v v_{w1} \text{ and } \dot{\psi}_w = K_{\dot{\psi}} \dot{\psi}_{w1}$$

The derivatives are calculated as

$$\dot{v}_w = (dv_w/dh)\dot{h}$$

$$\dot{\dot{\psi}}_w = (d\dot{\psi}_w/dh)\dot{h}$$

with

$$0 \leq \phi_w < 360^\circ$$

$$dv_w/dh = \begin{cases} 0 & \text{If } h < K_h h_1 \text{ or } h > K_h h_J \\ K_v (v_{w(j+1)} - v_{wj}) / [K_h (h_{j+1} - h_j)] & \text{Otherwise} \end{cases}$$

$$d\phi_w/dh = \begin{cases} 0 & \text{If } h < K_h h_1 \text{ or } h > K_h h_J \\ K_\phi (\phi_{w(j+1)} - \phi_{wj}) / [K_h (h_{j+1} - h_j)] & \text{Otherwise} \end{cases}$$

where v_{wj} , ϕ_{wj} , and h_j ($j = 1, 2, \dots, 32$), K_v , and K_ϕ are input.

b. Wind Local and Launch Centered Cartesian Coordinate

The Cartesian components of wind velocity and acceleration in the local coordinate system (the 1-system) are

$$\dot{X}_{w11} = -v_w \cos \phi_w$$

$$\dot{Y}_{w11} = -v_w \sin \phi_w$$

$$\dot{Z}_{w11} = 0$$

$$\ddot{X}_{w11} = -\dot{v}_w \cos \phi_w + (\pi/180) \dot{\phi}_w v_w \sin \phi_w$$

$$\ddot{Y}_{w11} = -\dot{v}_w \sin \phi_w - (\pi/180) \dot{\phi}_w v_w \cos \phi_w$$

$$\ddot{z}_{w11} = 0$$

where \dot{x}_{w11} is positive north, \dot{y}_{w11} east, and \dot{z}_{w11} along the vector connecting the missile and earth center, positive down.

From Figure 24, the wind velocity components in the e-system are

$$\dot{\vec{x}}_{wee} = [A_1] \dot{\vec{x}}_{w11}$$

with

$$[A_1] = \begin{bmatrix} \cos \rho_L & 0 & \sin \rho_L \\ 0 & 1 & 0 \\ -\sin \rho_L & 0 & \cos \rho_L \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \mu' & -\sin \mu' \\ 0 & \sin \mu' & \cos \mu' \end{bmatrix} \begin{bmatrix} \cos \rho & 0 & -\sin \rho \\ 0 & 1 & 0 \\ \sin \rho & 0 & \cos \rho \end{bmatrix}$$

where ρ_L is the input latitude and ρ and μ' the instantaneous vehicle latitude and longitude change, respectively.

c.

Artificial Wind Profile

The MMREM TVC design wind profile is constructed from the input specified peak wind altitude, h_{mxwd} (L0682). This artificial altitude-wind velocity table is set into the wind profile table. The final and initial altitude of maximum wind shear used in the TVC duty cycle slow rate calculations are also set.

If $h_{mxwd} > 0$ the wind profile is established as

$$h_{mxwd} = \begin{cases} 240,000 & \text{If } h_{mxwd} > 240,000 \\ h_{mxwd} & \text{Otherwise} \end{cases}$$

Altitudes of maximum wind shear

$$h_{\alpha} = h_{mxwd} + 3000$$

$$h_{\beta} = \begin{cases} 0 & \text{If } h_{mxwd} < 3000 \\ h_{mxwd} - 3000 & \text{Otherwise} \end{cases}$$

Velocity of wind shear

$$V_{w1k} = V_{wmax} - 1,000 S_{1k}$$

$$V_{w3k} = V_{wmax} - 3,000 S_{3k}$$

$$V_{w5k} = V_{wmax} - 5,000 S_{5k}$$

where V_{wmax} is the maximum wind velocity and S_{1k} , S_{3k} , and S_{5k} are the wind shear for 1,000, 3,000, & 5,000 feet depths respectively, all of which are function of the peak wind altitude.

If $0 < h_{\text{mxwd}} \leq 1,000$

$$h_1 = 0$$

$$v_{w1} = [v_{w1k} h_{\text{mxwd}} - v_{w\text{max}} (h_{\text{mxwd}} - 1,000)]/1000$$

$$h_2 = h_{\text{mxwd}}$$

$$v_{w2} = v_{w\text{max}}$$

$$h_3 = h_{\text{mxwd}} + 1,000$$

$$v_{w3} = v_{w1k}$$

$$h_4 = h_{\text{mxwd}} + 3,000$$

$$v_{w4} = v_{w3k}$$

$$h_5 = h_{\text{mxwd}} + 5,000$$

$$v_{w5} = v_{w5k}$$

$$h_6 = 80,000$$

$$v_{w6} = 75$$

$$h_7 = 100,000$$

$$v_{w7} = 90$$

$$h_8 = 300,000$$

$$v_{w8} = 90$$

If $1,000 < h_{\text{mxwd}} \leq 3,000$

$$h_1 = 0$$

$$v_{w1} = [v_{w3k} (h_{\text{mxwd}} - 1,000) - v_{w1k} (h_{\text{mxwd}} - 3000)]/2,000$$

$$h_2 = h_{\text{mxwd}} - 1,000$$

$$v_{w2} = v_{w1k}$$

$$h_3 = h_{\text{mxwd}}$$

$$v_{w3} = v_{w\text{max}}$$

$$h_4 = h_{\text{mxwd}} + 1,000$$

$$v_{w4} = v_{w1k}$$

$$h_5 = h_{\text{mxwd}} + 3,000$$

$$v_{w5} = v_{w3k}$$

$$h_6 = h_{\text{mxwd}} + 5,000$$

$$v_{w6} = v_{w5k}$$

$$h_7 = 80,000$$

$$v_{w7} = 75$$

$$h_8 = 100,000$$

$$v_{w8} = 90$$

$$h_9 = 300,000$$

$$v_{w9} = 90$$

If $3,000 < h_{mxwd} \leq 5,000$

$$h_1 = 0$$

$$v_{w1} = [v_{w5k} (h_{mxwd} - 3000) - v_{w3k} (h_{mxwd} - 5000)] / 2,000$$

$$h_2 = h_{mxwd} - 3,000$$

$$v_{w2} = v_{w3k}$$

$$h_3 = h_{mxwd} - 1,000$$

$$v_{w3} = v_{w1k}$$

$$h_4 = h_{mxwd}$$

$$v_{w4} = v_{wmax}$$

$$h_5 = h_{mxwd} + 1,000$$

$$v_{w5} = v_{w1k}$$

$$h_6 = h_{mxwd} + 3,000$$

$$v_{w6} = v_{w3k}$$

$$h_7 = h_{mxwd} + 5,000$$

$$v_{w7} = v_{w5k}$$

$$h_8 = 80,000$$

$$v_{w8} = 75$$

$$h_9 = 100,000$$

$$v_{w9} = 90$$

$$h_{10} = 300,000$$

$$v_{w10} = 90$$

If $5,000 < h_{mxwd} \leq 10,000$

$$h_1 = 0$$

$$v_{w1} = 50 - .003 h_{mxwd}$$

$$h_2 = h_{mxwd} - 5,000$$

$$V_{w2} = V_{w5k}$$

$$h_3 = h_{mxwd} - 3,000$$

$$V_{w3} = V_{w3k}$$

$$h_4 = h_{mxwd} - 1,000$$

$$V_{w4} = V_{w1k}$$

$$h_5 = h_{mxwd}$$

$$V_{w5} = V_{wmax}$$

$$h_6 = h_{mxwd} + 1,000$$

$$V_{w6} = V_{w1k}$$

$$h_7 = h_{mxwd} + 3,000$$

$$V_{w7} = V_{w3k}$$

$$h_8 = h_{mxwd} + 5,000$$

$$V_{w8} = V_{w5k}$$

$$h_9 = 30,000$$

$$V_{w9} = 75$$

$$h_{10} = 100,000$$

$$V_{w10} = 90$$

$$h_{11} = 300,000$$

$$V_{w11} = 90$$

IF $10,000 < h_{mxwd} \leq 32,000$

$$h_1 = 0$$

$$V_{w1} = 20$$

$$h_2 = h_{mxwd} - 5,000$$

$$V_{w2} = V_{w5k}$$

$$h_3 = h_{mxwd} - 3,000$$

$$V_{w3} = V_{w3k}$$

$$h_4 = h_{mxwd} - 1,000$$

$$V_{w4} = V_{w1k}$$

$$h_5 = h_{mxwd}$$

$$V_{w5} = V_{wmax}$$

$$h_6 = h_{mxwd} + 1,000$$

$$V_{w6} = V_{w1k}$$

$$h_7 = h_{\text{mxwd}} + 3,000$$

$$v_{w7} = v_{w3k}$$

$$h_8 = h_{\text{mxwd}} + 5,000$$

$$v_{w8} = v_{w5k}$$

$$h_9 = 80,000$$

$$v_{w9} = 75$$

$$h_{10} = 100,000$$

$$v_{w10} = 90$$

$$h_{11} = 300,000$$

$$v_{w11} = 90$$

If $32,000 < h_{\text{mxwd}} \leq 42,000$

$$h_1 = 0$$

$$v_{w1} = 20$$

$$h_2 = 10,000$$

$$v_{w2} = 50$$

$$h_3 = h_{\text{mxwd}} - 5,000$$

$$v_{w3} = v_{w5k}$$

$$h_4 = h_{\text{mxwd}} - 3,000$$

$$v_{w4} = v_{w3k}$$

$$h_5 = h_{\text{mxwd}} - 1,000$$

$$v_{w5} = v_{w1k}$$

$$h_6 = h_{\text{mxwd}}$$

$$v_{w6} = v_{w\text{max}}$$

$$h_7 = h_{\text{mxwd}} + 1,000$$

$$v_{w7} = v_{w1k}$$

$$h_8 = h_{\text{mxwd}} + 3,000$$

$$v_{w8} = v_{w5k}$$

$$h_9 = h_{\text{mxwd}} + 5,000$$

$$v_{w9} = v_{w5k}$$

$$h_{10} = 80,000$$

$$v_{w10} = 75$$

$$h_{11} = 100,000$$

$$v_{w11} = 90$$

$$h_{12} = 300,000$$

$$v_{w12} = 90$$

If $h_{\text{mxwd}} > 42,000$

| | |
|-------------------------------------|----------------------------|
| $h_1 = 0$ | $v_{w1} = 20$ |
| $h_2 = 10,000$ | $v_{w2} = 50$ |
| $h_3 = h_{\text{mxwd}} - 5,000$ | $v_{w3} = v_{w5k}$ |
| $h_4 = h_{\text{mxwd}} - 3,000$ | $v_{w4} = v_{w3k}$ |
| $h_5 = h_{\text{mxwd}} - 1,000$ | $v_{w5} = v_{w1k}$ |
| $h_6 = h_{\text{mxwd}}$ | $v_{w6} = v_{w\text{max}}$ |
| $h_7 = h_{\text{mxwd}} + 1,000$ | $v_{w7} = v_{w1k}$ |
| $h_8 = h_{\text{mxwd}} + 3,000$ | $v_{w8} = v_{w3k}$ |
| $h_9 = h_{\text{mxwd}} + 5,000$ | $v_{w9} = v_{w5k}$ |
| $h_{10} = h_{\text{mxwd}} + 38,000$ | $v_{w10} = 75$ |
| $h_{11} = h_{\text{mxwd}} + 58,000$ | $v_{w11} = 90$ |
| $h_{12} = 300,000$ | $v_{w12} = 90$ |

Maximum Wind Velocity

The maximum wind velocity is a tabular function of the input altitude of peak winds. The table is linearly interpolated.

Peak Wind Altitude
 h_{mxwd} , feet

Maximum Wind Velocity
 V_{wmax} , ft/sec

| | |
|----------|-----|
| 0 | 92 |
| 19,000 | 210 |
| 32,000 | 348 |
| 42,000 | 348 |
| 61,500 | 197 |
| 90,000 | 197 |
| 196,000 | 590 |
| ∞ | 590 |

Wind Shears

The wind envelope shears for incremental altitude of 1,000, 3,000, and 5,000 feet from the input design wind altitude (L682). Tables for the shears are listed at 1,000 foot intervals, starting at zero feet altitude and ending at 90,000 feet altitude. If Peak Wind Altitude exceeds 90,000 feet values at 90,000 feet are used. The table is linearly interpolated.

Wind Shear Table

| Peak Wind Altitude <u>h_{mxwd}, feet</u> | <u>Shear Depth</u> | | |
|---|---|---|---|
| | 1,000 feet <u>S_{1k}, 1/sec x 10^3</u> | 3,000 feet <u>S_{3k}, 1/sec x 10^3</u> | 5,000 feet <u>S_{5k}, 1/sec x 10^3</u> |
| 0 | .0425 | .0325 | .0145 |
| 1,000 | .0409 | .0305 | .0153 |
| 2,000 | .0393 | .0288 | .0161 |
| 3,000 | .0378 | .0272 | .0168 |
| 4,000 | .0362 | .0258 | .0173 |
| 5,000 | .0348 | .0247 | .0177 |
| 6,000 | .0348 | .0238 | .0179 |
| 7,000 | .0321 | .0232 | .0178 |
| 8,000 | .0308 | .0227 | .0175 |
| 9,000 | .0296 | .0224 | .0171 |
| 10,000 | .0284 | .0222 | .0167 |

Wind Shear Table (Cont'd)

| Peak Wind Altitude | 1,000 feet | Shear Depth 3,000 feet | 5,000 feet |
|--------------------------|---------------------------|---------------------------|---------------------------|
| h_{mxwd} , feet | S_{1k} , 1/sec x 10^3 | S_{3k} , 1/sec x 10^3 | S_{5k} , 1/sec x 10^3 |
| 11,000 | .0273 | .0220 | .0164 |
| 12,000 | .0263 | .0219 | .0161 |
| 13,000 | .0253 | .0216 | .0158 |
| 14,000 | .0244 | .0210 | .0156 |
| 15,000 | .0237 | .0203 | .0158 |
| 16,000 | .0230 | .0198 | .0163 |
| 17,000 | .0226 | .0194 | .0169 |
| 18,000 | .0226 | .0192 | .0176 |
| 19,000 | .0232 | .0193 | .0183 |
| 20,000 | .0226 | .0200 | .0190 |
| 21,000 | .0271 | .0208 | .0197 |
| 22,000 | .0300 | .0217 | .0203 |
| 23,000 | .0311 | .0227 | .0210 |
| 24,000 | .0318 | .0236 | .0216 |
| 25,000 | .0324 | .0247 | .0223 |
| 26,000 | .0331 | .0258 | .0230 |
| 27,000 | .0341 | .0274 | .0236 |
| 28,000 | .0360 | .0295 | .0245 |
| 29,000 | .0487 | .0318 | .0258 |
| 30,000 | .0550 | .0347 | .0285 |
| 31,000 | .0588 | .0384 | .0308 |
| 32,000 | .0631 | .0432 | .0321 |
| 33,000 | .0683 | .0478 | .0328 |
| 34,000 | .0758 | .0501 | .0332 |
| 35,000 | .0764 | .0503 | .0334 |
| 36,000 | .0759 | .0482 | .0333 |
| 37,000 | .0744 | .0386 | .0330 |
| 38,000 | .0707 | .0356 | .0325 |
| 39,000 | .0651 | .0337 | .0316 |
| 40,000 | .0562 | .0325 | .0300 |
| 41,000 | .0487 | .0316 | .0277 |

Wind Shear Table (Cont'd)

| Peak Wind Altitude h_{mxwd} , feet | Shear Depth | | |
|--|--|--|--|
| | 1,000 feet S_{1k} , 1/sec $\times 10^3$ | 3,000 feet S_{3k} , 1/sec $\times 10^3$ | 5,000 feet S_{5k} , 1/sec $\times 10^3$ |
| 42,000 | .0442 | .0308 | .0256 |
| 43,000 | .0407 | .0303 | .0243 |
| 44,000 | .0379 | .0299 | .0235 |
| 45,000 | .0359 | .0296 | .0228 |
| 46,000 | .0346 | .0295 | .0222 |
| 47,000 | .0338 | .0294 | .0217 |
| 48,000 | .0336 | .0292 | .0212 |
| 49,000 | .0342 | .0291 | .0207 |
| 50,000 | .0363 | .0288 | .0202 |
| 51,000 | .0397 | .0287 | .0198 |
| 52,000 | .0428 | .0286 | .0195 |
| 53,000 | .0440 | .0283 | .0191 |
| 54,000 | .0442 | .0280 | .0187 |
| 55,000 | .0432 | .0277 | .0183 |
| 56,000 | .0428 | .0272 | .0179 |
| 57,000 | .0411 | .0267 | .0175 |
| 58,000 | .0389 | .0259 | .0171 |
| 59,000 | .0362 | .0252 | .0168 |
| 60,000 | .0348 | .0243 | .0164 |
| 61,000 | .0327 | .0233 | .0160 |
| 62,000 | .0308 | .0223 | .0157 |
| 63,000 | .0291 | .0213 | .0153 |
| 64,000 | .0275 | .0203 | .0149 |
| 65,000 | .0262 | .0193 | .0146 |
| 66,000 | .0249 | .0186 | .0143 |
| 67,000 | .0239 | .0178 | .0140 |
| 68,000 | .0231 | .0172 | .0137 |
| 69,000 | .0223 | .0166 | .0134 |
| 70,000 | .0217 | .0160 | .0131 |
| 71,000 | .0213 | .0156 | .0128 |
| 72,000 | .0209 | .0152 | .0126 |

Wind Shear Table (Cont'd)

| Peak Wind Altitude h_{mxwd} , feet | <u>Shear Depth</u> | | |
|---|--|--|--|
| | 1,000 feet S_{1k} , 1/sec $\times 10^3$ | 3,000 feet S_{3k} , 1/sec $\times 10^3$ | 5,000 feet S_{5k} , 1/sec $\times 10^3$ |
| 73,000 | .0206 | .0148 | .0124 |
| 74,000 | .0205 | .0145 | .0122 |
| 75,000 | .0204 | .0142 | .0120 |
| 76,000 | .0204 | .0139 | .0118 |
| 77,000 | .0203 | .0136 | .0116 |
| 78,000 | .0202 | .0133 | .0114 |
| 79,000 | .0201 | .0131 | .0112 |
| 80,000 | .0200 | .0128 | .0110 |
| 81,000 | .0198 | .0126 | .0109 |
| 82,000 | .0197 | .0124 | .0107 |
| 83,000 | .0193 | .0122 | .0105 |
| 84,000 | .0191 | .0119 | .0103 |
| 85,000 | .0188 | .0117 | .0102 |
| 86,000 | .0185 | .0113 | .0100 |
| 87,000 | .0182 | .0110 | .0098 |
| 88,000 | .0179 | .0107 | .0096 |
| 89,000 | .0176 | .0103 | .0094 |
| 90,000 | .0173 | .0100 | .0093 |
| ∞ | .0173 | .0100 | .0093 |

3. Angles of Attack and Side Slip

The angles of attack and side slip are shown in Figure 27.

a. Still Air Angles of Attack

The still air angles of attack are functions of the component of missile velocity in the b system.

$$\vec{X}_{bb} = [D]^{-1} \vec{X}_{ee} + [\dot{D}]^{-1} \vec{X}_{ee}$$

The still air angle of attack is

$$\tilde{\alpha} = \begin{cases} 0 & \text{If } \dot{X}_{bb} = \dot{Z}_{bb} = 0 \\ \arctan (-\dot{Z}_{bb} / \dot{X}_{bb}) & \text{Otherwise} \end{cases}$$

$$\tilde{\beta} = \begin{cases} 0 & \text{If } \dot{X}_{bb} = \dot{Y}_{bb} = 0 \\ \arctan (\dot{Y}_{bb} / \dot{X}_{bb}) & \text{Otherwise} \end{cases}$$

$$\bar{\alpha}' = \begin{cases} 0 & \text{If } V_e = 0 \\ \arctan \left[\left((\dot{Z}_{bb}^2 + \dot{X}_{bb}^2)^{1/2} \right) / \dot{X}_{bb} \right] & \text{Otherwise} \end{cases}$$

$$\epsilon = \begin{cases} 0 & \text{If } \dot{Y}_{bb} = \dot{Z}_{bb} = 0 \\ \arctan (\dot{Y}_{bb} / \dot{Z}_{bb}) & \text{Otherwise} \end{cases}$$

$$\beta = \arctan \left[\dot{Y}_{bb} (\dot{X}_{bb}^2 + \dot{Z}_{bb}^2)^{-1/2} \right]$$

The vehicle velocity components with respect to the air are

$$\vec{\dot{X}}_{aee} = \vec{\dot{X}}_{ee} - \vec{\dot{X}}_{we},$$

and the total velocity is

$$V_a = (\dot{X}_{aee}^2 + \dot{Y}_{aee}^2 + \dot{Z}_{aee}^2)^{1/2}$$

b. Angles of Attack with Winds

Angles of attack are a function of missile velocity with respect to air and missile attitude. The components of missile velocity in the b-system are

$$\vec{\dot{X}}_{abb} = [D]^{-1} \vec{\dot{X}}_{aee}$$

where the matrix $[D]$ is defined in Section B.1.b

The component angles of attack (see Figure 27) are

$$\alpha = \begin{cases} \bar{\alpha} & \text{If outside atmosphere or } \dot{X}_{abb} = \dot{Z}_{abb} = 0 \\ \arctan (\dot{Z}_{abb} / \dot{X}_{abb}) & \end{cases}$$

$$\beta = \begin{cases} \bar{\beta} & \text{If outside atmosphere or } \dot{X}_{abb} = \dot{Y}_{abb} = 0 \\ \arctan (\dot{Y}_{abb} / \dot{X}_{abb}) & \end{cases}$$

$$\epsilon = \begin{cases} \bar{\epsilon} & \text{If outside atmosphere or } \dot{Y}_{abb} = \dot{Z}_{abb} = 0 \\ \arctan (\dot{Y}_{abb} / \dot{Z}_{abb}) & \end{cases}$$

with

$$-180^\circ < \alpha, \beta \leq 180^\circ$$

and the total angle of attack is

$$\alpha' = \begin{cases} \bar{\alpha} & \text{If outside atmosphere} \\ \arctan (\dot{z}_{abb}^2 + \dot{y}_{abb}^2)^{1/2} / \dot{x}_{abb} & \text{Otherwise} \end{cases}$$

The effective angles of attack used to compute the aerodynamic normal forces are given below. These values account for the reduction in the forces as the angles of attack move from ± 90 degrees to ± 180 degrees. The values are

$$\alpha_E = \begin{cases} \alpha & \text{If } -90^\circ \leq \alpha \leq 90^\circ \\ 180^\circ - \alpha & \text{If } 90^\circ < \alpha \leq 180^\circ \\ -180^\circ - \alpha & \text{If } -180^\circ < \alpha < -90^\circ \end{cases}$$

and

$$\beta_E = \begin{cases} \beta & \text{If } -90^\circ \leq \beta \leq 90^\circ \\ 180^\circ - \beta & \text{If } 90^\circ < \beta \leq 180^\circ \\ -180^\circ - \beta & \text{If } -180^\circ < \beta < -90^\circ \end{cases}$$

and

$$\alpha'_E = \begin{cases} \alpha' & \text{If } 0 \leq \alpha \leq 90^\circ \\ 180^\circ - \alpha & \text{Otherwise} \end{cases}$$

c. Time Rate Change of Angle of Attack

The time rate change of angle of attack shall be calculated if the input multiplier, $\bar{M}_\alpha \neq 0$ and the mode type $M_y = 5$.

Pitch

$$\dot{\alpha} = \begin{cases} 0 & \text{If } \dot{Z}_{abb} = \dot{X}_{abb} = 0 \\ (180/\pi)(\dot{X}_{abb}\ddot{Z}_{abb} - \dot{Z}_{abb}\ddot{X}_{abb})/(\dot{X}_{abb}^2 + \dot{Z}_{abb}^2) & \text{Otherwise} \end{cases}$$

Yaw

$$\dot{\beta} = \begin{cases} 0 & \text{If } \dot{Y}_{abb} = \dot{X}_{abb} = 0 \\ (180/\pi)(\dot{X}_{abb}\ddot{Y}_{abb} - \dot{Y}_{abb}\ddot{X}_{abb})/(\dot{X}_{abb}^2 + \dot{Y}_{abb}^2) & \text{Otherwise} \end{cases}$$

where \vec{X}_{abb} , the missile velocity components with respect to the surrounding air in the b-coordinate directions, are given in Section F. 3. a and the corresponding components of the missile acceleration are:

$$\vec{X}_{abb} = [D]^{-1} \vec{X}_{ee} + [\dot{D}]^{-1} \vec{X}_{ee} - [D]^{-1} [A_1] \vec{X}_{w11} - [D]^{-1} [\dot{A}_1] \vec{X}_{w11} - [D]^{-1} [A_1] \dot{\vec{X}}_{w11}$$

where \vec{X}_{ee} and $\dot{\vec{X}}_{ee}$ are the components of missile velocity and acceleration in a right handed Cartesian coordinate system located at the launcher; \vec{X}_{w11} and $\dot{\vec{X}}_{w11}$ are the components of wind acceleration and velocity in the local coordinate system (the 1 system; the matrix D is defined in section B. 1. b and the time derivative of the inverse is

$$[\dot{D}]^{-1} = [A_b]^{-1} [A_i]^{-1} [\dot{A}_{eo}]^{-1} + [A_b]^{-1} [A_i]^{-1} [A_{eo}]^{-1}$$

where the matrix $[A_i]$ which rotates the inertial axes coordinate components from the i-system to the eo-system is defined in section B. 1. b; the matrix $[A_{eo}]$ which rotates the inertial axes coordinate components from the eo-system to the e-system is defined in section B. 1. b and the time derivative of the inverse is

$$[\dot{A}_{eo}]^{-1} = \omega \begin{bmatrix} 0 & \sin \rho_L & 0 \\ -\sin \rho_L & 0 & -\cos \rho_L \\ 0 & \cos \rho_L & 0 \end{bmatrix} [A_{eo}]^{-1}$$

where ω is the input magnitude of the earth's angular velocity and ρ_L is the input launcher latitude.

The matrix $[A_b]$ which rotates the inertial axes coordinate components from the b-system to the i-system is defined in Section B. 1. b and the time derivative of the inverse is

$$[\dot{A}_b]^{-1} = \begin{bmatrix} 0 & +R_b & -Q_b \\ -R_b & 0 & +P_b \\ Q_b & -P_b & 0 \end{bmatrix} [A_b]^{-1}$$

where P_b , Q_b and R_b are the instantaneous vehicle angular velocities in roll, pitch, and yaw respectively.

The matrix $[A_1]$ which rotates the axes components from the 1-system to the 3-system is defined in Section F. 2. b and the time derivative is

$$[\dot{A}_1](\pi/180) = \dot{\mu}' \begin{bmatrix} 0 & \sin \rho_L & 0 \\ -\sin \rho_L & 0 & -\cos \rho_L \\ 0 & \cos \rho_L & 0 \end{bmatrix} + \dot{\rho} \begin{bmatrix} 0 & \cos \rho_L \sin \mu' & -\cos \mu' \\ -\cos \rho_L \sin \mu' & 0 & \sin \rho_L \sin \mu' \\ \cos \mu' & -\sin \rho_L \sin \mu' & 0 \end{bmatrix} [A_1]$$

where time rate change of vehicle longitude change from the launcher and vehicle latitude are

$$\dot{\mu}' = (180/\pi)(\dot{Z}_{cc} Y_{cc} - \dot{Y}_{cc} Z_{cc}) / (Y_{cc}^2 + Z_{cc}^2)$$

$$\dot{\rho} = (180/\pi)[\dot{X}_{cc}(Y_{cc}^2 + Z_{cc}^2) - \dot{Y}_{cc} X_{cc} Y_{cc} - \dot{Z}_{cc} X_{cc} Z_{cc}] / [r_c^2(Y_{cc}^2 + Z_{cc}^2)^{3/2}]$$

where \vec{X}_{cc} and $\dot{\vec{X}}_{cc}$ are the earth's geocentric coordinate system vector and time derivative respectively.

The rate change of the missile velocity components is:

$$\dot{\vec{X}}_{bb} = [D]^{-1} \dot{\vec{X}}_{ee} + [\dot{D}]^{-1} \vec{X}_{ee}$$

thus

Pitch

$$\dot{\alpha} = \begin{cases} 0 & \text{if } \dot{z}_{bb} = \dot{x}_{bb} = 0 \\ (180/\pi) (\dot{x}_{bb} \ddot{z}_{bb} - \dot{z}_{bb} \ddot{x}_{bb}) / (\dot{x}_{bb}^2 + \dot{z}_{bb}^2) \end{cases}$$

Yaw

$$\dot{\beta} = \begin{cases} 0 & \text{if } \dot{y}_{bb} = \dot{x}_{bb} = 0 \\ (180/\pi) (\dot{x}_{bb} \ddot{y}_{bb} - \dot{y}_{bb} \ddot{x}_{bb}) / (\dot{x}_{bb}^2 + \dot{y}_{bb}^2) \end{cases}$$

These are calculated only if $T_y = 10$ or 11 .

4. Mach Number and Dynamic Pressure

The Mach number is

$$M = V_a / C_a$$

and dynamic pressure is

$$q = (0.7) P_a M^2$$

G. AERODYNAMIC CHARACTERISTICS

The aerodynamic force and moments are contained here. The aerodynamic representative is applicable only to a symmetrical body about the longitudinal axis.

1. Aerodynamic Stages

There are four aerodynamic stages. All aerodynamic characteristics are input as functions of Mach number. The Mach numbers are input monotonically increasing. The following logic and comments apply to all parameters:

If $|M| \leq M_1$

where M_1 is the first input Mach number, then the coefficients are held at the first input values.

If $|M| \geq M_J$

where M_J ($J = 1, 2, \dots, 15$) is the last input Mach number, then the coefficients are held at the last input values.

a. Body Axial Force

A maximum of fifteen axial force coefficients can be input per stage. The axial force multiplier is

$$\bar{C}_k = \begin{cases} 1.0 & \text{If } \bar{C}'_k = 0 \\ \bar{C}'_k & \text{Otherwise} \end{cases}$$

The axial force during the current stage is

$$C = S_{RC} q C_A \bar{C}_k |\cos \alpha'| \cos \alpha'$$

Where S_{RC} and \bar{C}'_k are input.

The axial force coefficient for

$$M_j \leq |M| \leq M_{j+1}$$

is

$$C_A = \begin{cases} \frac{(M_j C_{A(j+1)} - M_{j+1} C_{Aj} + [C_{Aj} - C_{A(j+1)}]M)}{(M_j - M_{j+1}) + C_{BN}} & \text{if } |\alpha| \leq 90 \\ C_{CA} & \text{Otherwise} \end{cases}$$

where C_{Aj} and its corresponding Mach number M_j (not necessarily the same Mach numbers as those for the normal force) are input.

The added aerodynamic base drag coefficient due to nozzles not thrusting is

$$C_{BN} = \begin{cases} 0 & \text{if } K_{ED} = 1 \text{ or } 2 \text{ and } F_M > 0 \text{ or } F_C > 0 \\ (C_{BAM} + C_{BAC}) C_{ED} / 2.0 & \text{Otherwise} \end{cases}$$

Area coefficient for main motor

$$C_{BAM} = \begin{cases} A_{eM} / S_{RC} & \text{If } F_M = 0 \text{ and } K_{BD} \neq 1 \\ 0.0 & \text{Otherwise} \end{cases}$$

Area coefficient for complementary motor

$$C_{BAC} = \begin{cases} A_{eC} / S_{RC} & \text{If } F_C = 0 \text{ and } K_{BD} \neq 2 \\ 0.0 & \text{Otherwise} \end{cases}$$

Generalized base drag coefficient

$$C_{BD} = \begin{cases} 0.79996568 + 0.28892727 |M| - 10.60569 M^2 + 105.77183 |M|^3 \\ -486.47910 M^4 + 943.6044 |M|^5 - 647.72025 M^6 & \text{if } |M| < 0.5 \\ 3.4709 - 26.428046 |M| + 102.16591 M^2 - 213.47669 |M|^3 \\ +247.78677 M^4 - 150.51554 |M|^5 + 37.510830 M^6 & \text{if } 0.5 \leq |M| < 1.0 \\ 41.875203 - 153.36892 |M| + 238.07985 M^2 - 198.19504 |M|^3 \\ + 92.924624 M^4 - 23.211652 |M|^5 + 2.4099132 M^6 & \text{if } 1.0 \leq |M| < 2.0 \\ 0.34063761 - 0.95438446 |M| - 0.01990222 M^2 + 0.15989115 |M|^3 \\ -0.0034737133 M^4 + 0.00033548493 |M|^5 - 0.000012362510 M^6 & \text{if } 2.0 \leq |M| < 7.0 \\ 0.007 - 0.007 |M| & \text{if } 7.0 \leq |M| < 10.0 \\ 0.0 & \text{if } 10.0 \leq |M| \end{cases}$$

The drag coefficient at 180° angle of attack

$$C_{CA} = \begin{cases} 0.85 + 0.02076766 |M| & \text{if } |M| < 0.60 \\ 1.7337905 - 2.8023463 |M| + 2.2502164 M^2 & \text{if } 0.60 \leq |M| < 1.00 \\ -1.8550591 + 5.1110871 |M| - 2.4796399 M^2 \\ + 0.40418455 |M|^3 & \text{if } 1.00 \leq |M| < 2.14 \\ 1.688 & \text{if } 2.14 \leq |M| \end{cases}$$

where A_{eM} and A_{eC} are the input nozzle exit areas for the main motor and complementary motor, respectively, F_M and F_C are the delivered thrusts of the main motor and complementary motor respectively, S_{RC} is the input aerodynamic axial force coefficient reference, M is the Mach number, and K_{BD} is the input base drag suppression flag input in Lk108.

b. Body Normal Forces Due to Angles of Attack

A maximum of fifteen normal force coefficients can be input per stage.

The normal force multiplier is

$$\bar{N}_k = \begin{cases} 1.0 & \text{if } \bar{N}_k' = 0 \\ \bar{N}_k' & \text{otherwise} \end{cases}$$

The normal force for the current stage is:

$$N_Y = S_{RNG} C_N \bar{N} \sin \epsilon$$

$$N_Z = S_{RNG} C_N \bar{N} \cos \epsilon$$

where ϵ is the bank angle.

where S_{RN} is input and C_N is defined as follows

$$C_N = \begin{cases} C_{N1} \alpha'_E + C_{N2} \alpha'_E |\alpha'_E| + C_{N3} \alpha_E^3 & \text{if } S_{PF} = 0 \\ \frac{C_{N1} \alpha'_E + [(S_{PF}/S_{RN})C_{CN} - (180/\pi)(\pi/2)C_{N1}] \sin \alpha'_E}{|\sin \alpha'_E|} & \text{Otherwise} \end{cases}$$

The coefficients for

$$M_j \leq |M| \leq M_{j+1}$$

are

$$C_{N1} = (M_j C_{N1(j+1)} - M_{j+1} C_{N1j} + [C_{N1j} - C_{N1(j+1)}]M) / (M_j - M_{j+1})$$

$$C_{N2} = (M_j C_{N2(j+1)} - M_{j+1} C_{N2j} + [C_{N2j} - C_{N2(j+1)}]M) / (M_j - M_{j+1})$$

$$C_{N3} = (M_j C_{N3(j+1)} - M_{j+1} C_{N3j} + [C_{N3j} - C_{N3(j+1)}]M) / (M_j - M_{j+1})$$

where C_{N1j} , C_{N2j} , and C_{N3j} and their corresponding Mach number M_j ($j = 1, 2, \dots, 15$) are input.

The following logic apply:

If $C_{N21} = C_{N22} = 0$, then

$$C_{N2} = 0 \text{ for all } M$$

and if $C_{N31} = C_{N32} = 0$, then

$$C_{N3} = 0 \text{ for all } M$$

where C_{N21} , C_{N22} , C_{N31} , and C_{N32} are input.

where the normal force coefficient at 90° angle of attack

$$C_{CN} = \begin{cases} 0.84584966 + 0.32629796 |M| - 3.1030112 |M|^2 + 11.086155 |M|^3 \\ \quad - 16.513306 |M|^4 + 9.3484993 |M|^5 \text{ if } |M| < 0.9 \\ -628.76609 + 2,827.6544 |M| - 5,035.6157 |M|^2 + 4,584.0631 |M|^3 \\ \quad - 2,070.4406 |M|^4 + 374.70503 |M|^5 \text{ if } 0.9 < |M| < 1.2 \\ 4.3744073 - 5.5002559 |M| + 4.1332796 |M|^2 - 1.6453339 |M|^3 \\ \quad + 0.33668120 |M|^4 - 0.026740990 |M|^5 \text{ if } 1.2 \leq |M| < 2.2 \\ 1.268 \quad \text{if } |M| \geq 2.2 \end{cases}$$

c. Aerodynamic Normal Force Due to Damping

The transverse force, positive down or to the left, attributable to the vehicle pitching and yawing and to rate change of angle of attack is:

$$N_{Py} = \begin{cases} 0 & \text{if } V_a = 0 \\ q S_{RN} C_{N1} \ell_{cp} (\bar{M}_Q R_b + \bar{M}_\alpha \dot{\beta}) / (2V_a) \end{cases}$$

$$N_{Pz} = \begin{cases} 0 & \text{if } V_a = 0 \\ q S_{RN} C_{N1} \ell_{cp} (\bar{M}_Q Q_b + \bar{M}_\alpha \dot{\alpha}) / (2V_a) \end{cases}$$

where V_a is the missile velocity with respect to the air, Q_b and R_b are the missile angular pitch and yaw rates respectively, $\dot{\alpha}$ and $\dot{\beta}$ are the angular angle of attack rate in pitch and yaw respectively, q is the dynamic pressure ℓ_{cp} is the center of gravity to center of pressure distance, C_{N1} is the linear normal force coefficient, and S_{RN} , \bar{M}_Q and \bar{M}_α are input.

d. Aerodynamic Fin Force Coefficient

A maximum of fifteen aerodynamic pitch movable fin linear fin lift coefficients, C_{Lz} , nonlinear fin lift coefficients, C_{lz} , drag coefficient, C_{Dz} , and drag due to lift factor, K_{Lz} can be input per stage.

the coefficient for

$$M_j \leq |M| \leq M_{(j+1)}$$

let

$$K_{int} = \frac{M_{(j+1)} - M}{M_{(j+1)} - M_j} \quad \text{and linearly interpolate}$$

$$C_{Lz} = \bar{C}_{Lz} [K_{int} C_{Lz(j+1)} + (1 - K_{int}) C_{Lzj}]$$

$$C_{lz} = \bar{C}_{lz} [K_{int} C_{lz(j+1)} + (1 - K_{int}) C_{lzj}]$$

$$C_{Dz} = \bar{C}_{Dz} [K_{int} C_{Dz(j+1)} + (1 - K_{int}) C_{Dzj}]$$

$$K_{Lz} = \bar{K}_{Lz} [K_{int} K_{Lz(j+1)} + (1 - K_{int}) K_{Lzj}]$$

where C_{Lzj} , C_{lzj} , C_{Dzj} , and K_{Lzj} and their corresponding Mach numbers M_j ($j = 1, 2, \dots, 15$) are input in the same table with the pitch aerodynamic control fin center of pressure data.

First and last input logic for the aerodynamic pitch movable fin force coefficients are

$$\begin{aligned}
 C_{Lz} &= \begin{cases} \bar{C}_{Lz} C_{Lz1} & \text{if } |M| < M_1 \\ \bar{C}_{Lz} C_{LzJ} & \text{if } |M| > M_J \end{cases} \\
 C_{1z} &= \begin{cases} \bar{C}_{1z} C_{1z1} & \text{if } |M| < M_1 \\ \bar{C}_{1z} C_{1zJ} & \text{if } |M| > M_J \end{cases} \\
 C_{Dz} &= \begin{cases} \bar{C}_{Dz} C_{Dz1} & \text{if } |M| < M_1 \\ \bar{C}_{Dz} C_{DzJ} & \text{if } |M| > M_J \end{cases} \\
 K_{Lz} &= \begin{cases} \bar{K}_{Lz} K_{Lz1} & \text{if } |M| < M_1 \\ \bar{K}_{Lz} K_{LzJ} & \text{if } |M| > M_J \end{cases}
 \end{aligned}$$

where the subscript 1 refers to the first table input coefficient and the subscript J refers to the last table entry.

The coefficients multipliers

$$\begin{aligned}
 \bar{C}_{Lz} &= \begin{cases} 1.0 & \text{if } \bar{C}_{Lz}' = 0 \\ \bar{C}_{Lz}' & \text{otherwise} \end{cases} \\
 \bar{C}_{1z} &= \begin{cases} 1.0 & \text{if } \bar{C}_{1z}' = 0 \\ \bar{C}_{1z}' & \text{otherwise} \end{cases} \\
 \bar{C}_{Dz} &= \begin{cases} 1.0 & \text{if } \bar{C}_{Dz}' = 0 \\ \bar{C}_{Dz}' & \text{otherwise} \end{cases} \\
 \bar{K}_{Lz} &= \begin{cases} 1.0 & \text{if } \bar{K}_{Lz}' = 0 \\ \bar{K}_{Lz}' & \text{otherwise} \end{cases}
 \end{aligned}$$

where \bar{C}_{Lz}' , \bar{C}_{1z}' , \bar{C}_{Dz}' , and \bar{K}_{Lz}' are input

e. Aerodynamic Fin Forces

Fin angle of Attack

$$\alpha_{cf} = \alpha_E - K_{cf} \delta_P$$

$$\alpha_{cf1} = \alpha_{cf} + \delta_R + \delta_{MR} - \alpha_{he}$$

$$\alpha_{cf2} = \alpha_{cf} - \delta_R - \delta_{MR} - \alpha_{he}$$

$$\beta_{cf} = \beta_E - K_{cf} \delta_Y$$

$$\beta_{cf1} = \beta_{cf} + \delta_R + \delta_{MR} + \alpha_{he}$$

$$\beta_{cf2} = \beta_{cf} - \delta_R - \delta_{MR} - \alpha_{he}$$

where the Helix Angle of attack is: $\alpha_{he} = \arctan \{ [P_b (\pi/180) (\ell_{br}) / [V_e]] \}$

where the lift coefficient is:

$$\hat{C}_{Lz1} = C_{LZ} \alpha_{cf1} + C_{1Z} \alpha_{cf1} |\alpha_{cf1}|$$

$$\hat{C}_{Lz2} = C_{LZ} \alpha_{cf2} + C_{1Z} \alpha_{cf2} |\alpha_{cf2}|$$

$$\hat{C}_{Lz} = (\hat{C}_{Lz1} + \hat{C}_{Lz2})/2$$

$$\hat{C}_{Ly1} = C_{LZ} \beta_{cf1} + C_{1Z} \beta_{cf1} |\beta_{cf1}|$$

$$\hat{C}_{Ly2} = C_{LZ} \beta_{cf2} + C_{1Z} \beta_{cf2} |\beta_{cf2}|$$

$$\hat{C}_{Ly} = (\hat{C}_{Ly1} + \hat{C}_{Ly2})/2$$

the drag coefficient is:

$$\hat{C}_{DZ1} = C_{DZ} + K_{LZ} \hat{C}_{Lz1}^2$$

$$\hat{C}_{DZ2} = C_{DZ} + K_{LZ} \hat{C}_{Lz2}^2$$

$$\hat{C}_{DZ} = (\hat{C}_{DZ1} + \hat{C}_{DZ2})/2.0$$

$$\hat{C}_{Dy1} = C_{DZ} + K_{LZ} \hat{C}_{Ly1}^2$$

$$\hat{C}_{Dy2} = C_{DZ} + K_{LZ} \hat{C}_{Ly2}^2$$

$$\hat{C}_{Dy} = (\hat{C}_{Dy1} + \hat{C}_{Dy2})/2.0$$

Normal Force

Pitch

$$N_{\delta z} = -S_{Fz} q (\hat{C}_{Lz} \cos \alpha_E + \hat{C}_{Dz} \sin \alpha_E)$$

Yaw

$$N_{\delta y} = -S_{Fz} q (\hat{C}_{Ly} \cos \beta_E + \hat{C}_{Dy} \sin \beta_E)$$

Drag

$$C_{\delta z} = S_{Fz} q (\hat{C}_{Dz} \cos \alpha_E + \hat{C}_{Dy} \cos \beta_E - \hat{C}_{Lz} \sin \alpha_E - \hat{C}_{Ly} \sin \beta_E)$$

2. Aerodynamic Moments

a. Body Center of Pressure

A maximum of fifteen total center of pressure body stations can be input.

The center of pressure location for

$$M_j < M \leq M_{j+1}$$

is

$$x_{cp} = \begin{cases} \bar{x}_{cp} & \text{if } x_{pc} = 0 \\ x_{pc} (\sin \alpha)^2 + \bar{x}_{cp} (\cos \alpha)^2 & \text{if } |\alpha| \leq 90^\circ \text{ \& } x_{pc} \neq 0 \\ x_{pc} (\sin \alpha)^2 + (0.8 x_e + 0.2 x_{pc}) (\cos \alpha)^2 & \text{if } |\alpha| > 90^\circ \text{ \& } x_{pc} \neq 0 \end{cases}$$

where x_{pc} is the input plan form area centroid body station, x_e is the nozzle exit body station, and α is the angle of attack.

$$\text{where } \bar{x}_{cp} = \frac{\bar{x}_{cp} (M_j x_{cp(j+1)} - M_{j+1} x_{cpj}) + [x_{cpj} - x_{cp(j+1)}] M}{M_j - M_{j+1}}$$

where x_{cpj} and M_j ($j = 1, 2, \dots, 15$) and \bar{x}_{cp} are input.

$$\bar{x}_{cp} = \begin{cases} \bar{x}_{cp} & \text{If } \bar{x}_{cp} = 0 \\ 1.0 & \text{Otherwise} \end{cases}$$

The center of pressure and normal force coefficient values are input in the same table. The Mach numbers are input monotonically increasing so the $M_1 < M_2 \dots$

First and last input logic for the center of pressure is

$$\bar{x}_{cp} = \begin{cases} \bar{x}_{cp} x_{cpl} & \text{If } M < M_1 \\ \bar{x}_{cp} x_{cpJ} & \text{If } M > M_J \end{cases}$$

where the x_{cpl} and M_1 and the x_{cpJ} and M_J ($J = 1, 2, \dots, \text{or } 15$) are the first and last input values, respectively.

b. Pitching and Yawing Damping Coefficients

The aerodynamic pitch damping moment coefficients are

$$C_{MQ} = \begin{cases} 0 & \text{if } D_{AN} = 0 \\ \hat{C}_{MQ} + K_Q (2C_{N1}/D_{RN}^2) [2x_{cp}(x_{RQ} - x_{cg}) - x_{cg}^2 + x_{RQ}^2] & \text{otherwise} \end{cases}$$

$$C_{M\dot{r}} = \begin{cases} 0 & \text{if } D_{RN} = 0 \\ \hat{C}_{M\dot{r}} + K_{\dot{r}} (D_{RN}^2) [2x_{cp}(x_{R\dot{r}} - x_{cg}) - x_{cg}^2 + x_{R\dot{r}}^2] & \text{otherwise} \end{cases}$$

where C_{MQ} and $\hat{C}_{M\dot{r}}$ are the unadjusted aerodynamic pitch damping moment coefficients, C_{N1} is the linear normal force coefficient, x_{cp} is the aerodynamic center of pressure body station, x_{cg} is the vehicle center of gravity body station, x_{RQ} and $x_{R\dot{r}}$ are the reference aerodynamic pitch damping moment body stations, and K_Q , $K_{\dot{r}}$, D_{RN} are input.

Reference Pitch Damping Body Stations

The reference aerodynamic pitch damping moment body stations are

$$x_{RQ} = \bar{\lambda}_{cp} x_{RQ}^i$$

$$x_{R\dot{r}} = \bar{\lambda}_{cp} x_{R\dot{r}}^i$$

where x_{RQ}^i and $x_{R\dot{r}}^i$ are input

c.

Unadjusted Aerodynamic Pitch Damping Moment Coefficient

A maximum of ten total unadjusted aerodynamic pitch damping moment coefficients can be input.

The coefficients for $M_j \leq |M| \leq M_{j+1}$ are

$$\hat{C}_{MQ} = M_j C_{MQ(j+1)} - M_{j+1} C_{MQj} + [C_{MQj} - C_{MQ(j+1)}] / (M_j - M_{j+1})$$

$$\hat{C}_{M\dot{\alpha}} = M_j C_{M\dot{\alpha}(j+1)} - M_{j+1} C_{M\dot{\alpha}j} + [C_{M\dot{\alpha}j} - C_{M\dot{\alpha}(j+1)}] / (M_j - M_{j+1})$$

The unadjusted aerodynamic pitch damping moments coefficient for pitch rate and angle of attack rate are input in the same table. The Mach numbers are input monotonically increasing so that $M_1 < M_2 \dots$

First and last input logic for the unadjusted aerodynamic pitch damping moment coefficients are

$$\hat{C}_{MQ} = \begin{cases} C_{MQ1} & \text{if } |M| < M_1 \\ C_{MQJ} & \text{if } |M| < M_J \end{cases}$$

$$\hat{C}_{M\dot{\alpha}} = \begin{cases} C_{M\dot{\alpha}1} & \text{if } |M| < M_1 \\ C_{M\dot{\alpha}J} & \text{if } |M| > M_J \end{cases}$$

where the C_{MQ1} , $C_{M\dot{\alpha}1}$, and M_1 and the C_{MQJ} , $C_{M\dot{\alpha}J}$, and M_J ($J = 1, 2, \dots, \text{or } 15$) are the first and last input values respectively.

d. Aerodynamic Control Fin Center of Pressure

A maximum of fifteen pitch aerodynamic control fin center of pressure ratio of the input pitch fin base root length can be input.

The pitch aerodynamic control fin center of pressure location for

$$M_j \geq |M| \geq M_{j+1}$$

is

$$U_{cz} = \frac{[M_j U_{cz(j+1)} - M_{(j+1)} U_{czj} - U_{cz(j+1)} |M|]}{(M_j - M_{(j+1)})}$$

where U_{czj} and M_j ($j = 1, 2, \dots, 15$) are input

The pitch aerodynamic control fin center of pressure, and force coefficients are input in the same table. The Mach numbers are input monotonically increasing so that $M_1 < M_2 \dots$

First and last input logic for the aerodynamic control surface center of pressure is

$$U_{cz} = \begin{cases} U_{cz1} & \text{if } |M| < M_1 \\ U_{czJ} & \text{if } |M| > M_J \end{cases}$$

where the U_{cz1} and the U_{czJ} and M_J ($J = 1, 2, \dots, \text{or } 15$) are the first and last input values, respectively.

e. Aerodynamic Disturbing Pitch and Yaw Moments

The moments due to the aerodynamic normal forces are:

$$M_{CZG} = C \quad z_{cg}$$

$$M_{NSQ} = N_Z \quad l_{cp}$$

$$M_{NDQ} = \begin{cases} 0 & \text{If } V_a = 0 \\ [q \quad S_{RN} \quad D_{RN}^2 / (2V_a)] [\bar{M}_Q C_{MQ} Q_b + \bar{M}_\alpha C_{M\dot{\alpha}} \dot{\alpha}] \end{cases}$$

$$M_{NQ} = M_{CZG} + M_{NSQ} + M_{NDQ}$$

$$M_{CYG} = -C \quad y_{cg}$$

$$M_{NSR} = -N_y \quad l_{cp}$$

$$M_{NDR} = \begin{cases} 0 & \text{If } V_a = 0 \\ [q \quad S_{RN} \quad D_{RN}^2 / (2V_a)] [\bar{M}_Q C_{NR} R_b + \bar{M}_\alpha C_{M\dot{\alpha}} \dot{\beta}] \end{cases}$$

$$M_{NR} = M_{CYG} + M_{NSR} + M_{NDR}$$

$$\bar{M}_Q = \begin{cases} \bar{M}_Q' & \text{If } \bar{M}_Q' \neq 0 \\ 1.0 & \text{Otherwise} \end{cases}$$

$$\bar{M}_\alpha = \begin{cases} \bar{M}_\alpha' & \text{If } \bar{M}_\alpha' \neq 0 \\ 1.0 & \text{Otherwise} \end{cases}$$

$$M_{NP} = N_z \quad y_{cg} - N_y \quad z_{cg}$$

where N_x and N_z are the aerodynamic static normal forces, l_{cp} is the center of pressure lever arm, q is the dynamic pressure, V_a is the missile velocity with respect to the air, C_{MQ} and $C_{M\dot{\alpha}}$ are the aerodynamic pitch damping moment derivative, Q_b and R_b are the missile angular pitch and yaw rates respectively, $\dot{\alpha}$ and $\dot{\beta}$ are the angular angle of attack rates, and S_{RN} , D_{RN} , \bar{M}_Q' and \bar{M}_α' are the input.

f. Disturbing Aerodynamic Rolling Moment

An aerodynamic rolling moment may occur when the missile is not a body of revolution. The equations given below are developed considering raceways, but can be applied to other protuberances as well. Two raceways for each stage can be defined. Their locations (see Figure 19) and reference areas are specified by input. The aerodynamic characteristics of both raceways are specified by a single set of normal force coefficients. A maximum of 10 normal force coefficients versus Mach number can be input for each stage.

If the input roll force reference area, S_{RR1} , is zero for the current stage or there is no atmosphere, then the rolling moment equations are ignored. Otherwise, the rolling moment is:

$$M_{RAP} = (\gamma_a/2) P_a (|M_{R1}| M_{P1} C_{RR1} S_{RR1} r_{R1} + |M_{R2}| M_{P2} C_{RR2} S_{RR2} r_{R2})$$

where the reference areas, S_{RRi} , and the center of pressure radial locations from the missile centerline, r_{Ri} ($i = 1, 2$), are input and the other parameters are computed as follows:

The Mach number due to the velocity normal to the i -th raceway is:

$$M_{Ri} = (-Z_{abb} \sin \phi_{Ri} - \dot{Y}_{abb} \cos \phi_{Ri}) / C_a$$

where the bank angles of the raceways, ϕ_{Ri} , are input.

The instantaneous normal force coefficient for $M_j \leq |M_{Ri}| \leq M_{j+1}$ is:

$$C_{RR} = [M_j C_{RR(j+1)} - M_{j+1} C_{RRj} + (C_{RRj} - C_{RR(j+1)}) |M_{Ri}|] / (M_j - M_{j+1})$$

where C_{RRj} ($j = 1, 2, \dots, 10$) and its corresponding Mach number, M_j (not necessarily the same as in the above sections), are input.

g. Pitch, Yaw and Roll Control Moments

The pitching moment due to the aerodynamic control force is:

$$M_{\delta Q} = N_{\delta z} \cdot l_{\delta z}$$

where $N_{\delta z}$ is the pitch fin normal force and $l_{\delta z}$ is the pitch movable control fin center of pressure to center of gravity distance.

The yawing moment due to the aerodynamic control force is:

$$M_{\delta R} = N_{\delta y} \cdot l_{\delta y}$$

where $N_{\delta y}$ is the yaw fin normal force and $l_{\delta y}$ is the yaw movable control fin center of pressure to center of gravity distance.

The rolling moment due to the aerodynamic control force is:

$$M_{\delta P} = \frac{l_{\delta r} S_{Fz} q}{2.0} [(\hat{C}_{Lz1} - \hat{C}_{Lz2}) \cos \alpha_E + (\hat{C}_{Dz1} - \hat{C}_{Dz2}) \sin \alpha_E \\ + (\hat{C}_{Ly1} - \hat{C}_{Ly2}) \cos \beta_E + (\hat{C}_{Dy1} - \hat{C}_{Dy2}) \sin \beta_E]$$

where $l_{\delta r}$ is the fin radial center of pressure to missile centerline, S_{Fz} is the input fin reference area, q is the dynamic pressure, α_E is the effective angle of attack, β_E is the effective side slip angle, \hat{C}_{Lz1} and \hat{C}_{Lz2} are the pitch fin lift coefficients, \hat{C}_{Ly1} and \hat{C}_{Ly2} are the yaw fin lift coefficient, \hat{C}_{Dz1} and \hat{C}_{Dz2} are the pitch fin drag coefficient and \hat{C}_{Dy1} and \hat{C}_{Dy2} are the yaw fin drag coefficients.

The torque about the pitch fin hinge axis is:

$$M_{hz} = S_{fz} q \hat{C}_{Lz} \cdot l_{hz}$$

where l_{hz} is the pitch movable control fin center of pressure to hinge axis distance

$$M_{hy} = S_{Fz} q \hat{C}_{Ly} \cdot l_{hz}$$

where l_{hy} is the yaw movable control fin center of pressure to hinge axis location.

H. MISSILE THRUST AND WEIGHT

1. THRUST-WEIGHT STAGES

There are four thrust-weight stages. Missile thrust is computed either from input vacuum thrust, nozzle exit area, and atmospheric pressure or from internal ballistics. Instantaneous weight is a function of input stage weight, weight flow, and propellant vacuum specific impulse. There are two thrust-weight tables for each stage: the main and complementary thrust-weight tables. These two tables allow the capability of simulating the simultaneous operation of motors having different characteristics or they can be used in sequence. Twenty-five data points can be input in each table. Under the internal ballistics option, the input main thrust-weight table is replaced by a thrust vs time, a pressure vs time or a burning area vs web table.

Total axially directed thrust, F , is computed from main thrust, F_M , and complementary thrust, F_C , as follows:

$$F = F_M + F_C$$

a. Noninternal Ballistics Evaluation of Main Thrust Weight Table--The main thrust-weight table consists of the following inputs: stage termination control parameters, σ_s , k_g ; total vacuum impulse quantities, I_{VT} , I_{VM} ; main stage weight, W_{MO} ; thrust, weight flow and time perturbation factors, K_{FM} , K_{WM} , K_{tM} ; specific impulse, I_{spM} ; nozzle exit area, A_{eM} ; weight carryover flag, K_O ; nozzle separated flow parameters, ϵ_d , γ_d , C_d , α_d , a_s , c_s , and a maximum of 25, $j = 1, 2, \dots, 25$, monotonically increasing main thrust weight switching times, $t_M(j)$, with corresponding vacuum thrust, $F_{M(j)}$, and weight flow, $\dot{W}_{M(j)}$.

An adjusted main thrust-weight table of 6 parameters and a maximum of 25 rows is generated as follows:

(1) Adjusted time switching points

$$t_{M(j)} = K_{tM} t_{M(j)}$$

(2) Adjusted vacuum thrust points

$$F_{M(j)} = K_{FM} F_{M(j)}$$

(3) Adjusted total main weight flow points

$$W_{M(j)} = \begin{cases} 0 & \text{if } \hat{t}_{M(j+1)} = \hat{t}_{Mj} \text{ or } j = J \text{ and } W'_{MO} < 0 \\ (W_{Mj} - W_{M(j+1)}) / t_{M(j+1)} - \hat{t}_{Mj} & \text{if } \hat{t}_{M(j+1)} \neq \hat{t}_{Mj} \text{ and } j \neq J \text{ and } W'_{MO} < 0 \\ K_{WM} W_{M(j)} & \text{if } I_{spM} = 0 \text{ and } W'_{MO} \geq 0 \\ K_{WM} W_{M(j)} + \hat{F}_{M(j)} / I_{spM} & \text{Otherwise} \end{cases}$$

(4) Adjusted time rate change of vacuum thrust points

$$\hat{F}_{M(j)} = \begin{cases} 0 & \text{if } \hat{t}_{M(j)} \geq t_{M(j+1)} \\ [\hat{F}_{M(j+1)} - \hat{F}_{M(j)}] / [\hat{t}_{M(j+1)} - \hat{t}_{M(j)}] & \text{Otherwise} \end{cases}$$

(5) Adjusted time rate change of weight flow points

$$\hat{W}_{M(j)} = \begin{cases} 0 & \text{if } \hat{t}_{M(j)} \geq t_{M(j+1)} \text{ or } W'_{MO} < 0 \\ [\hat{W}_{M(j+1)} - \hat{W}_{M(j)}] / [\hat{t}_{M(j+1)} - \hat{t}_{M(j)}] & \text{Otherwise} \end{cases}$$

(6) Adjusted main table expended weight points

$$\hat{W}_{M(j)} = \begin{cases} 0 & \text{if } j = 1 \\ W_{M2} - W_{Mj} & \text{if } W'_{MO} < 0 \\ \sum_{i=1}^j 0.5 [\hat{W}_{M(i)} + \hat{W}_{M(i-1)}] [\hat{t}_{M(i)} - \hat{t}_{M(i-1)}] & \text{Otherwise} \end{cases}$$

Weight, weight flow and thrust are evaluated as:

weight expended for main motor

$$W_M = \hat{W}_{M(j)} + \dot{\hat{W}}_{M(j)} \Delta t_M + 0.5 \ddot{\hat{W}}_{M(j)} \Delta t_M^2$$

weight flow rate

$$\dot{W}_M = \dot{\hat{W}}_{M(j)} + \ddot{\hat{W}}_{M(j)} \Delta t_M$$

vacuum thrust

$$F_{Mv} = \hat{F}_{M(j)} + \dot{\hat{F}}_{M(j)} \Delta t_M$$

where j is such that

$$\hat{t}_{M(j)} \leq t_B \leq \hat{t}_{M(j+1)}$$

and

$$\Delta t_M = t_B - \hat{t}_{M(j)}$$

b. Noninternal Ballistics Evaluation of Motor Chamber Pressure and Nozzle

Vacuum Pressure Ratio--If the input propellant diameter (D_p) is less than or equal to zero and the nozzle expansion ratio ϵ_d is greater than 1.0, the following logic is used to establish the motor chamber pressure (P_c) and the nozzle vacuum pressure ratio (P_c/P_e).

Nozzle half angle momentum correction coefficient

$$\lambda_d = (1 + \cos \alpha_d)/2.$$

Nozzle half angle

$$\alpha_d = \begin{cases} 15^\circ & \text{if } \alpha'_d = 0 \\ \alpha'_d & \text{Otherwise} \end{cases}$$

Where α'_d is the input nozzle half angle.

Optimum thrust coefficient ($P_c = P_d$)

$$C_{FO} = \Omega_d [1 - (P_c/P_e)^{-\Gamma_d}]^{\frac{1}{2}}$$

Chamber pressure

$$P_c = F_{Mv} \epsilon_d / \left\{ \left[C_D \lambda_d C_{FO} + \epsilon_d / (P_c/P_e) \right] \Lambda_{em} \times 144. \right\}$$

Nozzle efficiency coefficient

$$C_D = \begin{cases} 0.96 & \text{If } C'_D = 0 \\ C'_D & \text{Otherwise} \end{cases}$$

Where C'_D is the input nozzle efficiency coefficient

Ratio of specific heats functional constants

$$\Gamma_d = (\gamma_d - 1)/\gamma_d$$

$$\Xi_d = [(\gamma_d - 1)/(\gamma_d + 1)]^{\frac{1}{2}} [2/(\gamma_d + 1)]^{1/2} [1/(\gamma_d - 1)]$$

$$\Omega_d = \gamma_d [2/(\gamma_d - 1)]^{\frac{1}{2}} [2/(\gamma_d + 1)]^{1/2} [(\gamma_d + 1)/[2(\gamma_d - 1)]]$$

$$\gamma_d = \begin{cases} 1.18 & \text{if } \gamma'_d = 0 \\ \gamma'_d & \text{Otherwise} \end{cases}$$

Where γ'_d is the input exhaust gas ratio of specific heats.

Nozzle expansion ratio

$$\epsilon = \epsilon_d$$

Pressure ratio

Solve for (P_c/P_e) by Newton-Raphson iteration method

$$\epsilon_d = \Xi_d (P_c/P_e)^{(1/\gamma_d)} [1 - (P_c/P_e)^{-\Gamma_d}]^{-\frac{1}{\gamma_d}}$$

$$\text{Let } [P_c/P_e]_{(n)} = R_{(n)}$$

$$R_o = (0.3953 + 2.78 \gamma_d) \epsilon_d (0.28563 + 0.8631 \gamma_d)$$

Algorithm

$$R_{(n+1)} = R_{(n)} - F[R_{(n)}] / F'[R_{(n)}] \quad n = 0, 1, 2, \dots$$

Where

$$F[R_{(n)}] = \Xi_d (R_{(n)})^{(1/\gamma_d)} \{ 1 - [R_{(n)}]^{-\Gamma_d} \}^{-\frac{1}{\gamma_d}} - \epsilon_d$$

$$F'[R_{(n)}] = \Xi_d (1/\gamma_d) [R_{(n)}]^{-\Gamma_d} \{ 1 - [R_{(n)}]^{-\Gamma_d} \}^{-\frac{1}{\gamma_d}} \\ - (1/2) \Xi_d \Gamma_d [R_{(n)}]^{-(2/\gamma_d)} \{ 1 - [R_{(n)}]^{-\Gamma_d} \}^{-3/2}$$

Terminate iteration if

$$F[R_{(n)}] / \epsilon_d < 0.000001$$

Then set

$$(P_c/P_e) = R_{(n)}$$

Where ϵ_d input nozzle expansion ratio

c. Internal Ballistic Evaluation of Main Thrust Weight Table--If the input propellant diameter (D_p) is greater than zero, the following equations and logic are used to simulate the operation of a single chamber controllable motor.

| <u>L-Number</u> | <u>Symbol</u> | <u>Definition</u> | <u>Default</u> |
|-----------------|---------------|--|----------------|
| L-k001 | D_p | Diameter of propellant, in. | 0.0 |
| L-k002 | r'_{b1000} | Burning rate of propellant at 1000 lb/sq in. chamber pressure and flag to determine evaluation option, in./sec | 0.0 |
| K-k013 | ϵ_d | Nozzle expansion ratio, dim | 0.0 |
| L-k014 | γ_d | Ratio of specific heats of the rocket motor exhaust gases, dim | 1.18 |
| L-k015 | C_D | Nozzle efficiency coefficient, dim | 0.96 |
| K-k016 | α_d | Nozzle effective half angle, deg | 15 |
| L-k095 | ρ_p | Density of propellant, lb/cu in. | 0.065 |
| L-k096 | τ_w | Web fraction, dim | 0.8 |
| L-k097 | n | Burn rate exponent, dim | 0.6 |
| L-k098 | α_p | Propellant diffusivity, sq in./sec | 0.00027 |
| L-k099 | P_{max} | Maximum allowable chamber pressure, lb/sq in. | 0.0 |
| L-k407 | ω_{PC} | Pressure control frequency, rad/sec | 0.0 |

The following logic will initialize the following tables depending on the input options: (a) Vacuum Thrust-Time Table, i.e., if $r'_{b1000} = 0$, (b) Chamber Pressure-Time, i.e., if $r'_{b1000} < 0$, (c) Surface Area-Web Depth Fraction, i.e., if $r'_{b1000} > 0$.

| | | |
|---|----------------|--|
| 1 | \hat{t}_{Mj} | Time, sec |
| 2 | \hat{F}_{Mj} | Vacuum thrust, lb |
| 3 | P_{cj} | Chamber pressure, lb/sq in. |
| 4 | \dot{P}_{cj} | Time change of chamber pressure, lb/sq in.-sec |
| 5 | g_{wj} | Web depth fraction, dim |
| 6 | V_{cj} | Chamber volume, cu in. |

- 7 ξ_{pj} Expended propellant fraction, dim
 8 A_{Sj} Surface area, sq in.
 9 A_x Throat extinguishment area, sq in.

In addition to these tabular values, the following constants are also calculated:

C^* , A_{tref} , r_{b1000} , f_{wt} , W_p , I_{TM} , a , C_{AS1} , C_{AS2} and C_{AS3}

A_{xmax} , A_{xmin} , P_{cmxa} and \bar{P}_{cref}

Thrust coefficient route (dim)

$$C_f = f(\gamma_d, \epsilon_d, \alpha_d, C_d)$$

Ratio of specific heats functional constants

$$\Gamma_d = (\gamma_d - 1)/\gamma_d$$

$$\Xi_d = \left[(\gamma_d - 1)/(\gamma_d + 1) \right]^{1/2} \left[2/(\gamma_d + 1) \right] \left[1/\gamma_d - 1 \right]$$

$$\Omega_d = \gamma_d \left[2/(\gamma_d - 1) \right]^{1/2} \left[2/(\gamma_d + 1) \right] \left\{ (\gamma_d + 1)/[2\gamma_d - 1] \right\}$$

Pressure ratio

Solve for (P_c/P_e) by Newton-Raphson iteration method

$$\epsilon_d = \Xi_d (P_c/P_e)^{(1/\gamma_d)} \left[1 - (P_c/P_e) - \Gamma_d \right]^{-1/2}$$

$$\text{let } \left[\frac{P_c}{P_e} \right]_{(l)} = R_{(l)}$$

$$R_0 = (0.3953 + 2.785 \gamma_d) \epsilon_d (0.28563 + 0.8621 \gamma_d)$$

Algorithm

$$R_{(l+1)} = R_{(l)} - F[R_{(l)}] / F'[R_{(l)}] \quad l = 0, 1, 2, \dots$$

Where

$$F[R(t)] = \Xi_d [R(t)]^{(1/\gamma_d)} [1 - R(t)]^{-\Gamma_d - 1/2} - \epsilon_d$$

$$F'[R(t)] = \Xi_d (1/\gamma_d) [R(t)]^{-\Gamma_d} \left\{ 1 - [R(t)]^{-\Gamma_d} \right\}^{-1/2}$$

$$- (1/2) \Xi_d \Gamma_d [R(t)]^{-(2\Gamma_d)} \left\{ 1 - [R(t)]^{-\Gamma_d} \right\}^{-3/2}$$

Terminate iteration if

$$\left| F[R(t)] / \epsilon_d \right| < 0.000001 \text{ or } t = 10$$

then set

$$(P_c/P_e = R(t))$$

Optimum thrust coefficient ($P_e = P_d$)

$$C_{FO} = \Omega_d \left[1 - (P_c/P_e)^{-\Gamma_d} \right]^{1/2}$$

Vacuum thrust coefficient ($P_d = 0$)

$$C_f = C_D \lambda_d C_{FO} + \epsilon \frac{P_c}{P_e}$$

Characteristic Velocity (ft/sec)

$$C^* = \frac{I_{spH} \bar{g}_c}{C_f}$$

Reference Throat Area (in²)

$$A_{tref} = \frac{A_{eM} \times 144}{\epsilon_d}$$

Web Thickness (in)

$$f_{wt} = \tau_w D_p / 2$$

Number of points in table (dim)

Set J such that

$$t'_{MJ} > t'_{M(J+1)}$$

or when table is full J = 25

For option using input thrust versus time

$$\text{if } r'_{b1000} = 0$$

the thrust multiplier logic is used to evaluate the adjusted vacuum thrust time points \hat{F}_M and \hat{t}_{Mj}

Chamber Pressure (lb/in²)

$$p_{cJ} = \hat{F}_{Mj} / (A_{tref} \cdot C_f)$$

$$j = 1, \dots, J$$

The total impulse (lb-sec)

$$I_{Tn} = C_{f1} \sum_{j=1}^{J-1} (\hat{F}_{M(j+1)} + \hat{F}_{Mj})(\hat{t}_{M(j+1)} - \hat{t}_{Mj})$$

Burn Rate Coefficient ($[\text{in}/\text{sec}][\text{in}^2/\text{lb}]^n$)

$$a = \frac{f_{wt}}{I_r}$$

Where

$$I_{rb(jh)} = \begin{cases} \frac{[P_{c(j+1)}^{n+1} - P_{cj}^{n+1}] [\hat{t}_{M(j+1)} - \hat{t}_{Mj}]}{(n+1) [P_{c(j+1)} - P_{cj}]} & \text{if } P_{c(j+1)} \neq P_{cj} \\ P_{cj}^n |\hat{t}_{M(j+1)} - \hat{t}_{Mj}| & \text{otherwise} \end{cases}$$

$$I_r = \sum_{j=2}^J I_{rbj}$$

Reference Burn Rate at 1000 psi (in/sec)

$$r_{bref} = a(1000)^n$$

Fraction Web Burned at Thrust Time Points (dim)

$$g_{w1} = 0$$

$$g_{wj} = g_{w(j-1)} + \frac{a}{f_{wt}} I_{rbj}$$

$$j = 2, \dots, J$$

Fraction Propellant at Thrust Time Points (dim)

$$g_{p1} = 0$$

$$g_{pj} = g_{p(j-1)} + \frac{[\hat{F}_{M(j)} + \hat{F}_{M(j-1)}] [\hat{t}_{Mj} - \hat{t}_{M(j-1)}]}{2 * I_{TM}}$$

$$j = 2, \dots, J$$

Total Propellant Weight (lb)

$$W_p = I_{TM} / I_{SPM}$$

Initial Chamber Volume (in³)

$$V_{c1} = \frac{W_p}{\rho_p} \left(\frac{(1-\tau_w)^2}{1 - (1-\tau_w)^2} \right)$$

Chamber Volume at Thrust Time Points (in³)

$$V_{cj} = V_{c1} + \frac{W_p}{\rho_p} g_{pj} \quad j = 2, \dots, J$$

Time Rate Change of Chamber Pressure Between Thrust Time Points
(lb/in²-sec)

$$\dot{p}_c = \begin{cases} [P_{c(j+1)} - P_c] / [\hat{t}_{M(j+1)} - \hat{t}_{Mj}] & \text{If } \hat{t}_{M(j+1)} \neq \hat{t}_{Mj} \\ [P_{c(j+1)} - P_{cj}] / .0001 & \text{Otherwise} \end{cases}$$

$$j = 1, \dots, J-1$$

Last point

$$\dot{P}_{cJ} = 0$$

Burn Surface Coefficients (1/in), (in²/sec), ([lb/in²-sec][in²/lb]ⁿ)

$$C_{AS1} = \frac{\bar{g}_c \left(\frac{\gamma_d + 1}{2} \right)^{\frac{\gamma_d + 1}{\gamma_d - 1}}}{\gamma_d C^{*2} \times 12}$$

$$C_{AS2} = \frac{A_{tref} \bar{g}_e}{C^*}$$

$$C_{AS3} = \rho_p a$$

Surface Areas (in²)

$$A_{S1} = (C_{AS2}/C_{AS3}) P_{c1}^{1-n}$$

$$A_{Sj} = \frac{C_{AS1} \dot{p}_{cj} v_{cj} A_{S2} \dot{v}_{cj}}{C_{AS3} p_{cj}^n}$$

$$j = 2, \dots, J$$

If $A_{Sj} < 0$, A_{Sj} is set to zero

For option using input chamber pressure versus time

$$\text{If } r'_{b1000} < 0$$

Chamber Pressure (lb/in²)

$$P_{cj} = F'_{Mj} \quad j = 1, \dots, J$$

Vacuum Thrust (lb)

$$\hat{F}_{Mj} = P_{cj} A_{tref} C_f \quad j = 1, \dots, J$$

Total Impulse (lb-sec)

$$I_{TM} = 0.5 K_t \sum_{j=1}^{J-1} (\hat{F}_{M(j+1)} + \hat{F}_{Mj})(t'_{M(j+1)} - t'_{Mj})$$

The initialization parameters are set as:

$$I'_{VT} = 0$$

$$I'_{VM} = I_{TM}$$

$$P'_{arm} = 0$$

The thrust multiplier logic is used to evaluate the adjusted vacuum thrust time points \hat{t}_{Cj} and \hat{t}_{cj} and the logic in the option using the input thrust versus time is used to evaluate the ballistic parameters.

For option using input A_{Sj} versus g_{wj}

$$\text{If } r_{b1000} > 0$$

Set

$$g_{wj} = 0$$

$$g_{wj} = t'_{Mj} \quad j = 2, \dots, J$$

$$A_{Sj} = F'_{Mj} \quad j = 1, \dots, J$$

Burn Rate Coefficient ($[\text{in}/\text{sec}][\text{in}^2/\text{lb}]^n$)

$$a = r'_{\text{b1000}} / (1000)^n$$

Burn Surface Area Coefficients ($1/\text{in}$), (in^2/sec), ($[\text{lb}/\text{in}^2\text{-sec}][\text{in}^2/\text{lb}]^n$)

$$C_{\text{AS1}} = \frac{\bar{P}_c \left(\frac{\gamma_d + 1}{2} \right)^{\frac{\gamma_d + 1}{\gamma_d - 1}}}{12 \gamma_d C^{*2}}$$

$$C_{\text{AS2}} = \frac{A_{\text{tref}} \bar{g}_e}{C^*}$$

$$C_{\text{AS3}} = \rho_p a$$

Chamber Pressure Coefficients

$$C_{\text{PC1}} = \frac{C_{\text{AS1}} a}{(n+1) C_{\text{AS2}}}$$

$$C_{\text{PC2}} = \frac{C_{\text{AS1}}}{2 \rho_p}$$

$$C_{\text{PC3}} = \frac{C_{\text{AS3}}}{C_{\text{AS2}}}$$

Initial Chamber Pressure (lb/in^2)

$$P_{\text{c1}} = (C_{\text{PC3}} A_{\text{S1}})^{\frac{1}{1-n}}$$

Evaluating V_{cj} , P_{cj} , \dot{P}_{cj} , \ddot{t}_{Mj} at g_{wj} points

The following calculations are performed for $j = 1, \dots, J$

Incremental Burn Distance

$$\Delta r_{bj} = (g_{wj+1} - g_{wj}) f_{wt}$$

Iteration for Chamber Pressure, i.e., $P_{c(j+1)}$

let

k = iteration number

$$\begin{aligned} F(P_{ck}) &= P_{ck} + C_{PC1} \frac{V_{c(j-1)}}{\Delta r_{bj}} \left(P_{ck}^{n+1} - P_{cj-1}^{n+1} \right) \\ &\quad + C_{PC2} (P_{ck}^2 - P_{cj-1}^2) - C_{PC3} A_{S(j)} P_{ck}^n \\ F'(P_{ck}) &= 1 + C_{PC1} \frac{V_{c(j-1)}}{\Delta r_{bj}} (n+1) P_{ck}^n \\ &\quad + 2 C_{PC2} P_{ck} - n C_{PC3} A_{S(j)} P_{ck}^{n-1} \end{aligned}$$

Newton-Raphson Iteration Method

Algorithm

$$P_{(k+1)} = P_{ck} - F(P_{ck}) / F'(P_{ck}) \quad k = 1, 2, \dots$$

Terminate iteration if:

$$\left(\frac{P_{c(k+1)} - P_{ck}}{|P_{ck}|} \right) < 1.E-10$$

or $k = 50$

Set

$$P_c(j) = P_c(k+1)$$

Time rate change of chamber pressure

$$\dot{P}_{cj} = \frac{P_{c(j)} - P_{c(j-1)}}{\tau} = \frac{a}{\Delta r_{bj(n+1)}} \left(P_{c(j)}^{n+1} - P_{c(j-1)}^{n+1} \right)$$

Initial chamber volume

$$V_{c1} = \frac{(1-\tau_w)^2}{1-(1-\tau_w)^2} \frac{fwt}{2} \sum_{j=1}^{J-1} (A_{S(j+1)} + A_{Sj}) (g_{w(j+1)} - g_{wi})$$

Chamber volume

$$V_{c(j+1)} = V_{cj} + \frac{C_{AS2}}{2\rho} \tau_j (P_{c(j+1)} + P_{cj})$$

Incremental burn time (sec)

$$\tau_j = \frac{\Delta r_{bj(n+1)}}{a} \left[\frac{P_{c(j+1)} - P_{cj}}{P_{c(j+1)}^{n+1} - P_{cj}^{n+1}} \right]$$

Time

$$\hat{t}_{M1} = 0$$

$$\hat{t}_{Mj} = \sum_{i=2}^j \hat{t}_{M(i-1)} \tau_{i-1}$$

Vacuum Thrust (lb)

$$\hat{F}_{Mj} = P_{cj} C_f A_{crrf} \quad j = 1, \dots, J$$

Total Impulse (lb-sec)

$$I_{TM} = 0.5 \sum_{j=1}^{j_{\max}-1} (\hat{F}_{M(j+1)} + \hat{F}_{Mj}) (\hat{t}_{M(j+1)} - \hat{t}_{Mj})$$

Total Propellant Weight (lb)

$$W_p = I_{TM} / I_{STM}$$

Fraction Expended Propellant at Thrust Time Points for $j = 1, 2, \dots, J$

$$s_{p1} = 0$$

$$s_{pj} = s_{p(j-1)} + \frac{[\hat{F}_{M(j)} + \hat{F}_{M(j-1)}] [\hat{t}_{Mj} - \hat{t}_{M(j-1)}]}{2 \times I_{TM}}$$

The initialization parameters are set as:

$$I'_{VT} = 0$$

$$I'_{VM} = I_{TM}$$

$$P_{arm} = 0$$

The thrust multiplier logic is used to evaluate the adjusted complementary tube vacuum thrust time points \hat{F}_{Cj} and \hat{t}_{Cj} .

The following logic is applicable to all options when $D_p \neq 0$

Extinguishment Area

$$A_{xj} = 1.1 \frac{AS_j C_{AS3} C^*}{\bar{g}_e} \left[\frac{a}{n\alpha_p} \frac{V_{Cj}}{AS_j} \frac{C_{AS1}}{\rho_p} \right]^{\frac{1-n}{1+n}}$$

Maximum Extinguishment Area

$$A_{xmax} = \text{MAX} (A_{xj} \quad j = 1, \dots, j_{max})$$

Average Reference Chamber Pressure

$$\bar{P}_{cref} = \frac{I_{TM}}{A_{tref} C_f \hat{t}_{M,J}}$$

Maximum Reference Chamber Pressure

$$P_{cmax} = \text{MAX} (P_{cj} \quad j = 1, \dots, J)$$

Maximum Allowable Chamber Pressure

$$P_{CMXA} \begin{cases} 1.E 30 & P_{max} = 0 \\ P_{max} & P_{max} > 0 \\ -P_{max} \quad P_{cmax} & P_{max} < 0 \end{cases}$$

Maximum Surface Area

$$A_{SMAX} = \text{MAX} (A_{Sj} \quad j = 1, \dots, J)$$

Minimum Throat Area

$$A_{xmin} = A_{SMAX} P_{CMXA}^{n-1} C_{AS3} \frac{C^*}{\bar{g}_e}$$

d. Controllable Motor Dynamics

The following logic and equations evaluate the dynamic internal ballistics of a pintle controlled single chamber motor.

Burn Rate

$$r_b = \begin{cases} 0 & \text{If } A_t > A_{XI} \\ a p_c^n & \text{Otherwise} \end{cases}$$

Burn Depth

$$D_b = \int_0^t r_b dt$$

Percent Web

$$g_{wl} = D_b / l_{wt}$$

Interpolation Formulas

Index Table

j is such that

$$g_{wj} \leq g_{wl} < g_{w(j+1)}$$

Incremental Burn Distance

$$\Delta r_b = (g_{wl} - g_{wj}) f_{wt}$$

Interpolation Time

$$\tau = \begin{cases} \frac{[(n+1) \dot{P}_{cj} \frac{\Delta r_b}{a} + (P_{cj})^{n+1}]^{1/(n+1)} - P_{cj}}{\dot{P}_{cj}} & \text{If } P_{cj} \neq P_{c(j+1)} \\ \frac{\Delta r_b}{a} P_{cj}^{-n} & \text{Otherwise} \end{cases}$$

Chamber Volume

$$V_{cI} = V_{cj} + \frac{A_{tref} \cdot \bar{g}_e}{\rho_p C^*} (P_{cj} \tau + \frac{1}{2} \dot{P}_{cj} \tau^2)$$

Nominal Vacuum Thrust

$$F_{VN} = \hat{F}_{Mj} + \frac{(\hat{F}_{M(j+1)} - \hat{F}_{Mj})}{t_{M(j+1)} - t_{Mj}} \tau$$

Nominal Delivered Thrust

$$F_N = F_{VN} - P_a A_{eM}$$

Burn Surface Areas

$$A_{SI} = \frac{C_{AS1} \dot{P}_{cj} V_{cI} + C_{AS2} (P_{cj} + \dot{P}_{cj} \tau)}{C_{AS3} (P_{cj} + \dot{P}_{cj} \tau)^n}$$

Time Change of Chamber Pressure

$$\dot{P}_c = \begin{cases} (C_{AS3} A_{SI} P_c^n - \frac{A_t}{A_{tref}} C_{AS2} P_c) / (C_{AS1} V_{cI}) & \text{If } A_t < A_X \\ - \frac{A_t}{A_{tref}} C_{AS2} P_c / C_{AS1} V_{cI} & \text{Otherwise} \end{cases}$$

Equilibrium

$$P_{ceq} = \begin{cases} \left[\frac{C_{AS3} A_{tref} A_{SI}}{A_t C_{AS2}} \right]^{\frac{1}{1-n}} & \text{If } A_t < A_x \\ 0 & \text{Otherwise} \end{cases}$$

Chamber Pressure

$$P_c = \begin{cases} P_{co} + \int_{t_{Bk}=0}^t \dot{P}_c dt & \text{If TMC} \neq 0 \\ P_{ceq} & \text{Otherwise} \end{cases}$$

where TMC is the thrust dynamic mode, if = 0, the achieved thrust equals command thrust and, if = 1, the first order response system is solved.

The initial chamber pressure is set at $P_{co} = P_{cl}$ (\dot{P}_c equation)

Expansion Ratio

$$\epsilon = \epsilon_d A_{tref}/A_t$$

Thrust Coefficient

$$C_{FI} = f(\gamma_d, \epsilon, \alpha_d, C_d)$$

Thrust

$$F_{Hv} = P_c A_t C_{FI}$$

Mass Weight Flow Rate

$$\dot{W}_{MP} = \frac{P_c A_t \bar{g}_e}{C^*}$$

Mass Propellant Removed

$$W_{pr} = \int_{Bk=0}^{t_{Bk}} \dot{W}_{MP} dt$$

Fraction of Propellant Removed

$$g_{PI} = \frac{W_{pi}}{W_p}$$

Extinguishment Area

$$A_{XI} = \frac{A_{SI} C_{AS3} C^*}{\bar{g}_e} \left[\frac{a}{n\alpha_p} \frac{V_{CI}}{A_{SI}} \frac{C_{AS1}}{\rho_p} \right]^{\frac{1-n}{1+n}}$$

The following logic evaluates the commanded chamber pressure and equilibrium throat area for a given commanded thrust.

Commanded Vacuum p_t (lb)

$$F_{vcom} = F_c + P_a A_{em}$$

Iterate for R_{ATCC}

$$R_{ATCC0} = 1$$

$$\epsilon_{cci} = \epsilon_d / R_{ATcci}$$

$$C_{fi} = f(\gamma_d, \epsilon_{cci}, \alpha_d, C_d)$$

$$R_{ATcc(i+1)} = \left[\frac{C_{AS3}}{C_{AS2}} A_{sI} \right]^{\frac{1}{n}} \left(\frac{A_{tref} R_{ATcci} C_{fi}}{F_{vcom}} \right)^{\frac{1-n}{n}}$$

Converged if

$$\frac{|R_{ATcc(i+1)} - R_{ATcci}|}{R_{ATcci}} < 1. \times 10^{-6}$$

$$A_{tcc} = A_{tref} R_{ATcci}$$

Command Chamber Pressure (lb/in²)

$$P_{cc} = \frac{F_{cv}}{A_{tcc} C_{fi}}$$

Pintle Area Control Law

Rate Change of Throat Area

$$\dot{A}_t = K_S (P_c - P_{cc} + K_p \dot{P}_c)$$

where

the pintle control frequency (rad/sec)

$$\omega_p = \frac{C_{AS2} (1-n)}{C_{AS1} V_{CI}}$$

the dynamic constant (lb/in⁴-sec)

$$\lambda_p = \frac{C_{AS2}}{A_{tref} C_{AS1} V_{CI}} \left[\frac{C_{AS3} A_{SI}}{C_{AS2}} \right]^{\frac{1}{1-n}}$$

Controller Frequency

$$\omega_{pc} = \begin{cases} \omega_p & \text{if } \omega'_{pc} = 0 \\ \omega_{pc} & \text{otherwise} \end{cases}$$

Pressure Error Gain (in⁴/lb-sec)

$$K_S = \frac{\omega_p^2}{\lambda_p}$$

Pressure Rate Gain (sec)

$$K_p = \frac{4}{\omega_{pc}}$$

Throat Area

$$A_{tp} = \begin{cases} A_{t0} + \int_{t_{Bk}}^t \dot{A}_t dt & \text{If TMC} \neq 0 \\ A_{tcc} & \text{Otherwise} \end{cases}$$

$$A_t = \begin{cases} A_{xmax} & \text{If } A_{tp} > A_{xmax} \\ A_{xmin} & \text{If } A_{tp} < A_{xmin} \\ A_p & \text{Otherwise} \end{cases}$$

Initial Throat Area

$$A_{t0} = A_{tref}$$

If $A_{tp} > A_{xmin}$ or $A_{tp} < A_{xmin}$

Set

$$\dot{A}_t = 0$$

e. Main Table Delivered Thrust

Thrust equation to include flow separation in the nozzle:

$$F_M = \begin{cases} 0 & \text{if } F_{Mv} = 0 \\ F_{Mv} - P_d A_{eM} & \text{if } \epsilon_d = 0 \text{ or } P_s \leq P_e \\ 0 & \text{if } \epsilon_d \neq 0 \text{ and } P_c \leq P_d \\ \left\{ \lambda_d C_D \Omega_d [1 - (P_s/P_c)^{\gamma_d}]^{1/2} + (P_s - P_d) (\epsilon_s/P_c) \right\} & \\ [(P_c A_{eM}/\epsilon) (1/144)] & \text{Otherwise,} \end{cases}$$

Where F_{Mv} is obtained from the main vacuum thrust-weight table,

A_{eM} the input area, and P_d the static base pressure.

Nozzle exit pressure (lb/in.²)

$$P_e = P_c / (P_c/P_e).$$

Nozzle separation pressure (lb/in.²)

$$P_s = \begin{cases} P_d (a_s + b_s) \left[\frac{2}{(\gamma_d + 1)} \right] \left[\gamma_d / (\gamma_d - 1) \right] (P_c/P_d)^{-c_s} & \text{If } P_c > P^* \\ P_d & \text{Otherwise} \end{cases}$$

Static base pressure (lb/in.²)

$$P_d = P_a / 144.0$$

Where P_a is the ambient pressure.

Where

$$a_s = \begin{cases} 0.3 & \text{If } a'_s = b'_s = c'_s = 0 \\ a'_s & \text{Otherwise} \end{cases}$$

$$b_s = \begin{cases} 0.7 & \text{If } a'_s = b'_s = c'_s = 0 \\ b'_s & \text{Otherwise} \end{cases}$$

$$c_s = \begin{cases} 0.884 & \text{If } a'_s = b'_s = c'_s = 0 \\ c'_s & \text{Otherwise} \end{cases}$$

Where a'_s , b'_s , and c'_s are input nozzle separation polynomial coefficients.

Nozzle separation expansion ratio

$$\epsilon_s = \begin{cases} \Xi_d (P_s/P_c)^{-(1/\gamma_d)} [1 - (P_s/P_c)^{\gamma_d - 1}] & \text{If } P_c > P^* \\ 1 & \text{Otherwise} \end{cases}$$

Nozzle critical pressure

$$P^* = P_c [2/(\gamma_d + 1)]^{[\gamma_d/(\gamma_d - 1)]}$$

f. Complementary Thrust-Weight

The complementary thrust-weight table consists of the following input: thrust, weight flow and time perturbation factors, K'_{FC} , K_{WC} , K_{tC} ; specific impulse, I_{spC} ; nozzle exit area, A_{eC} ; complementary stage weight, W_{CO} ; total vacuum impulse quantities, I'_{VC} ; complementary weight carryover flag, K_{NO} ; and a maximum of 25, $j = 1, 2, \dots, 25$, monotonically increasing complementary thrust weight switching times, $t_{C(j)}$, and weight flow, $\dot{W}_{C(j)}$.

The adjusted complementary thrust-weight table is as follows: At stage initiation set up a 6 parameter table with a maximum of 25 rows such that the:

Adjusted time switching points are:

$$\hat{t}_{C(j)} = K_{tC} t_{C(j)}$$

Adjusted vacuum thrust points are:

$$\hat{F}_{C(j)} = K_{FC} F_{M(j)}$$

Adjusted total complementary weight flow points are

$$\hat{\dot{W}}_{C(j)} = \begin{cases} 0 & \text{If } \hat{t}_{C(j+1)} = \hat{t}_{Cj} \text{ or } j = J \text{ and } W_{Co} < 0 \\ (\hat{W}_{Cj} - W_{C(j+1)}) / (\hat{t}_{C(j+1)} - \hat{t}_{Cj}) & \text{If } \hat{t}_{C(j+1)} \neq \hat{t}_{Cj} \text{ and } j \neq J \text{ and } W'_{Co} < 0 \\ K_{WC} \dot{W}_{C(j)} & \text{If } I_{spC} = 0 \text{ and } W'_{Co} \geq 0 \\ K_{WC} \dot{W}_{C(j)} = \hat{F}_{C(j)} / I_{spC} & \\ \text{Otherwise} & \end{cases}$$

Adjusted time rate change of vacuum thrust points is

$$\hat{\dot{F}}_{C(j)} = \begin{cases} 0 & \text{If } \hat{t}_{C(j)} \geq t_{C(j+1)} \\ [\hat{F}_{C(j+1)} - \hat{F}_{C(j)}] / [\hat{t}_{C(j+1)} - \hat{t}_{C(j)}] & \text{Otherwise} \end{cases}$$

Adjusted time rate change of weight flow points is

$$\hat{\dot{W}}_{C(j)} = \begin{cases} 0 & \text{If } \hat{t}_{C(j)} \geq \hat{t}_{C(j+1)} \text{ or } W'_{CO} < 0 \\ [\hat{W}_{C(j+1)} - \hat{W}_{C(j)}] / [\hat{t}_{C(j+1)} - \hat{t}_{C(j)}] & \text{Otherwise} \end{cases}$$

Adjusted complementary table expended weight points are

$$\hat{\dot{W}}_{C(j)} = \begin{cases} 0 & \text{If } j = 1 \\ W_{C1} - W_{Cj} & \text{If } W'_{CO} < 0 \\ \sum_{i=1}^j 0.5 [\dot{W}_{C(i)} - \dot{W}_{C(i-1)}] [\hat{t}_{C(i)} - \hat{t}_{C(i-1)}] & \text{Otherwise} \end{cases}$$

For table interpolation:

Weight expended for complementary motor

$$W_C = \hat{W}_{C(j)} + \dot{W}_{C(j)} \Delta t_C + 0.5 \hat{\dot{W}}_{C(j)} \Delta t_C^2$$

Weight flow rate

$$\dot{W}_C = \hat{W}_{C(j)} + \hat{W}_{C(j)} \Delta t_C$$

Vacuum thrust

$$F_{Cv} = \hat{F}_{C(j)} + \hat{F}_{C(j)} \Delta t_C$$

Where j is such that

$$\hat{t}_{C(j)} \leq t_B < \hat{t}_{C(j+1)} \text{ or } t_{C(j+1)} < \hat{t}_{C(j)} < t_B$$

And

$$\Delta t_C = t_B - \hat{t}_B - \hat{t}_{C(j)}$$

Thrust equation for the complementary thrust

$$F_C = \begin{cases} 0 & \text{If } F_{Cv} = 0 \\ F_{Cv} - A_{eC} P_a & \text{Otherwise} \end{cases}$$

Where F_{Cv} is the complementary thrust weight table vacuum thrust, A_{eC} is the input complementary exit area, and P_a is the atmospheric pressure.

g.

Thrust Multipliers

The logic and equations presented in this section will accept the input thrust time table to correspond to any reference altitudes and convert them to vacuum conditions so that the trajectory program may use them in the standard manner. The reference altitude pressure, input in pounds per square foot will stipulate that the input thrust time points will be for that atmospheric pressure and similarly designate that the input specific impulse and input total impulse be applicable at that altitude pressure.

Main table time multiplier

$$K_{tM} = \begin{cases} 1.0 & \text{If } K'_{tM} = 0.0 \\ K_{tM} & \text{Otherwise} \end{cases}$$

Main table reference atmospheric pressure

$$P_{arM} = \begin{cases} 2116 & \text{If } P'_{arM} < 0 \\ P'_{arM} & \text{Otherwise} \end{cases}$$

Calculate the back pressure impulse as

$$I_{FM} = P_{arM} A_{eM} K_{tM} \sum_{j=1}^{J_M-1} S_{IMj} [t_{M(j+1)} - t_{Mj}]$$

Where

$$\delta_{IMj} = \begin{cases} 0 & \text{If } F'_{mj} = F'_{M(j+1)} = 0 \\ 1.0 & \text{Otherwise} \end{cases}$$

The input main total impulse adjusted to vacuum total impulse is:

$$\hat{I}_{vM} = \begin{cases} 0 & \text{If } I'_{vM} = 0 \\ I'_{vM} + I_{FM} & \text{Otherwise} \end{cases}$$

Main table time adjusted input thrust integral is:

$$I_{vM} = K_{tM} \sum_{j=1}^{J_M-1} [F'_{M(j)} + F'_{M(j+1)}] [t_{M(j+1)} - t_{M(j)}]^{1/2}$$

The main table time multiplier, K_{tM} is input in Lk009

The main table thrust reference atmospheric pressure, P'_{arM} , is input in Lk020

The main table nozzle exit area, A_{eM} , is input in Lk011

The main table tabular time points, t_{Mj} , are input in Lk0XX, where $XX = 17 + 3j$ and $t_{M1} = 0$

The main table tabular thrust points F'_{Mj} are input in Lk0YY, where $YY = 18 + 3j$

The main table total impulse, I'_{vM} , is input in Lk005

The subscript j refers to the j -th row of the thrust weight table

I_M refers to the last input row of the main thrust weight table. Such that $t_{M(j+1)} \geq t_{M(j)}$ or $j = 25$

Complementary table time multiplier:

$$K_{tC} = \begin{cases} 1.0 & \text{If } K'_{tM} = 0.0 \\ K'_{tM} & \text{Otherwise} \end{cases}$$

Complementary table reference atmospheric pressure:

$$P_{arC} = \begin{cases} 2116 & \text{If } P'_{arC} < 0 \\ P'_{arC} & \text{Otherwise} \end{cases}$$

Calculate the back pressure impulse as

$$I_{FC} = P_{arC} A_{eC} K_{tC} \sum_{j=1}^{J_C-1} \delta_{ICj} [t_{C(j+1)} - t_{Cj}]$$

Where

$$\delta_{ICj} = \begin{cases} 0 & \text{If } F'_{Cj} = F'_{C(j+1)} = 0 \\ 1.0 & \text{Otherwise} \end{cases}$$

The input complementary total impulse adjusted to vacuum total impulse is:

$$I_{vC} = \begin{cases} 0 & \text{If } I'_{vC} = 0 \\ I'_{vC} + I_{FC} & \text{Otherwise} \end{cases}$$

Complementary table adjusted input thrust integral

$$I_{VC} = K_{tC} \sum_{j=1}^{J_C-1} [F'_{C(j)} + F'_{C(j+1)}] [t_{C(j+1)} - t_{C(j)}]^{1/2}$$

The complementary table time multiplier, K'_{tC} , is input in Lk102

The complementary table thrust reference atmospheric pressure, P'_{arC} , is input in Lk110

The complementary table nozzle exit area, A_{eC} , is input in Lk104

The complementary table tabular time points, t_{Cj} , are input in Lk1XX, where $XX = 7 + 3j$ and $t_{C1} = 0$

The complementary tabular thrust points, F'_{Cj} , are input in Lk1YY, where $YY = 8 + 3j$

The complementary table total impulse, I'_{vC} , is input in Lk106

The subscript j refers to the j -th row of the thrust weight table, such that $t_{C(j+1)} \geq t_{C(j)}$ or $j = 2j$

J_C refers to the last input row of the complementary thrust weight table

Total main and complementary impulses corrected to vacuum

$$\hat{I}_{VT} = \begin{cases} 0 & \text{If } I'_{vT} = 0 \\ I'_{vT} + I_{FM} + I_{FC} & \text{Otherwise} \end{cases}$$

The vacuum scale factors for the main and complementary stage thrust-time table, are determined as follows:

$$K''_{FM} = \begin{cases} I'_{VT} / (I_{VM} + I_{VC}) & \text{If } I'_{VT} \neq 0 \\ I'_{VT} / I_{VM} & \text{If } I'_{VT} = 0 \text{ and } I'_{VM} \neq 0 \\ K'_{FM} & \text{If } I'_{VT} = I'_{VM} = 0 \\ 1.0 & \text{If } I'_{VT} = I'_{VM} = K'_{FM} = 0 \end{cases}$$

$$K''_{FC} = \begin{cases} I'_{VT} / (I_{VM} + I_{VC}) & \text{If } I'_{VT} \neq 0 \\ I'_{VT} / I_{VC} & \text{If } I'_{VT} = 0 \text{ and } I'_{VC} \neq 0 \\ K'_{FC} & \text{If } I'_{VT} = I'_{VC} = 0 \\ 1.0 & \text{If } I'_{VT} = I'_{VC} = K'_{FC} = 0 \end{cases}$$

Main table vacuum adjusted thrust integral is:

$$I^*_{VM} = I_{VM} + I_{FM} / K''_{FM}$$

The main table adjusted to vacuum thrust points are:

$$F_{Mj} = F'_{Mj} + P_{arM} A_{eM} \delta_{FMj}$$

Where

$$\delta_{FMj} = \begin{cases} 0 & \text{If } F'_{Mj} = 0 \\ 1.0 / K''_{FM} & \text{Otherwise} \end{cases}$$

Complementary table vacuum adjusted thrust integral

$$I_{vC}^* = I_{vC} + I_{FC} / K_{FC}''$$

The complementary table adjusted to vacuum thrust points are:

$$F_{Cj} = F_{Cj}' + P_{arC} A_{eC} \delta_{FCj}$$

Where

$$\delta_{FCj} = \begin{cases} 0 & \text{If } F_C' = 0 \\ 1.0 / K_{FC}'' & \text{Otherwise} \end{cases}$$

The total of the main and complementary impulse, I_{VT}' , is input in Lk004.

K_{FM} and K_{FC} , the multipliers of the main and complementary stage vacuum thrusts, respectively, are determined as follows:

$$K_{FM} = \begin{cases} \hat{I}_{VT}' / (I_{vM}^* + I_{vC}^*) & \text{If } I_{VT}' \neq 0 \\ \hat{I}_{vM}' / I_{vM}^* & \text{If } I_{VT}' = 0 \text{ and } I_{vM}' \neq 0 \\ K_{FM}' & \text{If } I_{VT}' = I_{vM}' = 0 \\ 1.0 & \text{If } I_{VT}' = I_{vM}' = K_{FM}' = 0 \end{cases}$$

$$K_{FC} = \begin{cases} \hat{I}_{VT}' / (I_{vM}^* + I_{vC}^*) & \text{If } I_{VT}' \neq 0 \\ \hat{I}_{vC}' / I_{vM}^* & \text{If } I_{VT}' = 0 \text{ and } I_{vC}' \neq 0 \\ K_{FC}' & \text{If } I_{VT}' = I_{vM}' = 0 \\ 1.0 & \text{If } I_{VT}' = I_{vM}' = K_{FC}' = 0 \end{cases}$$

Where the main table thrust multiplier, K_{FM}^I , is input in Lk007

The complementary table thrust multiplier, K_{FC}^I , is input in Lk100

The main table adjusted to vacuum specific impulse is:

$$I_{spM} = I'_{spM} \frac{I_{VM}^* K_{FM}^I}{(I_{VM}^* K_{FM}^I - I_{FM})}$$

Where

The main table specific impulse, I'_{spM} is input in Lk010

The complementary table adjusted to vacuum specific impulse is:

$$I_{spC} = I'_{spC} \frac{I_{VC}^* K_{FC}^I}{(I_{VC}^* K_{FC}^I - I_{FC})}$$

Where

The complementary table specific impulse, I'_{spC} , is input in Lk103

The total main and complementary tables vacuum adjusted thrust integral

$$I_{VT}^* = I_{VM}^* + I_{VC}^*$$

Total main and complementary calculated total vacuum impulse

$$I_{VT} = I_{VM}^* K_{FM}^I + I_{VC}^* K_{FC}^I$$

h. Auxiliary Roll Control System

The weight expended for roll control is determined by integrating the roll control weight flow determined from:

$$\dot{W}_R = \begin{cases} 0 & \text{If } I_{spR} = 0 \\ |F_R|/I_{spR} & \text{Otherwise} \end{cases}$$

where F_R is the instantaneous roll control thrust and:

$$I_{spR} = \begin{cases} I_{spR1} & \text{for } t_B \leq t'_{R2} \\ I_{spR2} & \text{for } t'_{R2} \leq t_B \leq t'_{R3} \\ I_{spR3} & \text{for } t_B \geq t'_{R3} \end{cases}$$

with I_{spRj} ($j = 1, 2, 3$) input for each stage with the roll control data and t_B the instantaneous current stage time.

At the initiation of the current stage, the expended roll control weight is:

$$W_R = \begin{cases} 0 & \text{If } K_{Ok} = 0 \\ W_R(t_{S(k-1)}) & \text{If } K_{Ok} \neq 0 \end{cases}$$

where $W_R(t_{S(k-1)})$ is the expended roll control weight at the end of the previous stage.

The roll thrust, F_R , for a given roll rate is given in section D.2.b.

2. Thrust Forces and Moments

Thrust components and moments required in the linear and angular momenta equations during the K-th stage are as follows:

a. Axial Forces

$$F_X = \begin{cases} F/[1.0 + \tan^2 (\delta_P + \delta_{MP}) + \tan^2 (\delta_Y + \delta_{MY})]^{\frac{1}{2}} & \text{If } K_\delta = 0 \\ \{F_M/[1.0 + \tan^2 (\delta_P + \delta_{MP}) + \tan^2 (\delta_Y + \delta_{MY})]^{\frac{1}{2}}\} \\ + F_C & \text{If } K_\delta = 1 \\ F/[1.0 + \tan^2 \delta_{MP} + \tan^2 \delta_{MY}]^{\frac{1}{2}} & \text{If } K_\delta = 2 \end{cases}$$

$$F_X = \begin{cases} F/[1.0 + \tan^2 \delta_P + \tan^2 \delta_Y]^{\frac{1}{2}} & \text{If } K_\delta = 0 \\ F_M/[1.0 + \tan^2 \delta_P + \tan^2 \delta_Y]^{\frac{1}{2}} & \text{If } K_\delta = 1 \\ F & \text{If } K_\delta = 2 \end{cases}$$

b. Lateral

$$F_y = \begin{cases} [F \tan (\delta_Y + \delta_{MY})] / [1.0 + \tan^2 (\delta_P + \delta_{MP}) + \tan^2 (\delta_Y + \delta_{MY})]^{\frac{1}{2}} & \text{If } K_\delta = 0 \\ \{[F_M \tan (\delta_Y + \delta_{MY})] / [1.0 + \tan^2 (\delta_P + \delta_{MP}) + \tan^2 (\delta_Y + \delta_{MY})]\}^{\frac{1}{2}} & \text{If } K_\delta = 1 \\ [F \tan \delta_{MY}] / [1.0 + \tan^2 \delta_{MP} + \tan^2 \delta_{MY}]^{\frac{1}{2}} & \text{If } K_\delta = 2 \end{cases}$$

$$F_Y = \begin{cases} [F \tan \delta_Y] / [1.0 + \tan^2 \delta_P + \tan^2 \delta_Y]^{\frac{1}{2}} & \text{If } K_\delta = 0 \\ [F_M \tan \delta_Y] / [1.0 + \tan^2 \delta_P + \tan^2 \delta_Y]^{\frac{1}{2}} & \text{If } K_\delta = 1 \\ 0 & \text{If } K_\delta = 2 \end{cases}$$

c. Transverse

$$F_z = \begin{cases} [F \tan (\delta_P + \delta_{MP})] / [1.0 + \tan^2 (\delta_P + \delta_{MP}) + \tan^2 (\delta_Y + \delta_{MY})]^{\frac{1}{2}} & \text{If } K_\delta = 0 \\ \{[F_M \tan (\delta_P + \delta_{MP})] / [1.0 + \tan^2 (\delta_P + \delta_{MP}) + \tan^2 (\delta_Y + \delta_{MY})]\}^{\frac{1}{2}} & \text{If } K_\delta = 1 \\ [F \tan \delta_{MP}] / [1.0 + \tan^2 \delta_{MP} + \tan^2 \delta_{MY}]^{\frac{1}{2}} & \text{If } K_\delta = 2 \end{cases}$$

$$F_Z = \begin{cases} [F \tan \delta_P] / [1.0 + \tan^2 \delta_P + \tan^2 \delta_Y]^{\frac{1}{2}} & \text{If } K_\delta = 0 \\ [F_M \tan \delta_P] / [1.0 + \tan^2 \delta_P + \tan^2 \delta_Y]^{\frac{1}{2}} & \text{If } K_\delta = 1 \\ 0 & \text{If } K_\delta = 2 \end{cases}$$

Where δ_P and δ_Y are the pitch and yaw thrust deflections, respectively, δ_{MP} and δ_{MY} are the stage input thrust vector misalignment angles, K_δ is the input per stage control flag, F is the total thrust, and F_M is the main thrust, F_C is the complementary thrust.

d. Thrust Moments

Pitch

$$M_{FOQ} = F_x (z_e - z_{cg}) \quad \text{Offset}$$

$$M_{FCQ} = F_z \ell_e \quad \text{Control}$$

Yaw

$$M_{FOR} = -F_x (y_e - y_{cg}) \quad \text{Offset}$$

$$M_{FCR} = -F_y \ell_e \quad \text{Control}$$

Roll

$$M_{FCP} = F_z (y_e - y_{cg}) - F_y (z_e - z_{cg}) \quad \text{Offset}$$

$$M_{FVP} = \eta_{vr} F \quad \text{Vortex} \quad \text{where } \eta_{vr} = 0.00363$$

unless otherwise input

6. Jet Damping

The jet damping forces and moments on a missile having an internally burning fuel arise from the reaction to the Coriolis force exerted on the exhaust gas as it moves along the missile x_b axis toward the nozzle exit plane in the presence of missile angular rotation.

a. Force

$$F_{JDy} = (\dot{W}/\bar{g}_e)(2\ell_E - \ell_{Pf} - \ell_{Pa}) R_b (\pi/180)$$

$$F_{JDz} = (\dot{W}/\bar{g}_e)(2\ell_E - \ell_{Pf} - \ell_{Pa}) Q_b (\pi/180)$$

b. Moment

$$M_{JDQ} = -(\dot{W}/\bar{g}_e)[\ell_E^2 - (\ell_{Pf}^2 + \ell_{Pf}\ell_{Pa} + \ell_{Pa}^2)/3] Q_b (\pi/180)$$

$$M_{JDR} = -(\dot{W}/\bar{g}_e)[\ell_E^2 - (\ell_{Pf}^2 + \ell_{Pf}\ell_{Pa} + \ell_{Pa}^2)/3] R_b (\pi/180)$$

where \dot{W} is the total instantaneous missile weight flow, \bar{g}_e is the input mass conversion gravity, Q_b and R_b are the instantaneous vehicle angular pitch and yaw velocities, and ℓ_E , ℓ_{Pf} , and ℓ_{Pa} are the nozzle exit, forward and aft propellant grain lever arms defined in Section 1.3.

f. Propellant Grain and Nozzle Exit Location

The values are computed as follows:

(1) Nozzle Exit

$$x_E = \begin{cases} x_e & \text{If } x_E' = 0 \\ \bar{x}_e x_E' & \text{Otherwise} \end{cases}$$

(2) Aft End of Propellant

$$x_{Pa} = \begin{cases} x_{cg} & \text{If } x_{Pa}' = 0 \\ \bar{x}_e x_{Pa}' & \text{Otherwise} \end{cases}$$

(3) Forward End of Propellant

$$x_{Pf} = \begin{cases} x_{cg} & \text{If } x_{Pf}' = 0 \\ \bar{x}_e x_{Pf}' & \text{Otherwise} \end{cases}$$

where x_E' , x_{Pf}' , and x_{Pa}' are input per stage, x_e is the thrust gimbal location, and x_{cg} is the vehicle instantaneous center of gravity.

g. Thrust Gimbal Location

The thrust gimbal location is specified in the left-handed Cartesian coordinate system shown in Figure 27. Thrust location components are x_e , the missile body station measured along the centerline, and y_e and z_e are measured from the vehicle centerline positive to the right and down, respectively. The gimbal components are input for each stage as constants. The Y and Z components represent a thrust eccentricity which yields moments during powered flight. The clustered motor configuration is shown in Figure 28 and the effect of typical variation of thrust history is pictured in Figure 29. The effect of clustered motors is simulated as follows as a thrust vector point offset.

$$\begin{aligned}
 x_e &= \bar{x}_e x'_e \\
 n'_m = 0 \text{ or } 1 &\quad \begin{cases} y_e = \bar{x}_e y'_e \\ z_e = \bar{x}_e z'_e \end{cases} \\
 n'_m = 2 &\quad \begin{cases} y_e = [\sigma_f R_c \sqrt{2}] \cos \phi_v + \bar{x}_e y'_e \\ z_e = [\sigma_f R_c \sqrt{2}] \sin \phi_v + \bar{x}_e z'_e \end{cases} \\
 n'_m > 2 = &\quad \begin{cases} y_e = [\sigma_f R_c \sqrt{2} n_m] \cos \phi_v + \bar{x}_e y'_e \\ z_e = [\sigma_f R_c \sqrt{2} n_m] \sin \phi_v + \bar{x}_e z'_e \end{cases}
 \end{aligned}$$

$$\sigma_f = [4.5 (F_h^2 + F_n^2 + F_L^2) / (F_h + F_n + F_L)^2 - 1.5]^{1/2}$$

and

$$F_L = \{1 / (1 + \{[\sigma_{tb}^2 + \sigma_{lt}^2] / 2\}^{1/2})\} \{f[F_{vac} (1 - \sigma_{tb}) t]\}$$

$$F_h = [1 + \{(\sigma_{tb}^2 + \sigma_{It}^2)/2\}^{1/2}] \{f[F_{vac}(1 + \sigma_{tb})t]\}$$

$$F_n = F_{vac}$$

The following are input to this part of the program:

$$\bar{X}_e, X'_e, y'_e, z'_e, n'_m, R_c, \phi_v, \sigma_{tb}, \sigma_{It}, \text{ and } F(t).$$

The following are required output from this analysis:

$$y_e = f(t)$$

$$z_e = f(t)$$

The internally calculated number of motors in a cluster (n_m) and the number of control nozzles in that cluster (n_c) are defined.

$$n_m = \begin{cases} i & \text{If } n'_m = 0 \\ n'_m & \text{Otherwise} \end{cases}$$

$$n_c = \begin{cases} n'_m & \text{If } n'_c = 0 \\ n'_c & \text{Otherwise} \end{cases}$$

where n'_m is the input number of motors for the k th stage, n'_c is the input number of control motors for the k th stage.

h. Movable Nozzle Tail-Wag-Dog Forces Moments

Pitch

$$F_{TDz} = \begin{cases} 0 & \text{if } I_n = 0 \text{ or } \omega_c = 0 \text{ or } M_y \neq 2, \text{ or } 5 \\ (\pi/180) W_n \ell_n \ddot{\delta}_p / W & \text{Otherwise} \end{cases}$$

$$M_{TDQ} = \begin{cases} 0 & \text{if } I_n = 0 \text{ or } \omega_c = 0 \text{ or } M_y \neq 2, \text{ or } 5 \\ (\pi/180)(I_n + W_n \ell_e \ell_n / \bar{g}_e) \ddot{\delta}_p & \text{Otherwise} \end{cases}$$

Yaw

$$F_{TDy} = \begin{cases} 0 & \text{if } I_n = 0 \text{ or } \omega_c = 0 \text{ or } M_y \neq 5 \\ (\pi/180) W_n \ell_n \ddot{\delta}_y / W & \text{Otherwise} \end{cases}$$

$$M_{TDR} = \begin{cases} 0 & \text{if } I_n = 0 \text{ or } \omega_c = 0 \text{ or } M_y \neq 5 \\ (\pi/180)(I_n + W_n \ell_e \ell_n / \bar{g}_e) \ddot{\delta}_y & \text{Otherwise} \end{cases}$$

where I_n is the movable portion of the nozzle mass moment of inertia, W_n is the weight of the movable portion of the nozzle, ℓ_e is the vehicle center of gravity to nozzle gimbal point distance, ℓ_n is the movable portion of the nozzle center of gravity to the gimbal point distance, ω_c is the input second order TVC transfer function flag, \bar{g}_e is the mass to weight conversion gravity, and $\ddot{\delta}_p$, $\ddot{\delta}_y$ are the nozzle angular deflection acceleration in pitch and yaw respectively.

3. Vehicle Weight

Instantaneous missile weight, W , is computed from the un-adjusted staging weight, W_S , the expended main weight, W_M , the expended complementary weight, W_C , the expended roll control weight, W_R , and the jettisoned weight, W_{JT} , respectively, as follows:

$$W = W_S - W_M - W_C - W_R - W_{JT}$$

Main and complementary weights are functions of input initial stage weights, weight flows, vacuum thrust and specific impulse, and multipliers. In addition, the main weight is dependent upon input weights at each thrust-weight switching time. Roll control and auxiliary motor expended weights are functions of thrust and specific impulse. If $W \leq 0$, the run is halted and "WEIGHT HAS GONE TO ZERO" is printed.

Missile mass is computed as follows:

$$m = W/\bar{g}_e$$

where

$$\bar{g}_e = \begin{cases} g_e & \text{If } \bar{g}'_e \text{ is input 1.4} \\ 32.174 & \text{If } \bar{g}'_e \text{ is input zero} \\ \bar{g}'_e & \text{Otherwise} \end{cases}$$

The unadjusted staging weight defined as follows:

$$W_S(k) = \begin{cases} W_{PL} + \sum_{p=k}^4 [W_{MO(p)} + W_{CO(p)}] & \text{if } k=K_k \text{ or } K_{O(k-1)} = 0 \text{ and } K_{NO(k-1)} = 0 \\ W_{(g)} & \\ W_{PL} - W_{C(g)} + W_{C(k-1)} + \sum_{p=k}^4 [W_{MO(p)} + W_{CO(p)}] & \text{if } K_{NO(k-1)} \neq 0 \text{ and } K_{O(k-1)} = 0 \end{cases}$$

Where k is the current stage number; K_k is the input stage start control function; $K_{O(k)}$ and $K_{NO(k)}$ are the input weight carryover flag and input complementary thrust-weight table carryover flag respectively; $W_{(g)}$ and $W_{C(g)}$ are the vehicle weight, and expended complementary weight at the termination of the $(k-1)$ th stage respectively, $W_{MO(k)}$ and $W_{CO(k)}$ are the main and complementary initial stage weight for the k -th stage, and W_{PL} is the input payload weight.

Main and complementary weights are functions of input initial stage weights, weight flows, vacuum thrust and specific impulse, and multipliers. In addition, the main weight is dependent upon input weights at each thrust-weight switching time. If $W \leq 0$, the run is halted and the statement "WEIGHT HAS GONE TO ZERO" is printed.

Total weight flow is

$$\dot{W} = \dot{W}_M + \dot{W}_C + \dot{W}_R$$

a. Initial Stage Weight Calculations--Initial stage weights are calculated as follows:

If the input main stage weight W_{MO} is input negative, the stage weight will be calculated as a function of stage time and the input values in the thrust weight table. The stage weight-history values are input in the column normally used for the input weight flow values. Linear interpolation between these input table weight points will be used to evaluate the instantaneous stage weight.

Similar logic holds for the complementary weight if W_{CO} is input negative.

Main Table Weight

$$W_{MO} = \begin{cases} W_{M1} & \text{if } W'_{MO} < 0 \\ W'_{MO} & \text{Otherwise} \end{cases}$$

Where W'_{MO} is the input main stage weight input in Lk006 and W_{M1} is the first input main table weight point input in Lk022.

Complementary table weight

$$W_{CO} = \begin{cases} W_{C1} & \text{if } W'_{CO} < 0 \\ W'_{CO} & \text{Otherwise} \end{cases}$$

Where W'_{CO} is the input complementary stage weight input in Lk105 and W_{C1} is the first input complementary table weight point input in Lk012.

b. Jettison Weight Calculations

The weight lost to jettisoning is

$$W_{JT} = \sum_{j=1}^8 W_{JT(j)}$$

Where

$$W_{JT(j)} = \begin{cases} 0 & \text{before } \sigma_J(j) = K_J(j) \\ W_{JT(j)} & \text{after } \sigma_J(j) = K_J(j) \end{cases}$$

with $\sigma_J(j)$ ($j = 1, 2, \dots, 8$) the achieved value of the parameter designated by code input and $K_J(j)$ the input value of that parameter at which the weight, $W_{JT(j)}$, is to be jettisoned. Logically the jettisoning must be satisfied sequentially.

I. MASS PROPERTIES

1. Center-of-Gravity

The center of-gravity location is specified in the same left-handed coordinate system as the gimbal location. The Y and Z components represent a center-of-gravity offset which yields moments during powered and atmospheric flight. The center-of-gravity location will be input for each stage as a linear function of the total instantaneous vehicle weight.

a. Center-of-Gravity Body Station

Fifteen center of gravity body stations (x_{cg}) can be input for each stage. The body station is computed from input during the current stage as follows:

$$\text{For } W_j \geq W \geq W_{j+1}$$

$$x_{cg} = \bar{x}_{cg} [W_j x_{cg(j+1)} - W_{j+1} x_{cgj} + (x_{cgj} - x_{cg(j+1)})W] / (W_j - W_{j+1})$$

where \bar{x}_{cg} , W_j , and x_{cgj} ($j = 1, 2, \dots, 15$) are input for each stage with the moment of inertia data, and W is the instantaneous vehicle weight. The W_j are input monotonically decreasing so that $W_1 > W_2 \dots$

The first and last input logic for the center of gravity is:

If $W > W_1$, then

$$x_{cg} = \bar{x}_{cg} x_{cg1}$$

or if $W < W_j$, then

$$x_{cg} = \bar{x}_{cg} x_{cgj}$$

where the W_1 and x_{cg1} and the W_j ($J = 1, 2, \dots$ or 15) and x_{cgJ} are the first and last input values respectively.

b. Center-of-Gravity Offset

Fifteen offsets can be input for each stage. The Y and Z offsets for the current stage are as follows:

$$y_{cg} = z_{cg} = 0$$

Otherwise for $W_j \geq W \geq W_{j+1}$

$$y_{cg} = \bar{X}_{cg} [W_j y_{cg(j+1)} - W_{j+1} y_{cgj} + (y_{cgj} - y_{cg(j+1)})W / (W_j - W_{j+1})]$$

$$z_{cg} = \bar{X}_{cg} [W_j z_{cg(j+1)} - W_{j+1} z_{cgj} + (z_{cgj} - z_{cg(j+1)})W / (W_j - W_{j+1})]$$

where $j = 1, 2, \dots, 15$ and $@_j$, y_{cgj} , and z_{cgj} are input for each stage in a table with the body station values. The W_j 's are input monotonically decreasing.

The first and last input logic given for the body station center of gravity are applicable for the offset data.

2. Moments of Inertia

Fifteen pitch, I_{YY} , yaw, I_{ZZ} , and roll, I_{XX} , moment of inertia values can be input per stage. The moments of inertia are linear functions of total instantaneous vehicle weight and are computed as follows:

For $W_j \geq W \geq W_{j+1}$

$$I_{XX} = \bar{I}_{Xk} [W_j I_{X(j+1)} - W_{j+1} I_{Xj} + (I_{Xj} - I_{X(j+1)})W / (W_j - W_{j+1})]$$

$$I_{YY} = \bar{I}_{Yk} [W_j I_{Y(j+1)} - W_{j+1} I_{Yj} + (I_{Yj} - I_{Y(j+1)})W / (W_j - W_{j+1})]$$

$$I_{ZZ} = \bar{I}_{Zk} [W_j I_{Z(j+1)} - W_{j+1} I_{Zj} + (I_{Zj} - I_{Z(j+1)})W / (W_j - W_{j+1})]$$

$$I_{XY} = \bar{I}_X [W_j I_{XY(j+1)} - W_{j+1} I_{XYj} + (I_{XYj} - I_{XY(j+1)})W / (W_j - W_{j+1})]$$

$$I_{XZ} = \bar{I}_X [W_j I_{XZ(j+1)} - W_{j+1} I_{XZj} + (I_{XZj} - I_{XZ(j+1)})W / (W_j - W_{j+1})]$$

$$I_{YZ} = \bar{I}_Y [W_j I_{YZ(j+1)} - W_{j+1} I_{YZj} + (I_{YZj} - I_{YZ(j+1)})W / (W_j - W_{j+1})]$$

where \bar{I}_X , \bar{I}_Y , \bar{I}_Z , \bar{I}_{XY} , \bar{I}_{XZ} , \bar{I}_{YZ} ($j = 1, 2, \dots, 15$) are input for each stage with the body station center of gravity and W is the instantaneous vehicle weight. The W_j 's are input monotonically decreasing.

The time derivatives of the moments of inertia required in the angular momenta equations are:

For $W_j \geq W \geq W_{j+1}$

$$\dot{I}_{XX} = \begin{cases} 0 & \text{If } \bar{I}_{Xk} = 0 \\ -\ddot{W}\bar{I}_X (I_{Xj} - I_{X(j+1)}) / (W_j - W_{j+1}) & \text{Otherwise} \end{cases}$$

$$\dot{I}_{YY} = -\ddot{W}\bar{I}_Y (I_{Yj} - I_{Y(j+1)}) / (W_j - W_{j+1}) \quad \text{Otherwise}$$

$$\dot{I}_{ZZ} = \begin{cases} -\ddot{W}\bar{I}_Z (I_{Zj} - I_{Z(j+1)}) / (W_j - W_{j+1}) & \text{If } \bar{I}_{Zk} \neq 0 \\ \dot{I}_{YY} & \text{Otherwise} \end{cases}$$

$$\dot{I}_{XY} = \begin{cases} 0 & \text{If } \bar{I}_X = 0 \\ -\ddot{W}\bar{I}_X (I_{XYj} - I_{XY(j+1)}) / (W_j - W_{j+1}) & \text{Otherwise} \end{cases}$$

$$\dot{I}_{XZ} = \begin{cases} 0 & \text{If } \bar{I}_X = 0 \\ -\ddot{W}\bar{I}_X (I_{XZj} - I_{XZ(j+1)}) / (W_j - W_{j+1}) & \text{Otherwise} \end{cases}$$

$$\dot{I}_{YZ} = \begin{cases} 0 & \text{If } \bar{I}_X = 0 \\ -\ddot{W}\bar{I}_X (I_{YZj} - I_{YZ(j+1)}) / (W_j - W_{j+1}) & \text{Otherwise} \end{cases}$$

where W is the total instantaneous vehicle weight flow.

The first and last input logic for the moments of inertia and their derivatives are:

$$\begin{aligned}
 I_{XX} &= \begin{cases} \bar{I}_X I_{X1} & \text{If } W > W_1 \\ \bar{I}_X I_{XJ} & \text{If } W < W_J \end{cases} \\
 I_{YY} &= \begin{cases} \bar{I}_Y I_{Y1} & \text{If } W > W_1 \\ \bar{I}_Y I_{YJ} & \text{If } W < W_J \end{cases} \\
 I_{ZZ} &= \begin{cases} I_{YY} & \text{If } \bar{I}_Z = 0 \\ \bar{I}_Z I_{Z1} & \text{If } \bar{I}_Z \neq 0 \text{ and } W > W_1 \\ \bar{I}_Z I_{ZJ} & \text{If } \bar{I}_Z \neq 0 \text{ and } W < W_J \end{cases} \\
 I_{XY} &= \begin{cases} \bar{I}_X I_{XY1} & \text{If } W > W_1 \\ \bar{I}_X I_{XYJ} & \text{If } W < W_J \end{cases} \\
 I_{XZ} &= \begin{cases} \bar{I}_X I_{XZ1} & \text{If } W > W_1 \\ \bar{I}_X I_{XZJ} & \text{If } W < W_J \end{cases} \\
 I_{YZ} &= \begin{cases} \bar{I}_X I_{YZ1} & \text{If } W > W_1 \\ \bar{I}_X I_{YZJ} & \text{If } W < W_J \end{cases}
 \end{aligned}$$

and if $W > W_1$ or $W < W_J$

where the W_1 and $I_{X,Y,Z1}$ and the W_J and $I_{X,Y,ZJ}$ ($J = 1, 2, \dots, 15$) are the first and last input values respectively.

3. Lever Arms

Significant distances shown in Figures 20 and 21 are given below:

- a. Gimbal Point to Center-of-Gravity

$$l_e = x_e - x_{cg}$$

- b. Movable Portion of Nozzle Center-of-Gravity to Gimbal Point

$$l_n = (x'_n - x'_e) \bar{x}_e$$

- c. Center-of-Gravity to Center of Pressure Distance

$$l_{cp} = x_{cg} - x_{cp}$$

- d. Nozzle Exit to Center-of-Gravity

$$l_E = x_E - x_{cg}$$

- e. Forward End of Propellant Grain to Center-of-Gravity

$$l_{pf} = x_{pf} - x_{cg}$$

- f. Aft End of Propellant Grain to Center-of-Gravity

$$l_{pa} = x_{pa} - x_{cg}$$

- g. Pitch Movable Control Fin Center of Pressure to Hinge Axis

$$l_{hz} = (U_{cz} - U_{hz}) l_{bz}$$

- h. Pitch Movable Control Fin Center of Pressure to Center-of-Gravity

$$\ell_{\delta z} = x_{hz} - x_{cg} + \ell_{hz} \cos (\delta_p * K_{cf})$$

$$\ell_{\delta} = x_{hz} - x_{cg} + \ell_{hz}$$

- i. Yaw Movable Control Fin Center of Pressure to Center-of-Gravity

$$\ell_{\delta y} = x_{hz} - x_{cg} + \ell_{hz} \cos (\delta_y * K_{cf})$$

where x_e is the gimbal point body station, x_n is the movable portion of nozzle center of gravity body station, x_{cp} is the aerodynamic center of pressure body station x_{cg} is the vehicle center-of-gravity body station, x_E is the nozzle exit body station, x_{pf} is the forward end of propellant grain body station, x_{pa} is the aft end of propellant grain body station. U_{cz} is the pitch movable control fin center of pressure to the leading pitch fin base root location distance to the pitch fin base root length ration, U_{hz} is the pitch movable control fin hinge axis to the leading fin base root location distance to the pitch fin base root length ratio, ℓ_{bz} is the input pitch fin base root length, x_{hz} is the input missile body station of the pitch fin hinge axis, δ_p is the instantaneous pitch deflection angle, δ_y is the instantaneous yaw deflection angle and K_{cf} is the fin control multiplier.

J. TRAJECTORY PARAMETERS

Parameters which have no effect on the solution of the momenta equations are formulated. The parameters are introduced because of their usefulness as switching functions and/or the additional trajectory characteristics they furnish. A few of the parameters that can be represented geometrically are shown in Figure 26.

1. Orbital Elements and Impact Determination

The equations in this section are computed if

$$K_{c1} \leq \sigma_c \leq K_{c2} \text{ or at termination of the final stage}$$

where σ_c is the achieved value of a quantity designated by code input and K_{c1} and K_{c2} are input limits.

If the quantities in this section are involved as switching functions, e.g., flight segment initiation or termination, then the proper values of $K_{c1,2}$ and σ_c must be input. However, the equations are always computed at cut-off, but cannot be used as cut-off switching function unless the σ_c -logic is satisfied. The print is always given at cut-off.

Once $\sigma_c \geq K_{c1}$ or $\sigma_c > K_{c2}$, the possibility that at some later time $\sigma_c < K_{c1}$ or $\sigma_c \leq K_{c2}$ is ignored. Obtaining the limit values by interpolation is not done.

a. Orbital Elements

If the above criteria apply, the following are computed:

The parameters

$$a_1 = r_c V_I^2 / g_e r_e^2$$

$$a_2 = a_1 \cos^2 \gamma_{1I}$$

$$a_3 = a_1 \sin \gamma_{1I} \cos \gamma_{1I}$$

where r_c , V_I , and γ_{1I} are current values

The eccentricity

$$e = [a_3^2 + (1 - a_2)^2]^{\frac{1}{2}}$$

and the perigee altitude

$$h_p = (r_p - r_e)/6076.1033$$

where r_e is input and $r_p = a_2 r_c / (1 + e)$

b. Apogee and Impact

If $0 < e < 1$, compute:

The apogee altitude

$$h_a = (r_a - r_e)/6076.10333$$

where $r_a = a_2 r_c / (1 - e)$

The velocity at apogee

$$v_{Ia} = | (r_c v_I \cos \gamma_{II}) / r_a |$$

The angle to apogee

$$\phi_a = \arctan [a_3 a_4 / (1 - a_2)]$$

where $0 \leq \phi_a < 360^\circ$ and

$$a_4 = \begin{cases} +1 \\ -1 \end{cases}$$

If $|\gamma_{II}| < 90^\circ$

Otherwise:

The flight time to apogee

$$\tau_a = (r_c^2 v_I \sin \gamma_{II}) / GM (2 - a_1) \\ + 2[r_c^3 / GM (2 - a_1)^3]^{1/2} (\pi/180) \arctan \{ [(1+e)/(1-e)]^{1/2} / \\ (1/\tan \frac{1}{2} \phi_a) \}$$

where $0 \leq \arctan \{ \} < 180$, t is the current time, and $\tau_a = 0$ if $\tan \frac{1}{2} \phi_a = 0$.

The total flight time to apogee

$$t_a = t + \tau_a$$

The orbital period

$$P = \pi[(r_a + r_p)/2]^{3/2} / 30\sqrt{GM}$$

and the terminal radial distance

$$r_f = r_e + h_f$$

where h_f is input

Besides the above criteria, the following must be satisfied in order to compute the equations given below:

1. If $K_\gamma = -1$, then, $\gamma_{II} > 0$, $r_a > r_f$, and $h < h_f$
2. If $K_\gamma = +1$, then, $r_a > r_f$, $r_p < r_f$, and if $\gamma_{II} < 0$, then, $h > h_f$

where K_γ is input as plus or minus one, so that

- $K_\gamma = +1$ if impact is to occur at an altitude of h_f
 $K_\gamma = -1$ if a space intercept is to occur at an altitude of h_f

If the above are satisfied, compute:

The glide range angle

$$\phi'_f = \phi_a + K_\gamma \arctan \{ [e^2 - (1 - a_2 r_c / r_f)^2]^{1/2} / (1 - a_2 r_c / r_f) \}$$

where $0 \leq \arctan \{ \} < 180^\circ$

The modified range angle is

$$\phi_f = \begin{cases} \phi'_f & \text{If } \phi'_f < 360^\circ \\ \phi'_f - 360^\circ & \text{Otherwise} \end{cases}$$

If $K_\gamma = 1$, $r_a > r_f$, and $r_p \geq r_f$, compute the modified range angle as follows:

$$\begin{aligned} \phi_f = (180/\pi) & \pi \{ (r_c/r_f) a_1 + 1 + 2[1 - (r_f/r_c)] / [1 - (r_c^2/r_f^2) \cos^2 \gamma_{II}] \} \\ & + (\pi/180) \arctan \{ 2a_4 [r_c/r_f] - 1 \} \tan \gamma_{II} / [(r_c/r_f - 1)^2 - \tan^2 \gamma_{II}] \} \end{aligned}$$

where $-180^\circ < \arctan \{ 2a_4 [(r_c/r_f) - 1] \tan \gamma_{II} / [(r_c/r_f - 1)^2 - \tan^2 \gamma_{II}] \} \leq 180^\circ$

The glide time is

$$\begin{aligned} \tau_f = r_f [(1 - a_2) \sin \phi_f + a_3 a_4 (-\cos \phi_f + r_c/r_f)] / (2 - a_1) V_I |\cos \gamma_{II}| \\ + 2[r_c^3 / GM(2 - a_1)^3]^{1/2} (\pi/180) \arctan \{ [(-1 + 2/a_1)^{1/2} \sin (\phi_f/2)] / \cos (a_5 + \phi_f/2) \} + \tau_p \end{aligned}$$

where $0 \leq \arctan \{ \} \leq 180^\circ$ and

$$a_5 = \begin{cases} \gamma_{1I} & \text{If } a_4 > 0 \\ -180 - \gamma_{1I} & \text{If } a_4 < 0 \text{ and } \gamma_{1I} < 0 \\ 180 - \gamma_{1I} & \text{Otherwise} \end{cases}$$

and

$$\tau_P = \begin{cases} 0 & \text{If } \phi_f < 360^\circ \\ 60 P & \text{Otherwise} \end{cases}$$

Total flight time is

$$t_f = t + \tau_f$$

where t is the current time.

The total range angle is

$$\phi_f = \phi + a_4 \phi_f - (180/\pi) \bar{\omega} t_f$$

where ϕ is the current range angle and $\bar{\omega}$ is input.

The ground range is

$$S_f = (\pi/180) \phi_f r_e / 6076.10333$$

The instantaneous latitude, longitudinal, and azimuthal flight path angles are:

$$\rho = \arcsin (\sin \rho_L \cos \phi + \cos \rho_L \sin \phi \cos \phi_i)$$

where

$$-90^\circ \leq \rho \leq 90^\circ$$

$$\mu' = \arctan [(\sin \phi \sin \phi_i \cos \rho_L) / (\cos \phi - \sin \rho_L \sin \rho)]$$

where

$$-180^\circ < \mu \leq 180^\circ$$

$$\mu = \mu_L - \mu'$$

$$-180^\circ < \mu \leq 180^\circ$$

$$\gamma_{21} = \arctan \left(\frac{[V_e \cos \gamma_1 \cos \rho_L \sin \phi_i]}{[V_e \cos \gamma_1 \cos \rho (\cos \phi_i \cos \mu' - \sin \phi_i \sin \mu' \sin \rho_L) + \omega r_c \cos^2 \rho]} \right)$$

$$0^\circ \leq \gamma_{21} < 360^\circ$$

ρ_f and μ_f are calculated as follows:

Impact latitude is

$$\rho_f = \arcsin (\sin \rho \cos |\phi_f| + \cos \rho \sin |\phi_f| \cos \gamma_{21})$$

with

$$-90^\circ \leq \rho_f \leq 90^\circ$$

where ρ and γ_{21} are the instantaneous latitude and azimuthal flight path angle, respectively.

Change in inertial longitude, positive in eastward direction, ($0 \leq \arctan [\] \leq 360^\circ$) $\mu'_I = (\text{sign } \phi_f) [\text{sign} (\sin \gamma_{21})] \arctan [(\sin |\phi_f| |\sin \gamma_{21}| \cos \rho) / (\cos |\phi_f| - \sin \rho_f \sin \rho)]$

Impact Longitude is

$$\mu_f = \begin{cases} \mu - \mu'_I + (180/\pi)\omega\tau_f & \text{If } -180^\circ < \mu - \mu'_I + (180/\pi)\omega\tau_f \leq +180^\circ \\ 360^\circ + \mu - \mu'_I + (180/\pi)\omega\tau_f & \text{If } -180 \leq \mu - \mu'_I + (180/\pi)\omega\tau_f \\ -360^\circ + \mu - \mu'_I + (180/\pi)\omega\tau_f & \text{If } 180 < \mu - \mu'_I + (180/\pi)\omega\tau_f \end{cases}$$

where ω is the input angular velocity of the earth.

The components of inertial velocity and total inertial velocity at the terminal altitude are

$$\begin{aligned}\dot{r}_f &= (V_I \cos \gamma_{1I} [a_3 a_4 \cos \phi_f - (1 - a_2) \sin \phi_f] / a_2) a_r \\ r_f \dot{\phi}_f &= (180/\pi) (r_c V_I \cos \gamma_{1I}) / r_f \\ V_{If} &= [\dot{r}_f^2 + (\pi/180)^2 (r_f \dot{\phi}_f)^2]^{1/2}\end{aligned}$$

and the terminal inertial flight path angle is

$$\gamma_{1If} = \arctan \dot{r}_f / r_f \dot{\phi}_f (\pi/180)$$

γ_{2If} , ρ_a , μ_a , S_a , γ_{2Ia} , and i are calculated as follows:

$$\gamma_{2If} = \arctan [\cos \rho \sin \gamma_{2I} \sin \phi_f / (\cos \phi_f \sin \rho_f - \sin \rho)]$$

with

$$-90^\circ \leq \gamma_{1If} \leq 90^\circ$$

and

$$0 \leq \gamma_{2If} < 360^\circ$$

Apogee longitude is

$$\mu_a = \begin{cases} \mu - \mu'_{Ia} + (180/\pi) \omega \tau_a & \text{If } -180^\circ < \mu - \mu'_{Ia} + (180/\pi) \omega \tau_a \leq 180^\circ \\ 360^\circ + \mu - \mu'_{Ia} + (180/\pi) \omega \tau_a & \text{If } -180^\circ \geq \mu - \mu'_{Ia} + (180/\pi) \omega \tau_a \\ -360^\circ + \mu - \mu'_{Ia} + (180/\pi) \omega \tau_a & \text{If } 180^\circ < \mu - \mu'_{Ia} + (180/\pi) \omega \tau_a \end{cases}$$

The total ground range to apogee is

$$S_a = \frac{(\pi/180)^k e}{6076.10333} \begin{cases} \arccos (\cos \rho_L \cos \rho_a \cos \Delta_a + \sin \rho_L \sin \rho_a) \\ \text{If } 0 \leq \Lambda_a < 180^\circ \\ 360^\circ - \arccos (\cos \rho_L \cos \rho_a \cos \Delta_a + \sin \rho_L \sin \rho_a) \\ \text{If } 180^\circ \leq \Lambda_a < 360^\circ \end{cases}$$

where $0 \leq \arccos [] \leq 180^\circ$

$$\Lambda_a = |\mu_L - \mu_a|$$

Inertial azimuthal flight path angle at apogee is

$$\gamma_{2Ia} = \arctan [(\cos \rho \sin \gamma_{2I} \sin \phi_a) / (\cos \phi_a \sin \rho_a - \sin \rho)]$$

where $0 \leq \gamma_{2Ia} < 360^\circ$

Inclination angle is

$$i = \arccos (\cos \rho \sin \gamma_{2I})$$

where $0 \leq i \leq 180^\circ$

Calculate the atmospheric entry condition if the following criteria are met:

1. $h_e \neq 0$ where h_e is input
2. $r_a > r_E$
3. $r_E = r_e + h_e$. If $\gamma_{1I} < 0$, then $h > h_e$

If the above are satisfied, compute the glide range to entry angle

$$\phi_E = \begin{cases} \phi_a + \arctan \{ [e^2 - (1 - a_2 r_c / r_E)^2]^{\frac{1}{2}} / (1 - a_2 r_c / r_E) \\ \quad \text{If } r_p < r_E \\ \text{where } 0 \leq \arctan [] < 180^\circ \\ (180/\pi) \left[\pi \left((r_c / r_E) a_1 + 1 + 2 [1 - (r_E / r_c)] / [1 - r_c^2 / r_E^2] \right. \right. \\ \quad \left. \left. \cos^2 \gamma_{1I} \right] \right] + (\pi/180) \arctan \left\{ (2a_4 [(r_c / r_E) - 1] \tan \right. \\ \quad \left. \gamma_{1I}) / [(r_c / r_E - 1)^2 - \tan^2 \gamma_{1I}] \right\} \\ \quad \text{If } r_p \geq r_E \\ \text{where } 0 \leq \arctan () < 180^\circ \end{cases}$$

$$-360^\circ < \phi_E < 360^\circ$$

The glide time is

$$\tau_E = r_E [(1-a_2) \sin \phi_E + a_3 a_4 (-\cos \phi_E + r_c / r_E)] / (2-a_1) V_I |\cos \gamma_{1I}| \\ + 2 [r_c^3 / GM (2-a_1)^3]^{\frac{1}{2}} (\pi/180) \arctan \{ [(-1+2/a_1)^{\frac{1}{2}} \sin (\phi_E/2)] / \\ \cos (a_5 + \phi_E) \}$$

where $0 \leq \arctan \{ \} \leq 180^\circ$ and

Total flight time to entry is

$$t_E = t + \tau_E$$

where t is the current time.

The total range angle to entry is

$$\phi_E = \phi + a_4 \phi_E - (180/\pi) \bar{\omega} \tau_E$$

where ϕ is the current range angle and $\bar{\omega}$ is the quasi earth rotation rate.

The ground range is

$$S_E = (\pi/180)\phi_E r_e / 6076.10333$$

Entry latitude is

$$\rho_E = \arcsin (\sin \rho \cos |\phi_E| + \cos \rho \sin |\phi_E| \cos \gamma_{2I})$$

with

$$-90^\circ \leq \rho_E \leq 90^\circ$$

where ρ and γ_{2I} are the instantaneous latitude and azimuthal flight path angle, respectively.

The components of inertial velocity and total inertial velocity at the entry altitude are

$$\dot{r}_E = \{v_I \cos \gamma_{1I} [a_3 a_4 \cos \phi_E - (1-a_2) \sin \phi_E] / a_2\} a_4$$

$$r_E \dot{\phi}_E = (180/\pi) (r_c v_I \cos \gamma_{1I}) / r_E$$

$$v_{IE} = [r_E^2 + (\pi/180)^2 (r_E \dot{\phi}_E)^2]^{1/2}$$

and the entry inertial flight angle is

$$\gamma_{1IE} = \arctan \dot{r}_E / [r_E \dot{\phi}_E (\pi/180)]$$

where $-180^\circ < \gamma_{1IE} \leq 180^\circ$

$$\gamma_{2IE} = \arctan [\cos \rho \sin \gamma_{2I} \sin \phi_E / (\cos \phi_E \sin \rho_E - \sin \rho)]$$

with

$$-90^\circ \leq \gamma_{1IE} \leq 90^\circ$$

and

$$0 \leq \gamma_{2IE} < 360^\circ$$

The velocity and flight path angle with respect to the ambient air at entry conditions are

$$V_{aE} = (V_{IE}^2 - 2\omega V_{IE} r_e \sin \gamma_{2IE} \cos \rho_E \cos \gamma_{1IE} + r_E^2 \omega^2 \cos^2 \rho_E)^{\frac{1}{2}}$$

$$\gamma_{1E} = \arcsin (V_{IE} \sin \gamma_{1IE} / V_{aE})$$

$$-90^\circ \leq \gamma_{1E} \leq 90^\circ$$

2. Integrals

a. Motor Impulse

The vacuum impulse is

$$I_v = \int_{t_k}^t F_v dt$$

and total impulse during the k-th stage is

$$I = \int_{t_k}^t F dt$$

where t_k is the time the k-th stage begins and t is the current time.

b. Control Impulse

The control system related integrals are

$$I_p = (1 + K_{\Delta}) \int_{t_k}^t |F_z| dt$$

$$I_y = (1 + K_{\Delta}) \int_{t_k}^t |F_y| dt$$

where

$$K_{\Delta} = \begin{cases} K'_{\Delta} & \text{If } K'_{\Delta} \neq 0 \\ 1.0 & \text{Otherwise} \end{cases}$$

A_L is the input amplitude of the limit cycle, ω_L is the input frequency of the limit cycle, t_B is stage time, K'_{Δ} is the input side impulse multiplier.

$$I_{\delta p} = 2 t_B A_L \omega_L / \pi + \int_{t_k}^t |\dot{\delta}_F| dt$$

$$I_{\dot{\delta}Y} = 2 \tau_B A_L \omega_L / \pi + \int_{t_k}^t |\dot{\delta}_Y| dt$$

$$\bar{I}_{\dot{\delta}P} = (n'_m / n'_c) I_{\dot{\delta}P}$$

$$\bar{I}_{\dot{\delta}Y} = (n'_m / n'_c) I_{\dot{\delta}Y}$$

where

If τ_c and $\omega_c \neq 0$

$$\dot{\delta}_P = (\delta_{Pj} - \delta_{P(j-1)}) / \Delta t_c$$

$$\dot{\delta}_Y = (\delta_{Yj} - \delta_{Y(j-1)}) / \Delta t_c$$

where I_P and I_Y are the pitch and yaw side impulse, respectively;
and $I_{\dot{\delta}P}$ and $I_{\dot{\delta}Y}$ are the sum of angular thrust vectoring velocities.
The integrals are ignored if $M_y \neq 5$.

The roll control expended impulse is

$$I_R = \int_{t_k}^t F_R dt$$

c. Aerodynamic Heating

The heat integral is

$$H_e = \int_{t_0}^t q V_a dt$$

where t_0 is the trajectory start time, q the missile dynamic pressure and V_a the total vehicle velocity with respect to the air.

d. Delta Velocities

The following are computed merely for print purposes.

The thrust-to-weight-flow ratio

$$|F/\dot{W}| = \begin{cases} 0 & \text{If } \dot{W} = G \\ |F/\dot{W}| & \text{Otherwise} \end{cases}$$

where F and \dot{W} are total instantaneous values.

The gravity loss from trajectory initiation

$$L_g = \int_{t_0}^t g_{Z1} \sin \gamma_1 dt$$

where t_0 is the trajectory start time, G_{Z1} is the gravity acceleration components and γ_1 the instantaneous flight path angle.

The ideal velocity from stage initiation

$$\Delta V = \bar{g}_e \int_{t_k}^t (F/\dot{W}) dt$$

where \bar{g}_e is gravity at the reference body surface and t_k is the stage initiation time.

The drag loss from stage initiation is

$$L_D = \bar{g}_e \int_{t_k}^t [(C + C_{\delta z}) \cos \bar{\alpha}' + (N_Z - N_{Pz} - N_{\delta z}) \sin \bar{\alpha} + (N_Y - N_{Py} - N_{\delta y}) \sin \bar{\beta}] / W dt$$

where C is the instantaneous aerodynamic axial force.

Instantaneous back pressure loss is

$$L_F = g_e \int_{t_k}^t (F_V - F)/W dt$$

where F_V is the instantaneous total vacuum thrust, F is the instantaneous delivered thrust g_e is the mass gravity and W is the instantaneous vehicle weight. Vector velocity loss from stage initiation is

$$L_V = \Delta V - L_F - L_g - L_D - V_e + V_{eok}$$

where V is the ideal velocity from stage initiation; L_F is the back pressure velocity loss. L_g is the gravity velocity loss, L_D is the drag velocity loss, V_e is the instantaneous missile earth reference velocity, and V_{eok} is the missile earth reference velocity at state initiation.

3. Target Position

The target position and velocities are determined from

- (1) input code (q_{Tto}), and value (K_{Tto}) which designates the start of the target maneuvering; (2) input initial velocity (V_{To}), flight path angle (γ_{To}), differential range azimuth (ζ_{To}), altitude (h_{To}), down range (S_{To}) and cross range (S_{TCO}) and;
- (3) tabular input target earth reference accelerations in "g's" tangential (a_{TTj}) normal (a_{TNj}) and transverse (a_{TCj}) to the target velocity vector and the target time terminating the j -th acceleration value (t_{Tj}).

a. Target Start Time

The target start time is set, i.e., ($t_{TS} = t$) when the specific value, K_{Tto} , delineated by the code, a_{Tto} , is achieved.

If the value has not been achieved set:

$$t_{To} = 0 \qquad a_{TT} = 0$$

$$\dot{v}_T = 0 \qquad a_{TN} = 0$$

$$\gamma_T = \gamma_{To} \qquad a_{TC} = 0$$

$$\zeta_T = \zeta_{To} \qquad \dot{h}_T = 0$$

$$s_T = s_{To} \qquad \dot{s}_T = 0$$

$$s_{TC} = s_{TCo} \qquad s_{TC} = 0$$

$$h_T = h_{To}$$

b. Target Coordinates

The target coordinates are as follows.

Acceleration (ft/sec)

$$\dot{v}_{Tj} = a_{TTj} \bar{g}_e$$

$$\dot{v}_{Nj} = a_{TNj} \bar{g}_e$$

$$\dot{v}_{Cj} = a_{TCj} \bar{g}_e$$

where j is such that $t_{T(j-1)} \leq t - t_{TS} < t_{Tj}$

If $t - t_{TS} \geq t_{Tj}$ set $j = J$

where J is the number of input time points such that

$$t_{T(k-1)} < t_{Tj}$$

The following differentials (target coordinates) are numerically integrated with respect to time.

Flight Path Angle Rate

$$\dot{\gamma}_T = (180/\pi) \dot{V}_N / V_T$$

Azimuthal Path Angle Rate

$$\dot{\zeta}_T = (180/\pi) \dot{V}_c / (V_T \cos \gamma_T)$$

Altitude Rate

$$\dot{h}_T = V_T \sin \gamma_T$$

Down Range Rate

$$\dot{S}_T = V_T \cos \gamma_T \cos \zeta_T$$

Cross Range Rate

$$\dot{S}_{TC} = V_T \cos \gamma_T \sin \zeta_T$$

4. Missile-Target Coordinates

The relation between the target and missile is used in Intercept Guidance ($T_y = 10$) and Homing Guidance ($T_y = 11$) types of flight to direct the attacking missile to the target. The following equations and logic delineate missile to target; differential altitude and earth surface down range and cross range distance (Δh , ΔS , and ΔS_c) distance rates ($\dot{\Delta h}$, $\dot{\Delta S}$, and $\dot{\Delta S}_c$) and total range distance and distance rate (R_{MT} and \dot{R}_{MT}), angle and angular rate of the missile to target line and local horizontal (α_{MT} and $\dot{\alpha}_{MT}$), angle and angular rate of the missile to target line differential azimuth (λ_{MT} and $\dot{\lambda}_{MT}$); seeker look angle and angular rate in pitch (ϵ_{MT} and $\dot{\epsilon}_{MT}$) and yaw (δ_{MT} and $\dot{\delta}_{MT}$); time to intercept (t_{MI}); range to target intercept (R_{MI}); intercept coordinates (S_{MI} , S_{MCI} , and h_{MI}), local flight path angle to intercept (α_{MI}) and differential flight path azimuth to intercept (γ_{MI}); flight path error to intercept (ϵ_{MI}); and flight path azimuth error to intercept (δ_{MI}).

a. Missile to Target Distance

Earth surface difference and distance rate

Down Range

$$\Delta S = S_T - S$$

$$\dot{\Delta S} = \dot{S}_T - \dot{S}$$

Cross Range

$$\Delta S_c = S_{TC} - S_c$$

$$\dot{\Delta S}_c = \dot{S}_{TC} - \dot{S}_c$$

Altitude Difference Distance and Distance Rate

$$\Delta h = h_T - h$$

$$\Delta \dot{h} = \dot{h}_T - \dot{h}$$

Missile to Target Distance and Distance Rate

$$R_{MT} = (\Delta S^2 + \Delta S_c^2 + \Delta h^2)^{\frac{1}{2}}$$

$$\dot{R}_{MT} = (\Delta S \Delta \dot{S} + \Delta S_c \Delta \dot{S}_c + \Delta h \Delta \dot{h}) / R_{MT}$$

b. Missile to Target Angles

Elevation

$$\alpha_{MT} = \arcsin (\Delta h / R_{MT}) \quad - 90^\circ \leq \alpha_{MT} \leq 90^\circ$$

$$\dot{\alpha}_{MT} = (180/\pi) (\Delta \dot{h} R_{MT} - \dot{R}_{MT} \Delta h) / (R_{MT}^2 \cos \alpha_{MT})$$

Differential Azimuth

$$\lambda_{MT} = \arctan (\Delta S_c / \Delta S) \quad - 180^\circ < \lambda_{MT} \leq 180^\circ$$

$$\dot{\lambda}_{MT} = (180/\pi) (\Delta \dot{S}_c \Delta S - \Delta S_c \Delta \dot{S}) \cos^2 \lambda_{MT} / \Delta S^2$$

Seeker Look Angle and Angular Rate

Relative Azimuthal velocity vector component

$$\gamma_M = \arctan (\dot{Y}_{TM} / \dot{X}_{TM}) \quad - 180^\circ < \gamma_M \leq 180^\circ$$

$$\dot{\gamma}_M = \begin{cases} 0 & \text{If } \dot{X}_{TM} = 0 \\ (180/\pi) \cos^2 \gamma_M [(\ddot{Y}_{TM} \dot{X}_{TM} - \dot{Y}_{TM} \ddot{X}_{TM}) / \dot{X}_{TM}^2] & \end{cases}$$

$$[\dot{A}_{TM}] = \left\{ \dot{\xi} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & -1 \\ 0 & -1 & 0 \end{bmatrix} + \dot{\phi} \begin{bmatrix} 0 & \sin \xi & \cos \xi \\ -\sin \xi & 0 & 0 \\ -\cos \xi & 0 & 0 \end{bmatrix} \right\} [A_{TM}]$$

where

$$[A_{TM}] = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \zeta & \sin \zeta \\ 0 & -\sin \zeta & \cos \zeta \end{bmatrix} \begin{bmatrix} \cos \phi & 0 & \sin \phi \\ 0 & 1 & 0 \\ -\sin \phi & 0 & \cos \phi \end{bmatrix} \begin{bmatrix} \cos \psi_i & -\sin \psi_i & 0 \\ \sin \psi_i & \cos \psi_i & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\dot{\vec{x}}_{TM} = [A_{TM}] \dot{\vec{x}}_{ee}$$

$$\ddot{\vec{x}}_{TM} = [A_{TM}] \ddot{\vec{x}}_{ee} + [\dot{A}_{TM}] \dot{\vec{x}}_{ee}$$

$$\epsilon_{MT} = (\alpha_{MT} - \gamma_1) \cos \phi + (\lambda_{MT} - \gamma_M) \sin \phi - \bar{\alpha}$$

$$\dot{\epsilon}_{MT} = (\dot{\alpha}_{MT} - \dot{\gamma}_1) \cos \phi + (\dot{\lambda}_{MT} - \dot{\gamma}_M) \sin \phi - \dot{\bar{\alpha}} \\ + \dot{\phi} [(\lambda_{MT} - \gamma_M) \cos \phi - (\alpha_{MT} - \gamma_1) \sin \phi]$$

$$\delta_{MT} = (\alpha_{MT} - \gamma_1) \sin \phi + (\lambda_{MT} - \gamma_M) \cos \phi + \bar{\beta}$$

$$\dot{\delta}_{MT} = (\dot{\alpha}_{MT} - \dot{\gamma}_1) \sin \phi + (\dot{\lambda}_{MT} - \dot{\gamma}_M) \cos \phi + \dot{\bar{\beta}} \\ + \dot{\phi} [(\alpha_{MT} - \gamma_1) \cos \phi + (\lambda_{MT} - \gamma_M) \sin \phi]$$

c. Target Intercept Parameters

Time to Target Intercept

$$t_{MI} = R_{MT} / \{ [v_c^2 - v_T^2 \sin^2 \epsilon_{MI}^*]^{\frac{1}{2}} - v_T \cos \epsilon_{MI}^* \}$$

where

$$\epsilon_{MI}^* = \arccos [\cos \alpha_T \cos \gamma_T \cos (\lambda_{MT} - \gamma_M) \\ + \sin \alpha_T \sin \gamma_T]$$

Range to Target Intercept

$$R_{MI} = V_e t_{MI}$$

Intercept Coordinates

$$S_{MI} = S_T + \dot{S}_T t_{MI}$$

$$h_{MI} = h_T + \dot{h}_T t_{MI}$$

$$S_{CMI} = S_{CT} + \dot{S}_{CT} t_{MI}$$

Angle to Target Intercept

Elevation

$$\alpha_{MI} = \arcsin [(h_{MI} - h)/R_{MI}]$$

$$-90^\circ \leq \alpha_{MI} \leq 90^\circ$$

Azimuth

$$T_{MI} = \arctan [(S_{CMI} - S_C)/(S_{MI} - S)]$$

$$-180^\circ < T_{MI} \leq 180^\circ$$

Flight Path Error to Intercept

Elevation

$$\epsilon_{MI} = \alpha_{MI} - \gamma_1 \quad -180^\circ < \epsilon_{MI} \leq 180^\circ$$

Azimuth

$$\delta_{MI} = T_{MI} - \gamma_M \quad -180^\circ < \delta_{MI} < 180^\circ$$

5. General

Because the following parameters can be involved as switching functions, their solutions are necessary after each integration step.

a. Stage Data

The instantaneous current stage time and main weight are

$$t_B = t - t_k$$

and

$$W_B = W_{gjk} - \Delta W_M$$

where t is the instantaneous time, t_k the stage start time, W_{gjk} the main step weight for the current stage at time t_j , and W_M the main weight lost between t_j and t .

b. Earth Referenced Values

The total vehicle velocity with respect to the launch site is

$$V_e = (\dot{x}_{ee}^2 + \dot{y}_{ee}^2 + \dot{z}_{ee}^2)^{\frac{1}{2}}$$

where $\dot{\vec{x}}_{ee}$ is obtained from the integration of the linear momenta equations.

The total vehicle acceleration along the flight path with respect to the launcher is

$$\dot{V}_e = \begin{cases} (\ddot{x}_{ee}^2 + \ddot{y}_{ee}^2 + \ddot{z}_{ee}^2)^{\frac{1}{2}} & \text{If } V_e = 0 \\ \frac{\dot{x}_{ee}\ddot{x}_{ee} + \dot{y}_{ee}\ddot{y}_{ee} + \dot{z}_{ee}\ddot{z}_{ee}}{V_e} & \text{Otherwise} \end{cases}$$

where $\vec{\ddot{x}}_{ee}$ is obtained from the linear momenta equations.

The local pitch flight path angle is

$$\gamma_1 = \begin{cases} 0 & \text{If } v_e = 0 \\ \arcsin (-\dot{z}_{11}/v_e) & \text{Otherwise} \end{cases}$$

with

$$-90^\circ \leq \gamma_1 \leq 90^\circ$$

$$\dot{\gamma}_1 = \begin{cases} 0 & \text{If } v_e = 0 \\ (\dot{z}_{11}\dot{v}_e - \ddot{z}_{11}v_e)/(v_e^2 \cos \gamma_1) & \text{Otherwise} \end{cases}$$

and the local azimuthal angle is

$$\gamma_2 = \begin{cases} 0 & \text{If } v_e = 0 \\ \arctan (\dot{y}_{11}/\dot{x}_{11}) & \text{Otherwise} \end{cases}$$

where $0 \leq \gamma_2 < 360^\circ$

$$\dot{\gamma}_2 = \begin{cases} 0 & \text{If } \dot{x}_{11} = 0 \\ \frac{(\ddot{y}_{11}\dot{x}_{11} - \ddot{x}_{11}\dot{y}_{11}) \cos^2 \gamma_2}{\dot{x}_{11}^2} & \text{Otherwise} \end{cases}$$

where the velocity and acceleration components in the 1 system are

$$\vec{\dot{x}}_{11} = [A_1]^{-1} \vec{\dot{x}}_{ee}$$

$$\vec{\ddot{x}}_{11} = [A_1]^{-1} \vec{\ddot{x}}_{ee} + [\dot{A}_1]^{-1} \vec{\dot{x}}_{ee}$$

c. Local Bank Attitude

Transformation from the local, north, east, and down system to the missile axis system for a commanded angle of attack, angle of sideslip, and bank angle is accomplished by

$$\dot{X}_{bb} = [A_\alpha] [A_\epsilon] [A_\omega] [A_{\gamma_1}] [A_{\gamma_2}] \dot{X}_{11}$$

$$\dot{X}_{bb} = [D]^{-1} [A] \dot{X}_{11}$$

where the azimuth velocity vector transformation is

$$[A_{\gamma_2}]^{-1} = \begin{bmatrix} \cos \gamma_2 & -\sin \gamma_2 & 0 \\ \sin \gamma_2 & \cos \gamma_2 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

and

$$[\dot{A}_{\gamma_2}]^{-1} = \dot{\gamma}_2 \begin{bmatrix} -\sin \gamma_2 & -\cos \gamma_2 & 0 \\ \cos \gamma_2 & -\sin \gamma_2 & 0 \\ 0 & 0 & 0 \end{bmatrix} = \begin{bmatrix} 0 & -\dot{\gamma}_2 & 0 \\ \dot{\gamma}_2 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} [A_{\gamma_2}]^{-1}$$

where the elevation velocity vector transformation is

$$[A_{\gamma_1}]^{-1} = \begin{bmatrix} \cos \gamma_1 & 0 & \sin \gamma_1 \\ 0 & 1 & 0 \\ \sin \gamma_1 & 0 & \cos \gamma_1 \end{bmatrix}$$

and

$$[\dot{A}_{\gamma_1}]^{-1} = \dot{\gamma}_1 \begin{bmatrix} -\sin \gamma_1 & 0 & \cos \gamma_1 \\ 0 & 0 & 0 \\ \cos \gamma_1 & 0 & -\sin \gamma_1 \end{bmatrix} = \begin{bmatrix} 0 & 0 & \dot{\gamma}_1 \\ 0 & 0 & 0 \\ -\dot{\gamma}_1 & 0 & 0 \end{bmatrix} [A_{\gamma_1}]^{-1}$$

The bank angle transformation is

$$[A_{\varphi}] = \begin{bmatrix} 1 & \hat{0} & 0 \\ 0 & \cos \varphi & \sin \varphi \\ 0 & -\sin \varphi & \cos \varphi \end{bmatrix}$$

The angle of attack transformation is

$$[A_{\alpha}]^{-1} = \begin{bmatrix} \cos \bar{\alpha} & 0 & +\sin \bar{\alpha} \\ 0 & 1 & 0 \\ -\sin \bar{\alpha} & 0 & \cos \bar{\alpha} \end{bmatrix}$$

$$[A_{\alpha}]^{-1} = \frac{1}{\alpha} \begin{bmatrix} -\sin \alpha & 0 & \cos \alpha \\ 0 & 0 & 0 \\ -\cos \alpha & 0 & -\sin \alpha \end{bmatrix} = \begin{bmatrix} 0 & 0 & \alpha \\ 0 & 0 & 0 \\ \alpha & 0 & 0 \end{bmatrix} [A_{\alpha}]^{-1}$$

The side slip angle transformation is

$$[A_{\beta}]^{-1} = \begin{bmatrix} \cos \bar{\beta}' & +\sin \bar{\beta}' & 0 \\ -\sin \bar{\beta}' & \cos \bar{\beta}' & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

where $\bar{\beta}' = \arctan [(\tan \bar{\beta})/(\sec \bar{\alpha})]$

$$[A_{\beta}]^{-1} = \frac{1}{\bar{\beta}'} \begin{bmatrix} -\sin \bar{\beta}' & \cos \bar{\beta}' & 0 \\ -\cos \bar{\beta}' & -\sin \bar{\beta}' & 0 \\ 0 & 0 & 0 \end{bmatrix} = \begin{bmatrix} 0 & \frac{1}{\bar{\beta}'} & 0 \\ \bar{\beta}' & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} [A_{\beta}]^{-1}$$

where

$$\frac{1}{\bar{\beta}'} = \begin{cases} 0 & \text{If } \cos \beta = 0 \\ \frac{\cos^2 \frac{1}{\beta}}{\cos^2 \bar{\beta}} & \left[\frac{1}{\bar{\beta}} \cos \bar{\alpha} + \bar{\alpha} \sin \bar{\beta} \cos \bar{\beta} \sin \bar{\alpha} \right] & \text{otherwise} \end{cases}$$

The instantaneous bank angle is

$$\varphi = \arctan [a_{\varphi 23} / a_{\varphi 22}]$$

$$[A_{\phi}] = [A_{\alpha}]^{-1} [A_{\beta}]^{-1} [D]^{-1} [A_1] [A_{\gamma 2}]^{-1} [A_{\gamma 1}]^{-1}$$

where

$$\begin{aligned} \dot{[A_{\phi}]} = & [A_{\beta}]^{-1} [A_{\alpha}]^{-1} [D]^{-1} [A_1] [A_{\gamma 2}]^{-1} [A_{\gamma 1}]^{-1} \\ & + [A_{\beta}]^{-1} [A_{\alpha}]^{-1} [D]^{-1} [A_1] [A_{\gamma 2}]^{-1} [\dot{A}_{\gamma 1}]^{-1} \\ & + [A_{\beta}]^{-1} [A_{\alpha}]^{-1} [\dot{D}]^{-1} [A_1] [A_{\gamma 2}]^{-1} [A_{\gamma 1}]^{-1} \\ & + [A_{\beta}]^{-1} [A_{\alpha}]^{-1} [E]^{-1} [\dot{A}_1] [A_{\gamma 2}]^{-1} [A_{\gamma 1}]^{-1} \\ & + [A_{\beta}]^{-1} [A_{\alpha}]^{-1} [D]^{-1} [A_1] [\dot{A}_{\gamma 2}]^{-1} [A_{\gamma 1}]^{-1} \\ & + [A_{\beta}]^{-1} [A_{\alpha}]^{-1} [D]^{-1} [A_1] [A_{\gamma 2}]^{-1} [\dot{A}_{\gamma 1}]^{-1} \end{aligned}$$

$$\dot{\phi} = (180/\pi) \quad (a_{\phi 22} \dot{\phi}_{23} - a_{\phi 23} \dot{\phi}_{22})$$

J.

Inertial Values

The inertial values are referenced to a system fixed in, but not rotating with the earth.

The missile energy per unit mass is

$$E/m = GM/r_c - GM/r_i + V_i^2/2$$

where zero potential energy is assumed at the surface of the reference body, r_c is the input reference body radius, G is computed from input, and r_c and V_i are the missile distance from earth center and inertial velocity respectively.

The inertial velocity components are

$$\begin{aligned}\dot{x}_{111} &= \dot{x}_{11} \\ \dot{y}_{111} &= \dot{y}_{11} + \omega r_c \cos \rho \\ \dot{z}_{111} &= \dot{z}_{11}\end{aligned}$$

$$V_I = (\dot{x}_{11}^2 + \dot{y}_{111}^2 + \dot{z}_{11}^2)^{1/2}$$

The flight path angles are

$$\gamma_{11} = \begin{cases} 0 & \text{If } V_I = 0 \\ \arcsin (-\dot{z}_{11}/V_I) & \text{Otherwise} \end{cases}$$

and

$$\gamma_{21} = \begin{cases} \gamma_{i0} & \text{If } \dot{y}_{111} = \dot{x}_{11} = 0 \\ \arctan (\dot{y}_{111}/\dot{x}_{11}) & \text{Otherwise} \end{cases}$$

with

$$-90^\circ \leq \gamma_{11} < 90^\circ$$

$$0 \leq \gamma_{21} < 360^\circ$$

where γ_{i0} is the input azimuth angle.

e. Generalized Coordinates

The g system, introduced below, can be used to obtain vehicle position and velocity components in a coordinate system oriented about the c system. The system also is a part of the guidance system model. The orientation of the g system is specified by input Euler angles which perform the following rotations: θ_g about the Y_c -axis, ψ_g about the resulting Z-axis, and ϕ_g about the X-axis. The components are computed from the following

if the input "PL-KB" is nonzero or if the type of flight, T_y , is four or five or the current stage σ_{gk} is nonzero.

$$\ddot{x}_{gg} = [A_g] \ddot{x}_{ee}$$

$$\dot{x}_{gg} = [A_g] \dot{x}_{ee}$$

$$\ddot{x}_{gg} = [A_g] \ddot{x}_{ee}$$

where

$$[A_g] = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \psi_g & \sin \psi_g \\ 0 & -\sin \psi_g & \cos \psi_g \end{bmatrix} \begin{bmatrix} \cos \psi_g & \sin \psi_g & 0 \\ -\sin \psi_g & \cos \psi_g & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \cos \psi_g & 0 & -\sin \psi_g \\ 0 & 1 & 0 \\ \sin \psi_g & 0 & \cos \psi_g \end{bmatrix}$$

The orientation of the g system is shown in Figure 17 for ψ_g and ϕ_g equal to zero.

6. SVC Requirements and Duty Cycle

The following parameters are calculated and stored in the L-7000-7999 block, if $K_{dc} \neq 0$ (I-671).

| <u>L-No.</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|--------------|-----------------------|--|--------------|
| 7000 | \bar{I} | Motor thrust impulse for TVC duty cycle stage. | lb-sec |
| 7001 | \bar{I}_v | Motor vacuum thrust impulse for TVC duty cycle stage. | lb-sec |
| 7002 | x_e | TVC duty cycle stage thrust vector point body station. | ft |
| 7003 | x_{nf} | Body station of nozzle flange of the TVC design stage. Input in L-680. | ft |
| 7004 | δ_{me} | Design maximum vector angle for TVC duty cycle stage. Input in L-681. | deg |
| 7005 | I_{SPM} | Main table specific impulse for the TVC duty cycle stage. Input in L-(K _{dc}) 010. | sec |
| 7006 | $\bar{\omega}_c$ | Slew frequency used in the TVC design stage slew rate calculation. | rad/sec |
| 7007 | δ_s | Control system design slew rate for TVC design stage. | deg/sec |
| 7008 | $\bar{\delta}_s$ | Slew angle for TVC design stage. | deg |
| 7009 | \bar{I}_p | Pitch control thrust impulse per control motor from TVC duty cycle initiation to stage termination. | lb-sec |
| 7010 | $\bar{I}_{\delta p}$ | Integral of the pitch angular thrust vectoring velocities from TVC duty cycle stage initiation to stage termination. | deg |
| 7011 | $t_{\eta p}$ | Stage time at which maximum magnitude pitch thrust vector deflection angle occurs during the TVC design stage (δ_{pmax}). | sec |
| 7012 | η_p | Ratio of the delivered thrust (F) to vacuum thrust (Fvac) at maximum magnitude pitch TVC deflection angle (δ_{pmax}). | dim |
| 7013 | $\dot{\delta}_{pmax}$ | Maximum pitch thrust vector deflection angular rate, for the TVC design stage. | deg/sec |
| 7014 | $\bar{\delta}_{pmax}$ | Maximum magnitude pitch thrust vector deflection angle, per control motor for the TVC design stage. | deg |

| <u>I-No.</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|--------------|------------------------|--|--------------|
| 7015 | \bar{I}_y | Yaw control thrust impulse per control motor from TVC stage initiation to stage termination. | lb-sec |
| 7016 | $\bar{I}_{\delta y}$ | Yaw deflection rate integral per vehicle control motor. | deg |
| 7017 | $t_{\eta y}$ | Stage time at which maximum magnitude yaw thrust vector deflection angle occurs during the TVC design stage ($\delta_{y\max}$). | sec |
| 7018 | η_y | Ratio of the delivered thrust (F) to vacuum thrust (F_{vac}) at maximum magnitude yaw TVC deflection angle ($\delta_{y\max}$). | dim |
| 7019 | $\dot{\delta}_{y\max}$ | Maximum yaw thrust vector deflection angular rate, for the TVC design stage. | deg/sec |
| 7020 | $\delta_{y\max}$ | Maximum magnitude yaw thrust vector deflection angle, per control motor for the TVC design stage. | deg |
| 7021 | $q\alpha'_{\max}$ | Product of the maximum absolute value of the dynamic pressure-angle of attack for the TVC design stage. | lb-deg/sq ft |
| 7022 | $q_{q\alpha'}$ | Dynamic pressure at maximum $q\alpha'$ during the TVC duty cycle stage. | lb/sq ft |
| 7023 | $t_{q\alpha}$ | TVC duty cycle stage time at maximum $q\alpha'$. | sec |
| 7024 | $C_{Nq\alpha}$ | Aerodynamic normal force coefficient at maximum $q\alpha'$ during the TVC duty cycle stage. | 1/deg |
| 7025 | $M_{q\alpha}$ | Mach number at maximum $q\alpha'$ during the TVC duty cycle stage. | dim. |
| 7026 | $\bar{\delta}_{ave}$ | Average TVC deflection angle per control motor for the TVC design stage. | deg |
| 7027 | K_{dc} | Stage number of the TVC duty cycle stage. Input in I.-671. | dim. |
| 7028 | D_B | TVC duty cycle stage case diameter from axial force reference area. | in. |
| 7029 | A_{FW1} | Stage I vacuum thrust to liftoff weight used in the vehicle characteristics pertinent to roll requirements. | g's |
| 7030 | t_B | TVC duty cycle stage time. | sec |

| <u>L-No.</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|--------------|--------------------|---|--------------|
| 7031 | F_{vave} | TVC duty cycle stage average vacuum thrust. | lb |
| 7032 | W_o | TVC duty cycle stage liftoff weight used in the roll control requirements. | lb |
| 7033 | K_{PFV} | Ratio of motor chamber pressure to vacuum thrust of the main thrust table of the TVC design stage. | 1/sq in. |
| 7034 | $\bar{\epsilon}_d$ | Nozzle average expansion ratio for TVC design stage. Input in L-(K _{dc}) 013. | dim. |
| 7035 | \bar{A}_t | Nozzle throat area for the main motor of the TVC design stage. | sq in. |
| 7036 | $\bar{\gamma}_d$ | Ratio of specific heats of the rocket motor exhaust gases of the TVC design stage. | dim. |
| 7037 | P_{ca} | Action time average motor chamber pressure for the TVC design duty cycle stage. | lb/sq in. |
| 7038 | C^* | Rocket motor propellant characteristic velocity for the TVC design duty cycle stage. | ft/sec |
| 7039 | W_{TVC} | Estimated TVC system fixed weight. Used in TVC design stage for the reflly option. Input in L-677. | lb |
| 7040 | W_{exi} | Estimated weight of the TVC system expended weight during the TVC design stage during the original vehicle flight. Input in L-678. | lb |
| 7041 | I_{spaug} | Estimated TVC system caused specific impulse augmentation (positive) or degradation (negative). Used in trajectory TVC design program reflly. Input in L-679. | sec |
| 7044 | n_m | Number of motors in the stage cluster | dim. |
| 7045 | n_c | Number of control nozzles for the cluster motor logic. | dim. |
| 7046 | Δ_{dc} | Number TVC duty cycle t_b data points. | dim. |
| 7047 | M_{hzmaz} | Maximum of the absolute value pitch fin hinge torque for the TVC design stage. | ft-lb |

| <u>L-No.</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|--------------|---------------------|--|----------------------|
| 7048 | M_{hymax} | Maximum of the absolute value yaw fin hinge torque for the TVC design stage. | ft-lb |
| 7052 | $h_{q\alpha'}$ | Altitude of TVC duty cycle stage maximum $q\alpha'$. | ft |
| 7053 | $P_{q\alpha'}$ | Atmospheric pressure of TVC duty cycle stage maximum $q\alpha'$. | lb/sq ft |
| 7054 | \bar{I}_{VM} | Integral of the vacuum thrust of the input main thrust table in the TVC duty cycle stage. Input in L-(K _{dc}) 005. | lb-sec |
| 7055 | \bar{W}_{MO} | Initial main weight for the TVC duty cycle stage. Input in L-(K _{dc}) 006. | lb |
| 7056 | \bar{K}_{tm} | TVC duty cycle stage, the main switching time multiplier. Input in L-(K _{dc}) 009. | dim. |
| 7057 | $\alpha_{q\alpha'}$ | Angle of attack in pitch at TVC design stage maximum $q\alpha'$. | deg |
| 7058 | $\beta_{q\alpha'}$ | Angle of side slip in yaw at TVC design stage maximum $q\alpha'$. | deg |
| 7059 | P_{cmax} | Maximum main motor chamber pressure in TVC duty cycle stage. | lb/sq ft |
| 7060 | \dot{A}_{tmax} | Pintle System required throat area rate. | in ² /sec |
| 7061 | I_{At} | Integral of the absolute value of the pintle throat area rate. | in |
| 7062 | F_{max} | Pintle motor maximum vacuum thrust | lb |
| 7063 | P_{cmax} | Pintle motor chamber pressure at maximum vacuum thrust | lb/in. ² |
| 7064 | ϵ_{max} | Pintle motor expansion ratio at maximum vacuum thrust | dim. |
| 7065 | A_{tmin} | Pintle motor throat area at maximum vacuum thrust | in. ² |

| <u>L-No.</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|--------------|------------------|---|---------------------|
| 7066 | C_{fmax} | Pintle motor vacuum thr coefficient at maximum vacuum thrust | dim. |
| 7067 | F_{min} | Pintle motor minimum vacuum thrust | lb |
| 7068 | P_{cmin} | Pintle motor chamber pressure at minimum vacuum thrust | lb/in. ² |
| 7069 | ϵ_{min} | Pintle motor expansion ratio at minimum vacuum thrust | dim. |
| 7070 | A_{tmax} | Pintle motor throat area at minimum vacuum thrust | in. ² |
| 7071 | C_{fmin} | Pintle motor vacuum thrust coefficient at minimum vacuum thrust | dim. |
| 7072 | A_{xmax} | Motor extinguishment throat area | in. ² |
| 7073 | A_{tmin} | Pintle motor duty cycle minimum throat area | in. ² |
| 7074 | A_{tmx} | Pintle motor duty cycle maximum throat area | in. ² |
| 7100 7199 | t_{Bq} | Stage time at which TVC duty points occur. | sec |
| 7200 7299 | δ_{Pq} | Pitch thrust deflection angle at t_{Bq} . | deg |
| 7300 7399 | δ_{Yq} | Output modified yaw thrust deflection angle at t_{Bq} for TVC design stage. | deg |
| 7400 7499 | F_q | Delivered motor thrust (F) at t_{Bq} during TVC design stage. | lb |
| 7500 7599 | X_{cgq} | Vehicle center-of-gravity at t_{Bq} ; the TVC duty cycle point. | ft |
| 7600 | F_{vacq} | Vacuum motor thrust during the TVC design stage (\bar{F}_{vac}) at t_{Bq} . | lb |
| 7700 | \dot{W}_q | Output motor weight flow (W) at t_{Bq} the | lb/sec |

a. Slew Rate

The calculation of maximum TVC slew rate is computed as follows:

$$\bar{\omega}_S = 0.22797 \bar{\omega}_c \bar{\delta}_S$$

where $\bar{\omega}_S$ is the design slew rate, $\bar{\delta}_S$ is the pitch slew angle. The 0.45594 ($\omega_c/2$) factor is created by the maximum velocity of the response to a unit input step function at one-half band width frequency. If the input does not have ω_c , then the following logic is used for evaluating the actuator system band width frequency.

Slew Frequency

$$\bar{\omega}_c = \begin{cases} \omega_s & \text{If } \omega_s \neq 0 \\ \omega_c & \text{If } \omega_s = 0 \text{ and } \omega_c \neq 0 \\ \text{anti } \ln [12.146979 - 1.3829872 (\ln W_{01})] \\ + 0.062446656 (\ln W_{01})^2 - 0.00093655891 (\ln W_{01})^3] & \text{Otherwise} \end{cases}$$

where W_{01} is the stage I liftoff weight, ω_s is the input slew frequency and ω_c is the input second order TVC frequency.

Slew Angle Amplitude

The deflection terms of the slew rate are computed as follows:

$$\delta'_{Pmax} = \begin{cases} \text{The maximum magnitude pitch deflection in the region where} \\ h_o < h < h_\beta \text{ and } h_\alpha < h \end{cases}$$

and

$$\delta_{PW} = \begin{cases} |\delta_{PM} - \delta_{PL}| \\ \text{or} \\ |\delta_{PM} - \delta_{PH}|, \text{ whichever is greater} \end{cases}$$

$$\delta_{YW} = \begin{cases} |\delta_{YM} - \delta_{YL}| \\ \text{or} \\ |\delta_{YM} - \delta_{YH}|, \text{ whichever is greater} \end{cases}$$

where δ_{PM} and δ_{YM} are the maximum magnitude pitch and yaw deflection angle in the region where $h_\beta \leq h \leq h_\alpha$ and δ_{PL} , δ_{PM} , δ_{YL} , and δ_{YH} are the pitch and yaw deflections at the input altitudes h_β and h_α .

If h_β falls outside the TVC design stage altitude regime, set $\delta_{PL} = \delta_{YL} = 0$.

$$\delta_S = \text{MAX} (|\delta'_{Pmax}|, \delta_{PW}, \text{ and } \delta_{YW})$$

$$\delta_S = (n_m / n_c) \delta_S$$

where n_m and n_c are the internally calculated number of motors in a cluster and the number of control nozzles in that cluster respectively.

It is suggested that the altitudes h_β and h_α correspond to the altitude at which the wind shears start and stop, respectively. Using these altitudes will assure that the maximum thrust vector deflection used in evaluating design slew rates will be approximately compatible with the actual system requirements for near step function inputs.

b. Duty Cycle Storage Logic

The values of $\bar{\delta}_{pq}$, $\bar{\delta}_{yq}$, x_{cgq} , F_q , F_{vacq} , \dot{W}_q at t_{Bq} are stored for the k_{dc} -th stage for use in the hardware design subroutine.

Where

$\bar{\delta}_{pq}$ is the modified pitch thrust deflection angle ($\bar{\delta}_p$) at t_{Bq} (deg),

$\bar{\delta}_{yq}$ is the modified yaw thrust deflection angle ($\bar{\delta}_y$) at t_{Bq} (deg),

x_{cgq} is the instantaneous vehicle center-of-gravity at t_{Bq} (ft),

F_q is the delivered motor thrust (\bar{F}) at t_{Bq} (lb),

F_{vacq} is the vacuum motor thrust (\bar{F}_{vac}) at t_{Bq} (lb),

\dot{W}_q is motor weight flow (\dot{W}) at t_{Bq} (lb/sec)

Where

t_{Bq} is the stage compute time just greater than or equal to Jt_f^i/Δ_{dc} ($J = 0, 1, 2, \dots, \Delta_{dc}$) and t_B at stage termination. If any of these conditions coincide, one value shall be stored. The number of t_B data points shall be counted and stored as n_{dc} .

Where

t_c^i is greatest, t_j^K or $t_{cj}^i t_c^K$ ($j = 1, 2, \text{ or } 10$) value on the input thrust time values for the TVC duty cycle stage,

Δ_{dc} is the input value of number of desired duty cycle points (99 maximum) if input zero, set equal to 50,

k_{dc} is the input stage number of the TVC duty cycle stage,

K_t and K_{tc} are the switching time multipliers for the main and complementary thrust tables.

c. Modified Thrust Deflection Angle--The modified thrust deflection angle is

$$\bar{\delta}_p = [\delta_p + A_L \sin (\omega_L [180/\pi] [t - t_k])] (n_m/n_c)$$

$$\bar{\delta}_y = [\delta_y + A_L \sin (\omega_L [180/\pi] [t - t_k])] (n_m/n_c)$$

$$\bar{\dot{\delta}}_p = [\dot{\delta}_p + A_L \omega_L \cos (\omega_L [180/\pi] [t - t_k])] (n_m/n_c)$$

$$\bar{\dot{\delta}}_y = [\dot{\delta}_y + A_L \omega_L \cos (\omega_L [180/\pi] [t - t_k])] (n_m/n_c)$$

Where

$\delta_{p, y}$ are the pitch and yaw thrust deflection angles (deg),

$\dot{\delta}_{p, y}$ are the pitch and yaw thrust deflection angular rates (deg/sec)

A_L is the amplitude of the limit cycle (deg),

t is the time (sec) and t_k is stage initiation time (sec),

ω_L is the frequency of the limit cycle (rad/sec),

n_m is internally calculated number of motors in a cluster (dim),

n_c is the number of control motors in the cluster (dim),

d. Modified Duty Cycle Thrust Vector Integrals and Weights Flow for a Single Motor

The thrust vector integrals and weight flow per motor of a cluster configuration is

$$\bar{F} = F/n_m$$

$$\bar{F}_{vac} = F_{vac}/n_m$$

$$\dot{W} = \dot{W}/n_m$$

$$\bar{I}_v = I_v/n_m$$

$$\bar{I} = I/n_m$$

$$\bar{I}_p = I_p/n_c$$

$$\bar{I}_y = I_y/n_c$$

$$\bar{I}_{SP}^* = (n_m/n_c) \bar{I}_{SP}^*$$

$$I_{SY}^* = (n_m/n_c) I_{SY}^*$$

Where

\bar{F} is the instantaneous motor thrust (lb),

\bar{F}_{vac} is the instantaneous vacuum motor thrust (lb),

\dot{W} is the instantaneous motor weight flow (lb/sec),

\bar{I}_v is the motor vacuum thrust impulse from TVC duty cycle stage initiation to stage termination (lb-sec),

I_v is the total vehicle vacuum thrust impulse from TVC duty cycle stage initiation to stage termination (lb-sec),

I is the total vehicle delivered thrust impulse from TVC duty cycle stage initiation to stage termination (lb-sec).

\bar{I}_p is the pitch control thrust impulse per control motor from TVC duty cycle stage initiation to stage termination (lb-sec),

$\bar{I}_{\epsilon p}$ is the pitch deflection rate integral per vehicle control motor (deg),

$\dot{I}_{\epsilon p}$ is the integral of pitch angular thrusting vectoring velocity from stage initiation (deg).

Vehicle Characteristics Pertinent to Roll Requirement

Average Stage Vacuum Thrust

$$F_{vave} = I_v / t_B$$

where I_v and t_B are the TVC duty cycle stage vacuum impulse and stage time respectively at stage termination.

TVC Stage Liftoff Weight

$W_o = W_o(Kdc)$ is the vehicle weight at TVC duty cycle stage initiation.

Stage I Vacuum Thrust to Weight

$$A_{FW1} = \begin{cases} A_{FW1} & \text{If } A_{FW1} \neq 0 \\ (I_v/t_{B1})/W_{o1} & \text{If } K_k = 1 \\ 3.0 & \text{Otherwise} \end{cases}$$

Base Diameter

$$D_B = 24.0 (S_{RC_{kdc}} / \pi \tau)^{\frac{1}{2}}$$

Maximum Dynamic Pressure - Angle of Attack

The maximum q' and the corresponding normal force coefficient and stage time are saved for the TVC duty cycle stage.

$$C_{Noq} = |N_z| / [S_{RN} (q\alpha')] \text{ at } q\alpha' \text{ max}$$

where N_z is the normal force, S_{RN} is the aerodynamic normal reference area and $q\alpha'$ is the dynamic pressure-angle of attack product.

$$q\alpha'_{\text{max}} = q\alpha' \text{ at maximum } q\alpha'$$

$$t_{q\alpha} = t_B \text{ at maximum } q\alpha' \text{ (stage time)}$$

$$M_{q\alpha} = \text{Mach number at maximum } q\alpha'$$

$$q_{q\alpha}' = \text{Dynamic pressure at maximum } q\alpha'$$

$$h_{q\alpha}' = \text{Altitude at maximum } q\alpha'$$

$$\alpha_{q\alpha}' = \text{Angle of attack at } q\alpha'$$

$$\beta_{q\alpha}' = \text{Angle of side slip at } q\alpha'$$

Nozzle Parameter

The parameters input of internally calculated in the program germane to the nozzle design are R_{PFV} , ϵ_d , \bar{A}_t , I_{spM} , P_{ca} , C^* , and γ_d for the TVC design stage. ϵ_d and I_{spM} are input and γ_d is specified in Main Thrust Weight logic.

Motor Chamber Pressure to Vacuum Thrust Ratio

$$R_{PFV} = \begin{cases} 0 & \text{If } \epsilon_d = 0 \\ PCOFMV \cdot n_m / 144 & \text{Otherwise} \end{cases}$$

where PCOFMV is the ratio of chamber pressure to vehicle main vacuum thrust calculated in the nozzle separated flow logic, n_m is the number of motors in a cluster and ϵ_d is the input nozzle expansion ratio.

Motor Nozzle Throat Area

$$\bar{A}_t = \begin{cases} 0 & \text{If } \epsilon_d = 0 \\ 144 A_{eM} / (\epsilon_d n_m) & \text{Otherwise} \end{cases}$$

where A_{eM} is the input nozzle exit area.

Action Time Average Motor Chamber Pressure

$$P_{ca} = \bar{I}_v \cdot R_{PFV} / t_B$$

where \bar{I}_v is the motor vacuum thrust impulse from TVC duty cycle stage initiation to stage termination, and t_B is the TVC duty cycle stage time.

Rocket Motor Propellant Characteristic Velocity

$$C^* = \begin{cases} 0 & \text{If } \epsilon_d = 0 \\ \text{PCOFMV} \cdot A_e^M \cdot \bar{g}_e \cdot I_{spM} / \epsilon_d & \text{Otherwise} \end{cases}$$

where I_{spM} is the input vacuum specific impulse for the main thrust weight table.

Average Thrust Vector Deflection Angle

$$\bar{\delta}_{ave} = \arcsin \{(\bar{I}_p + \bar{I}_y) / \bar{I}\}$$

where \bar{I}_p and \bar{I}_y and \bar{I} are the pitch control thrust impulse, yaw control thrust impulse delivered thrust impulse per control motor for the TVC duty cycle stage.

e. Thrust Modulation Control Related Parameter

If $D_p \neq 0$ for the TVC design stage the following parameters are calculated and stored.

Pintle System Required Throat Area Rate (in^2/sec)

$$\dot{A}_{t\max} = 0.45594 \omega_p (A_{x\max} - A_{x\min})$$

where ω_p is the pintle control frequency (rad/sec), $A_{x\max}$ is the maximum extinguishment throat area and $A_{x\min}$ is the minimum throat area and 0.45594 is the factor created by the maximum velocity of the response to a unit input step function at a band width frequency ω_p and amplitude of $(A_{x\max} - A_{x\min})$.

Integral of Pintle area rate (in)

$$I_{At} = \int_0^{t_B} \dot{A}_t dt$$

where \dot{A}_t is the rate change of throat area and t_B is the stage time.

Minimum Throat Conditions

The minimum throat area value is evaluated from each compute interval and the corresponding values of thrust coefficient, chamber pressure, vacuum thrust, and nozzle expansion ratio are also saved.

$$A_{t\min} = A_t$$

$$C_{f\max} = C_{FI}$$

$$F_{\max} = F_{MV}$$

$$\epsilon_{\max} = \epsilon$$

Minimum Throat Conditions

The minimum throat area value is evaluated from each computer interval and the corresponding values of thrust coefficient chamber pressure, vacuum thrust, and nozzle expansion ratio are also saved.

$$A_{tmin} = A_T$$

$$C_{fmax} = C_{FI}$$

$$F_{max} = F_{MV}$$

$$\epsilon_{max} = \epsilon$$

Maximum Throat Conditions

The maximum throat area value is evaluated from each compute interval and the corresponding values of thrust coefficient, chamber pressure, vacuum thrust and nozzle expansion ratio are also saved.

$$A_{tmax} = A_T$$

$$C_{fmin} = C_{FI}$$

$$F_{min} = F_{MV}$$

$$\epsilon_{max} = \epsilon$$

K. TRAJECTORY LOGIC

Logic governing stage initiation and termination, numerical integration step size, and the times at which trajectory values are printed are defined.

1. Initiation - Termination

a. Trajectory Initiation

It is possible to start a trajectory at any stage initiation. Besides the initial values required for the differential equations and the values for vehicle characteristics, the following additional data are required input: (1) the stage designation parameter, K_k ($k = 1, 2, 3$, or 4), (2) the trajectory start time, t_o , (3) the type of flight segment, T'_{yj} ($j = 1, 2, \dots$, or 16), and (4) the mode segment, M'_{oj} ($j = 1, 2, \dots$, or 10). There are exceptions to the requirement of inputting the last two items. These are explained in Mode and Flight Control Sections.

b.

Stage Termination

Each of the four stages will end when

$$\Delta_k = 0 \quad (k = 1, 2, 3, 4)$$

with

$$\Delta_k = \sigma_{Sk} - k_{3k}$$

where σ_{Sk} is the achieved value of a quantity designated by code input, k_{3k} is input. If σ_{Sk} is designated as stage time, t_B or time, t , then the input k_{3k} is multiplied by the input k_{tk} ,

when $\Delta_k = 0$, let $t = t_{Sk}$

If $\sigma_{S1} = 0$, halt the run and print the reason.

If $\sigma_{S2} = 0$, only one stage is desired and cutoff occurs

when $\Delta_1 = 0$

If $\sigma_{S3} = 0$, two-stage operation is desired and cutoff occurs

when $\Delta_2 = 0$

If $\sigma_{S4} = 0$, three-stage operation is desired and cutoff occurs

when $\Delta_3 = 0$

If σ_{S1} , σ_{S2} , σ_{S3} , and $\sigma_{S4} \neq 0$, four-stage operation is desired and cutoff occurs

when $\Delta_4 = 0$

Unless other logic applies, the run ends when cutoff occurs.
When the criterion for leaving a stage has been satisfied, that stage
is not re-entered during the trajectory.

c. Staging Values

The values of specified values at the termination of the k-th stage are made available to the hunting procedure control by specifying input T_{Bj} and σ_{Bj} ($j = 1, 2, \dots, 5$). The σ_{Bj} specifies the achieved value of the parameter designated by code input at the termination of the input T_{Bj} stage. Certain selected trajectory parameters, i.e., $V_I, h, \gamma_1, W, S_f, L_F, L_D, L_g, L_v, \Delta v, a_{xb}, q, I_v, h_p, h_a, t_f, \gamma_{lif}$, and V_{If} for stages 1, 2, 3 and 4, are also available to the hunting procedure.

d.

Trajectory Halts

Certain computations and parameter values result in program logic terminating the run. The error which causes the abort and the location of the error are identified by the printout. The printout format is discussed in the final section of this volume.

2. Compute Time

The following are computed for all modes:

1. The main and complementary thrust-weight switching times.
2. The times when the trajectory begins and each stage ends.
3. The times each segment of flight in the altitude control table and mode region ends.
4. The time when the special print is satisfied.
5. The times when weight jettison occur.
6. The times when TVC gains change.
7. The time when the main print occur.
8. The time when the auxiliary print occur.
9. If the wind table altitude multiplier K_h is nonzero at the time when the input wind altitude occurs.
10. The time each segment of target dynamical switch conditions occurs.
11. Time of lift off.
12. The time each segment of the TMC table ends.
13. The time each segment of the roll control values tables ends.

a.

Variable Compute Interval with Accuracy Check

The numerical integration method utilized in the trajectory program is a fifth-order Runge-Kutta-Merson with a fourth-order/fifth-order accuracy check routine. Generally this routine functions as follows.

Let y be the vector to be integrated (code 5701 thru 5750) and let y' be the derivative vector (5751 thru 5800). The differential equation to solve is

$$y' = f(y, t)$$

Following standard Runge-Kutta notation, define

$$k_1 = hf [y_n, t_n] / 3$$

$$k_2 = hf [y_n + k_1, t_n + h/3] / 3$$

$$k_3 = hf [y_n + (k_1 + k_2)/2, t_n + h/3] / 3$$

$$k_4 = hf [y_n + 3k_1/8 + 9k_3/8, t_n + h/2] / 3$$

$$k_5 = hf [y_n + 3k_1/2 - 9k_3/2 + 6k_4, t_n + h] / 3$$

Then two independent estimates of y are given by

$$y_{n+1} = y_n + 3k_1/2 - 9k_3/2 + 6k_4 + O(h^4)$$

and

$$y_{n+1} = y_n + (k_1 + 4k_4 + k_5)/2 + O(h^5)$$

The second of these is used in this program. An estimate of the error is the difference between the two, or

$$e = \left| k_1 - 9k_3/2 + 4k_4 - k_5/2 \right|$$

The error index is calculated as

$$E_i = \frac{e_i}{R_i + R_i |Y_i|} \quad i = 1, 2, \dots, 50$$

where the R_i are error tolerances, described below.

| <u>Code</u> | <u>Parameter</u> | <u>R</u> | <u>Code</u> | <u>Parameter</u> | <u>R</u> |
|-------------|------------------|----------|-------------|------------------|----------|
| 5701 | XDEE | .01 | 5726 | VN | .001 |
| 5702 | YDEE | .01 | 5727 | VC | .001 |
| 5703 | ZDEE | .01 | 5728 | GAMT | .001 |
| 5704 | XEE | .001 | 5729 | ZETAT | .001 |
| 5705 | YEE | .001 | 5730 | HT | .001 |
| 5706 | ZEE | .001 | 5731 | ST | .001 |
| 5707 | QB | .1 | 5732 | STC | .001 |
| 5708 | RB | .1 | 5733 | DB | .01 |
| 5709 | PR | .1 | 5734 | PC | .1 |
| 5710 | THETAB | .01 | 5735 | AT | .1 |
| 5711 | PSIB | .01 | 5736 | WPR | .01 |
| 5712 | PHIB | .01 | 5737 | IMP | .01 |
| 5713 | DELDP | .01 | 5738 | IV | .001 |
| 5714 | DELDY | .01 | 5739 | IP | .1 |
| 5715 | DELDR | .01 | 5740 | IY | .1 |
| 5716 | DELP | .001 | 5741 | IAT | 1.0 |
| 5717 | DELY | .001 | 5742 | Open | |
| 5718 | DELR | .001 | 5743 | LF | 1.0 |
| 5719 | FR | .01 | 5744 | DELTAV | 1.0 |
| 5720 | WR | .1 | 5745 | IR | 1.0 |
| 5721 | FRC | .1 | 5746 | LD | 1.0 |
| 5722 | THETAM | .01 | 5747 | LGG | .1 |
| 5723 | PSIM | .01 | 5748 | HE | 10.0 |
| 5724 | PHIM | .01 | 5749 | Open | |
| 5725 | VT | .001 | 5750 | Open | |

The error tolerances may be modified by input. In input locations L280 thru L303, up to 12 pairs of index/multiplier may be entered. For any index in the range of 1 thru 50, the corresponding values of R_i are multiplied by the input multiplier $A'r$.

The maximum E_i (EMAX) is employed to control the integration step size:

If $EMAX \geq 1.0$, halve the step size

If $EMAX \leq 0.031$, triple the step size

b. Specified Maximum Compute Interval

If the compute interval is input in the compute interval table, the interval is limited as follows:

| <u>Interval</u> | <u>Maximum Compute Interval</u> |
|--------------------------|-------------------------------------|
| $t \leq t_{c1}$ | Δt_{c1} |
| $t_{c1} < t \leq t_{c2}$ | Δt_{c2} |
| ... | . |
| $t_{c7} < t \leq t_{c8}$ | Δt_{c8} |

t_{cj} and Δt_{cj} ($j = 1, 2, \dots, 8$) are input and t is the instantaneous time.

If $t > t_{cJ}$ where the subscript J refers to the last input point in the compute interval table, the compute interval is unlimited.

c.

Discontinuity Print

The discontinuity print will occur when the input α_{Dj} specifies the first "L" number of an input table row.

| <u>TABLE</u> | <u>CODE</u> | <u>PARAMETER</u> |
|-----------------------------|---------------|----------------------------------|
| Jettison Weight | W_{JTj} | (j = 1, 2, ..., 8) |
| Special Print | σ_{tj} | (j = 1, 2, ..., 8) |
| Attitude Control | y_j | (j = 1, 2, ..., 16) |
| Wind Profile | h_j | (j = 1, 2, ..., 30) |
| Mode Control | M_{yj} | (j = 1, 2, ..., 10) |
| Main Thrust-Weight | t'_j | (j = 2, 3, ..., 25) Back side |
| Complementary Thrust-Weight | t'_{Cj} | (j = 2, 3, ..., 25) Back side |
| Gains | K_{DPj} | (j = 1, or 2) |
| Target dynamical condition | t_{Tj} | (j = 1, 2, ..., 10) |
| TMC | F_{yj} | (j = 1, 2, ..., 7) |
| Roll Control | K_{DRj} | (j = 1, or 2) |

d.

Variable Break-up Tolerances

Compute internal break ups are used to exactly compute discontinuities for the following conditions:

1. Attitude Control Table
2. Gains (TVC) Table
3. Weight Jettison Table
4. Special Print Table
5. Wind Profile Table
6. Mode Control Table
7. Staging
8. Target Dynamical Conditions Table
9. Main Thrust-Weight Table
10. Complementary Thrust-Weight Table
11. Lift off
12. TMC Table
13. Target Dynamical Condition Table
14. Roll Control Table

A break-up will occur whenever either delta time or delta x becomes less than the corresponding tolerance, DT_{min} or DX_{min} , where delta x is the difference between a break-up variable and its target value, and

$$DT_{min} = A_t + B_t \text{ TIME}$$

$$DX_{min} = A_x + B_x |x_{target}|$$

The default values, which are used unless overridden by positive input values, are

$$A_t = 2.E-4$$

$$B_t = 1.E-5$$

$$A_x = 1.E-9$$

$$B_x = 1.E-5$$

Experience has shown these values to be reasonable most of the time. There is probably little danger in using values that are too small; the principal effect would be an increase in running time although it is possible to cause the integration routine to fail (with appropriate messages and a dump) if the tolerances are too tight. Looser tolerances allow a more random flight, and could cause the hunting procedures to fail.

Any given break-up point will depend almost entirely on only one of the four break-up tolerance parameters. In general, the following rules apply:

A. If the break-up variable is changing slowly with time, DX_{min} will control:

1. if $|x_{target}|$ is small, A_x will control
2. if $|x_{target}|$ is large, B_x will control

B. If the break-up parameter is changing rapidly,
 DT_{\min} will control

1. if TIME is small, A_t will control

2. if TIME is large, B_t will control

3. Print

Trajectory print times are discussed. Two blocks of printout are featured, i.e., the main and auxiliary prints. The main print contains printlines A through and succeeding printlines that are given when special criteria are met. The auxiliary print is given in two lines which are labeled Printline Z and ZZ. Print times of the main and auxiliary prints are controlled by the logic given below.

a. Main Print Interval

Printout of the main print occurs when the following times are achieved:

| <u>Interval</u> | <u>Print Time</u> |
|--------------------------|--------------------------------|
| $t \leq t_{p1}$ | $t = n \Delta t_{p1}$ |
| $t_{p1} < t \leq t_{p2}$ | $t = t_{p1} + n \Delta t_{p2}$ |
| $t_{p7} < t \leq t_{p8}$ | $t = t_{p7} + n \Delta t_{p8}$ |

where t_{pj} and Δt_{pj} ($j = 1, 2, \dots, 8$) are input.

If $\Delta t_{pj} < 0$, every compute point is output.

b. Special Print

The main print is given when the logic given below is satisfied.

With σ_{tj} ($j = 1, 2, \dots, 8$) the achieved value of a parameter designated by code input and K_{tj} the input value of that parameter, then, the main print is printed when $\sigma_{tj} = K_{tj}$.

c.

Max Print

The maximum print and hunting procedure control quantities are specified by input T_{mj} and σ_{mj} ($j = 1, 2, \dots, 5$). The $|\sigma_{mj}|$ specifies the maximum or minimum achieved value of the parameter designated by the code input. Input $T_{mj} < 0$ specifies a minimum value; input $\sigma_{mj} = 0$ specifies ignore the max print logic for the j -th input; input $\sigma_{mj} > 0$ specifies a maximum value; and input $\sigma_{mj} < 0$ specifies the maximum absolute value regardless of the sign of T_{mj} .

The flag $|T_{mj}|$ directs the maximum control region. If $|T_{mj}| = 0$, the maximum print logic for the σ_{mj} parameter will be computed for each stage and the max print will appear after the termination of that stage. If $|T_{mj}| = k$ ($k = 1, 2, 3$, or 4), the max print logic for the σ_{mj} parameter will be computed for the k -th stage and the max print will appear after the termination of the k -th stage only. If $|T_{mj}| = 5$, the max print logic for the σ_{mj} parameter will be computed for the entire flight duration and the max print will appear after the termination of the last stage. When more than one parameter is designated, the prints occur in the order of the j -th index.

d.

Auxiliary Print

The auxiliary print consists of time and eleven parameters designated by the code input σ_{pj} ($j = 1, 2, \dots, 11$). The print will occur if the input, σ_{p1} is non-zero and when

Interval

$$t \leq t_{p1}$$

. . .

Print Time

$$t = n \Delta t_{p1}$$

.

Interval

$$t_{p1} < t \leq t_{p2}$$

$$t_{p7} < t \leq t_{p8}$$

Print Time

$$t = t_{p1} + n \Delta t_{p2}$$

$$t = t_{p7} + n \Delta t_{p8}$$

where t_{pj} and Δt_{pj} ($j = 1, 2, \dots, 8$) are input.

L. HUNTING PROCEDURE

Two methods of isolating variables and obtaining extremals are provided in the program. The first method incorporates an incremental hunting procedure (P1) which isolates and maximizes the dependent variable by varying the independent parameter. The second method incorporates a simultaneous hunting procedure (P2) which isolates and obtains extremals (maximum or minimum values) by varying up to seven parameters simultaneously. Either or both methods may be specified. If both methods are specified simultaneously, procedure 1 is used as a subroutine within procedure 2. (Experience has demonstrated that some problems will converge more rapidly if range is maximized by P1 while other parameters are simultaneously hunted using P2. Experience with the program will expose other areas where joint utilization of the hunting procedure is advantageous.)

The hunting procedures vary independent variables which are initially specified by input to obtain extremal and isolation solutions for dependent variables evaluated at cutoff.

Another option delineated in this section is one that allows the coefficients utilized in the steering equations to be automatically computed.

1. Incremental Hunting Procedure (P1)

The hunting procedure logic and equations for this option apply if the input P1 is non-zero.

The hunting procedure makes it possible to obtain a trajectory in which a specified quantity "a" (the dependent variable), can be found (isolated) or may be maximized with a single controller independent variable. The value of X (the independent variable) and the resulting value of "a" (the dependent variable) are designated by inputting the proper sigma code for σ_X and σ_a , respectively.

Isolation or maximization is an iterative process involving trajectory computations and hunting procedure logic. Dependent values for the first trajectory are computed with the input guess of the independent variable X_1 . Then the value of X is computed from their previous values and the input increment ΔX until the isolation or maximization region is bracketed. Thereafter, the independent variables are found by interpolation using quadratic equations.

If ΔX is input zero, the error message "DELTA X INPUT ZERO" is output and the run is terminated. If Δa is input zero, the error message "INTERNAL TOLERANCE INPUT ZERO" is output and the run is terminated. If the quadratic fit is singular, the error message "SINGULARITY IN QUADRIT FIT" is output and the run is terminated. If for the first two iterations, the dependent quantity does not vary, the error message "DEPENDENT PARAMETER NOT VARYING" is output and the run is terminated.

a. Isolation

The isolation procedure in this section will apply if $K_a \neq 0$.

Desired value of the dependent variable is the input a_f . The achieved dependent values resulting from trajectories computed with the dependent values \bar{X}_j ($j = 1, 2, 3$, or 4) are \bar{a}_j .

(1) Isolation Incrementing Routine

The dependent variable \bar{a}_j is computed using the input starting value X_1 then this point set (\bar{a}_1, \bar{X}_1) is transferred to the low point set (\bar{a}_3, \bar{X}_3) . The center point set (\bar{a}_2, \bar{X}_2) is computed using $\bar{X}_2 = \bar{X}_3 + \Delta X$.

If the desired dependent parameter is not bracketed but progressing in the correction direction, i.e., $\bar{a}_3 < \bar{a}_2 < a_f$ or $\bar{a}_3 > \bar{a}_2 > a_f$, then \bar{X}_2 is determined by incrementing, i.e., $X_1 = X_2 + \Delta X$ and the

\bar{a}_1 is evaluated by running a trajectory. The incremental process is continued until the desired dependent parameter is bracketed. Then the three data point sets are arranged such that the dependent variables are in descending order then sent to the quadratic interpolation routine. If after the incremental direction is established, the trend of the dependent variable reverse, i.e., diverges from the desired value a_f , then the error message "IMPOSSIBLE REGION EXISTS" is output and the run terminated.

If the desired dependent parameter is not bracketed but progressing in the wrong direction, i.e., $\bar{a}_2 < \bar{a}_3 < a_f$ or $\bar{a}_2 > \bar{a}_3 > a_f$, the second and third data sets are interchanged, the incremental direction changed, i.e., $\Delta X = -\Delta X$, and then the incremental process as described above is utilized.

(2) Isolation Linear Interpolation Routing

If the desired dependent parameter is bracketed then the two data sets are arranged in the first and third position such that $\bar{a}_1 > \bar{a}_3$, then \bar{X}_2 is determined by linear interpolation using a_f and then a_2 is evaluated by running a trajectory.

If the predicted dependent value is within the bracketed zone, then the three data points sets are such that the dependent variable are descending order and then sent to the quadratic interpolation routine. If not, the one point of the original point set and the newly predicted point which span the desired dependent variable are singled out and the process is repeated.

(3) Isolation Quadratic Interpolation Routine

When the dependent variable span the desired value, and are arranged in descending order, i.e., $\bar{a}_1 > a_f > \bar{a}_3$ and $\bar{a}_1 < \bar{a}_2 < \bar{a}_3$, then the predicted independent variable X_4 is determined by

quadratic interpolation using a_f and the predicted dependent variable \bar{a}_4 is evaluated by running a trajectory.

If the predicted dependent variable \bar{a}_4 is within the bracketed zone, then the bracket point sets and predicted point set are arranged such that the dependent variables are descending order, i.e., $\bar{a}_1 > \bar{a}_2 > \bar{a}_3$, and then transfer back to the quadratic interpolation routine.

If the predicted dependent variable \bar{a}_4 is outside the bracketed zone, then the predicted point set and the one point set of the two bracketed point set which span the desired dependent variable are singled out and transfer back to the linear interpolate routine.

(4) Isolation Convergence Criteria

If at any place in the logic the value of the dependent variable out of the trajectory routine is within the input Δ_a distance of the desired value a_f , then the hunting procedure 1 isolation has converged.

b. Maximization-Minimization

The maximization procedure in this section will apply if $K_a \neq 0$.

The achieved dependent values resulting from trajectories computed with the dependent values, \bar{X}_j ($j = 1, 2, 3, \text{ or } 4$) are a_j . If the input flag $P1$ is greater than zero, the function corresponding to σ_a is to be maximized. If the input flag $P1$ is less than zero, the function corresponding to σ_a is to be minimized.

(1) Maximization-Minimization Incrementing Routine

The dependent variable \bar{a}_1 is computed using the input starting value \bar{X}_1 , then this point set (\bar{a}_1, \bar{X}_1) is transferred to the low

point set (\bar{a}_3, \bar{X}_3) . The center point set (\bar{a}_2, \bar{X}_2) is computed using $\bar{X}_2 = \bar{X}_3 + \Delta X$, where ΔX is the input increment.

If the dependent variables are increasing for maximization or decreasing for minimization, i.e., $\bar{a}_2 > \bar{a}_3$ and $P_1 > 0$ or $a_2 < 0$, \bar{X}_1 is determined by incrementing, i.e., $\bar{X}_1 = \bar{X}_2 + \Delta X$, and \bar{a}_1 is evaluated by running a trajectory. This incremental process is continued in a hill climber fashion until the peak has been crossed; that is, the dependent variable has become less than for maximization or greater than for minimization, the previous value, i.e., $\bar{a}_1 < \bar{a}_2$ and $P_1 > 0$ or $\bar{a}_1 > \bar{a}_2$ and $P_1 < 0$.

These three point sets which form a peak or a valley are then sent to the quadratic routine. If the dependent parameter is progressing in the wrong direction; that is, decreasing for maximization or increasing for minimization, i.e., $\bar{a}_2 < \bar{a}_3$ and $P_1 > 0$ or $\bar{a}_2 > \bar{a}_3$ and $P_1 < 0$, the second and third data sets are interchanged, the incremental direction changed, i.e., $\Delta X = -\Delta X$, and then the incremental process as described above utilized.

2) Maximization-Minimization Quadratic Routine and Convergence Criteria

When the dependent variables describe a peak for maximization or a valley for minimization, i.e., $\bar{a}_1 < \bar{a}_2$ and $\bar{a}_3 > \bar{a}_2$ and $P_1 > 0$ or $\bar{a}_1 > \bar{a}_2$ and $a_3 > a_2$ and $P_1 < 0$, then the predicted independent variable X_4 is determined at the inflection point by a quadratic equation, the corresponding curve fit dependent variable set to a_f , and the predicted dependent variable a_4 evaluated by running a trajectory. If the predicted dependent value is within the input convergence tolerance, distance of the curve fit dependent variable a_f , then the maximization-minimization has converged.

If the predicted dependent variable \bar{a}_4 is progressing towards the optimum value; that is, the predicted dependent variable is greater than for maximization or less than for minimization, i.e.,

$\bar{a}_4 > \bar{a}_2$ and $P1 > 0$ or $\bar{a}_4 < \bar{a}_2$ and $P1 < 0$, then the points sets are arranged such that the predicted point set (\bar{a}_4, \bar{X}_4) are in the center data set (\bar{a}_2, \bar{X}_2) and the two independent variables; X , closest to but one greater than and one less than the predicted independent variable X are transfer to the high (\bar{a}_1, \bar{X}_1) and low (\bar{a}_3, \bar{X}_3) point sets where high and low correspond to the value of the independent variable X . These three point sets which form a peak or valley are then sent to the quadratic routine.

If the predicted variable \bar{a}_4 is not progressing towards the local optimum; that is, the predicted dependent variable is less than for maximization or greater than for minimization, the center set dependent variable, \bar{a}_2 , i.e., $\bar{a}_4 < \bar{a}_2$ and $P1 > 0$ or $\bar{a}_4 > \bar{a}_2$ and $P1 < 0$, then another point set in which the dependent variable is half way between the two independent variables, not spanning the predicted independent variable \bar{X}_a , is calculated by running another trajectory. Three point sets of the five inclusive of the center point set, (\bar{a}_2, \bar{X}_2) , in which the dependent variables form a peak for maximization or a valley for minimization with the independent values in numerical order are selected and then arranged such that the independent variable, X , are in descending order. These three data sets are then sent back to the quadratic routine.

2. Simultaneous Hunting Procedure (P2)

The hunting procedure logic and equations for this option apply if the input P2 is non-zero.

The logic for this section is contained in the OTTMZ subroutine writeup*, **which describes in detail a generalized hunting procedure. This hunting procedure uses one of three empirical models whose coefficients are estimated by least square fit

*Brinshall, R. K., "Design Optimization Using Model Estimation Programming", Thiokol Chemical Corporation No. 1166-13.63 dated 23 January 1967

**Olson, R. A., "Determining Extremals and/or Constraints Using the Method of Lagrange Multipliers", Thiokol Chemical Corporation Subroutine 9117 dated 4 November 1965.

The input code word P2 determines which model will be used.

| | | | |
|------|----|------------------------------------|----------------|
| P2 = | +1 | Linear Model | Isolation Only |
| | +2 | Complete Quadratic--Maximization | |
| | -2 | Complete Quadratic--Minimization | |
| | +3 | Incomplete Quadratic--Maximization | |
| | -3 | Incomplete Quadratic--Minimization | |

These three models will now be discussed to facilitate trajectory program input.

a) Linear Model

The logic in this section applies if P2 equals to one. The linear model is only used to isolate input dependent parameters. The linear empirical model consists of a system of polynomial equations equating the independent variables x_1, x_2, \dots, x_n to each of the dependent variables y_1, y_2, \dots, y_n .

$$\begin{aligned}
 y_1 &= a_{10} + a_{11}x_1 + a_{12}x_2 + a_{13}x_3 + \dots + a_{1n}x_n \\
 y_2 &= a_{20} + a_{21}x_1 + a_{22}x_2 + a_{23}x_3 + \dots + a_{2n}x_n \\
 y_3 &= a_{30} + a_{31}x_1 + a_{32}x_2 + a_{33}x_3 + \dots + a_{3n}x_n \\
 &\cdot \quad \cdot \quad \cdot \quad \cdot \quad \cdot \quad \dots \quad \cdot \\
 &\cdot \quad \cdot \quad \cdot \quad \cdot \quad \cdot \quad \dots \quad \cdot \\
 &\cdot \quad \cdot \quad \cdot \quad \cdot \quad \cdot \quad \dots \quad \cdot \\
 y_n &= a_{n0} + a_{n1}x_1 + a_{n2}x_2 + a_{n3}x_3 + \dots + a_{nn}x_n
 \end{aligned} \tag{1}$$

where n may vary from one to seven.

The generalized hunting procedure logic systematically varies the values of the independent variables (x's) from which the trajectory program evaluates the corresponding dependent variables (y's). The resulting dependent and independent variables are submitted to a multiple regression scheme to determine the coefficients (a's) of the above equation by at least square technique.

The desired value of the dependent variables (y_U 's) specified by input are equated to their polynomial equations and this system of linear equations is solved for the independent variables (x 's). These predicted independent variables (x 's) are input in the trajectory program to evaluate the dependent variables (y 's). Because the polynomial equations do not exactly match the true functions, the model determined dependent variables (y 's) will yield some error; this resulting error between the predicted and the achieved is further reduced to an acceptable increment specified by input by an incremented process involving the differential of the model system of equations.

The required input for this option is $\sigma_{x_1}, \sigma_{x_2}, \dots, \sigma_{x_n}$ to identify each independent variable; $x_{i1}, x_{i2}, \dots, x_{in}$ to specify the initial value for each of the corresponding independent variables (x 's); $\Delta x_{i1}, \Delta x_{i2}, \dots, \Delta x_{in}$ to establish the model array size and also to establish the largest allowable change in the independent variables (y 's) during an iteration; $\sigma_{y_1}, \sigma_{y_2}, \dots, \sigma_{y_n}$ to identify the dependent variable being isolated; $y_{U1}, y_{U2}, \dots, y_{Un}$ to specify the desired value of the dependent variables; $\epsilon_{c1}, \epsilon_{c2}, \dots, \epsilon_{cn}$ to stipulate a tolerance of convergence upon the dependent variables (y 's); $x_{L1}, x_{L2}, \dots, x_{Ln}$ to establish a lower restraint limit on the independent variables (x 's); and $x_{U1}, x_{U2}, \dots, x_{Un}$ to establish an upper restraint limit on the independent variables (x 's).

An example of utilizing the linear model isolation / simultaneous hunting procedure is as follows:

Problem -- 100 nm circular orbital injection

Model P2 = 1

Independent variables

$x_1 = Q_2$ (Pitch rate at kickover)

$x_2 = Q_4$ (Terminal pitch rate)

$x_3 = W_{PL}$ (Payload weight)

Set

$$\begin{array}{lllll}
 \sigma_{x1} = 320 & x_{i1} = 10 & \Delta x_{i1} = 1 & x_{L1} = -15 & x_{U1} = -5 \\
 \sigma_{x2} = 333 & x_{i2} = -0.05 & \Delta x_{i2} = 0.01 & x_{L2} = -0.15 & x_{U2} = 0.05 \\
 \sigma_{x3} = 20 & x_{i3} = 40,000 & \Delta x_{i3} = 5,000 & x_{L3} = 20,000 & x_{U3} = 60,000
 \end{array}$$

Dependent variables

$y_1 = V_I$ (circular orbital injection inertial velocity)

$y_2 = \gamma_{1I}$ (circular orbital injection inertial flight path angle)

$y_3 = h$ (circular orbital altitude)

$$\begin{array}{lll}
 \sigma_{y1} = 5029 & y_{U1} = 25,570 & \epsilon_{c1} = 5 \\
 \sigma_{x2} = 5255 & y_{U2} = 0 & \epsilon_{c2} = 0.01 \\
 \sigma_{y3} = 5501 & y_{U3} = 607,610 & \epsilon_{c3} = 100
 \end{array}$$

The generalized hunting routine uses the technique of Lagrange to maximize or minimize the function f subject to the constraint functions g_1, g_2, \dots, g_m . Thus

$$G = f(x_1, x_2, \dots, x_n) + \sum_{i=1}^{i=m} \lambda_i [g_i(x_1, x_2, \dots, x_n) - L_i]$$

where L_i is the value of the constraint, λ_i is the Lagrangian multiplier and G is the Lagrangian function. The Lagrangian function G is differentiated with respect to each x and each λ , then the partial derivatives of G are each equated to zero, and the system of $n + m$ equations are solved for the $n + m$ unknowns; thus yielding the required values of x_1, x_2, \dots, x_n which maximizes or minimizes the Lagrangian function G .

The generalized hunting routine is designed so that only maximums, as specified by $P2 = +2$, or minimums, as specified by $P2 = -2$, will be obtained. There is no guarantee that the solution obtained will not be a local maxima or minima. Saddle point solutions will not be obtained.

The functions f and g are represented by a quadratic response surface of the form:

function f

$$\begin{aligned} z = & a_{00} \\ & + a_{10}x_1 + a_{20}x_1^2 \\ & + a_{30}x_2 + a_{40}x_1x_2 + a_{50}x_2^2 \\ & + a_{60}x_3 + a_{70}x_1x_3 + a_{80}x_2x_3 + a_{90}x_3^2 \end{aligned}$$

function g

$$\begin{aligned} y_i = & a_{0i} \\ & + a_{1i}x_1 + a_{2i}x_1^2 \\ & + a_{3i}x_2 + a_{4i}x_1x_2 + a_{5i}x_2^2 \\ & + a_{6i}x_3 + a_{7i}x_1x_3 + a_{8i}x_2x_3 + a_{9i}x_3^2 \\ & + \quad . \quad . \quad . \quad . \quad . \quad . \quad . \end{aligned}$$

where $i = 1, 2, \dots, m$

The generalized hunt procedure will determine the coefficients (a 's) in the same manner as outlined for the linear model.

b. Complete Quadratic Response Surface

The logic in this section applies if $P2$ equals positive or negative two. The complete quadratic response surface model is used (1) to maximize or minimize a function subject to constraint or (2) to isolate a particular solution from a family of maximized or minimized functions subject to constraints.

If the input f_D equals zero, the generalized hunting procedure will maximize or minimize the primary dependent variables called z where $z = \hat{f}(x_1, x_2, \dots, x_n)$, subject to constraints in m^* secondary dependent variables called y_1, y_2, \dots, y_m where $y_i = g_i(x_1, x_2, \dots, x_n)$. The number of constraint functions may vary from zero to n where n is the number of independent variables (x 's) and n cannot exceed seven.

If the input f_D equals non-zero, the generalized hunting procedure will isolate a particular solution from a family of maximized or minimized functions subject to constraints. This family relates the independent variable x_1 as function of the maximized or minimized dependent variable z with respect to the independent variables x_2, x_3, \dots, x_n subject to constraints in m dependent variables y_1, y_2, \dots, y_m and m cannot exceed $n-1$. Isolation involves selecting the independent variables x_i which yields the maximized or minimized dependent variable z specified by the input value f_D .

The required input for this solution is σ_2 , identify the dependent variable for which the extremal solution is desired; $\sigma_{x1}, \sigma_{x2}, \dots, \sigma_{xn}$, to identify the independent variables; $x_{i1}, x_{i2}, \dots, x_{in}$, to specify the initial values of the independent variables; $\Delta x_{i1}, \Delta x_{i2}, \dots, \Delta x_{in}$, to specify the model array size and to specify the maximum change of an independent variable during a given iteration; $\sigma_{y1}, \sigma_{y2}, \dots, \sigma_{ym}$, to identify the dependent variables being constrained; $y_{L1}, y_{L2}, \dots, y_{Lm}$, to establish the lower constraint boundary; $y_{U1}, y_{U2}, \dots, y_{Um}$, to establish the upper constraint boundary; $\epsilon_{c1}, \epsilon_{c2}, \dots, \epsilon_{cm}$,

to establish tolerances or the constraint solution; x_{L1} , x_{L2} , ..., x_{Ln} , to establish a lower restraining limit on the independent variables; and x_{U1} , x_{U2} , ..., x_{Un} , to establish an upper restraining limit on the independent variable.

An example of utilizing the complete quadratic response surface model to maximize a function subject to constraints is as follows:

Problem -- maximize range with fixed payload subject to the constraint that the maximum dynamic pressure be less than 1000 psf

Model $P2 = +2$

Dependent Variables

$x_1 = Q_2$ (Pitch rate at kickover)

$x_2 = Q_4$ (Terminal pitch rate)

Set

$$\begin{array}{llllll} \sigma_{x1} = 319 & x_{L1} = -12 & \Delta x_{i1} = 2 & x_{L2} = -20 & x_{U1} = -4 \\ \sigma_{x2} = 331 & x_{L2} = -1 & \Delta x_{i2} = 0.1 & x_{L2} = -10 & x_{U2} = 2 \end{array}$$

Independent variables

$\sigma_z = S_f$ (range)

$\sigma_{y1} = q_{max}$ (maximum dynamic pressure)

Set

$$\begin{array}{llll} \sigma_z = 5013 & y_{L1} = 0 & y_{U1} = 1000 & \epsilon_z = 0.5 \\ \sigma_{y1} = 271 & & & \epsilon_{c1} = 1 \\ \sigma_{m1} = 5037 & T_m = 5 & & \end{array}$$

c. Incomplete Quadratic Response Surface

This model is used if $P2 = +3$ to specify maximization, or $P2 = -3$ to specify a minimization.

This model is used in identically the same manner as the complete quadratic response surface discussed in Section L.2.b. The relative merits between the two models are discussed in section L.2.c. The model used to estimate the dependent variables z and y_i is of the form:

function f

$$z = a_{00} + a_{10}x_1 + a_{20}x_1^2 + a_{30}x_2 + a_{40}x_2^2 + \dots + a_{(2n-1)0}x_n + a_{(2n)0}x_n^2$$

function g

$$y_i = a_{0i} + a_{1i}x_1 + a_{2i}x_1^2 + a_{3i}x_2 + a_{4i}x_2^2 + \dots + a_{(2n-1)i}x_n + a_{(2n)i}x_n^2$$

where $i = 1, 2, \dots, m^*$.

The required input is the same as that described in Section L.2.b.

An example of utilizing the incomplete quadratic response surface model to isolate a particular solution from a family of maximized functions subject to constraint is as follows:

Problem -- determine the payload consistent with a maximum range trajectory for a range of 5500 nm subject to the constraint that the maximum dynamic pressure be less than 1000 psf.

Model P2 = +3

Independent variables

$x_1 = W_{PL}$ (payload weight)

$x_2 = Q_2$ (pitch rate at kickover)

$x_3 = Q_4$ (terminal pitch rate)

Set

$$\sigma_{x_1} = 20 \quad x_{i1} = 10,000 \quad \Delta x_{i1} = 1,000 \quad x_{L1} = 0 \quad x_{U1} = 20,000$$

$$\sigma_{x_2} = 320 \quad x_{i2} = -8 \quad \Delta x_{i2} = 1 \quad x_{L2} = -12 \quad x_{U2} = 3$$

$$\sigma_{x_3} = 335 \quad x_{i3} = -0.5 \quad \Delta x_{i3} = 0.05 \quad x_{L3} = -5 \quad x_{U3} = 1$$

Dependent variables

$z = S_f$ (range)

$y_1 = q_{max}$ (maximum dynamic pressure)

Set

$$\sigma_z = 5024 \quad y_{L1} = 0 \quad y_{U1} = 1000 \quad \epsilon_z = 0.5$$

$$\sigma_{y_1} = 261 \quad \epsilon_{c1} = 1$$

$$\sigma_{m_1} = 5070 \quad T_m = 5 \quad f_D = 5500$$

d. Generalized Hunt Characteristics

The data described in this section is applicable to that described for each model.

In the extremal problem the variance of the model is evaluated at the apparent solution point. If the input parameter ϵ_m is

nonzero and if the probability is greater than 0.05 that the model error is greater than ϵ_m , the entire maximization (or minimization) will be repeated.

The independent variables may be transformed to aid the convergence of the model. A transform code input is available for each independent variable and is input $T_{T1}, T_{T2}, \dots, T_{Tn}$. A constant of transformation $a_{T1}, a_{T2}, \dots, a_{Tn}$ is input for each transformation. The available transformations are:

| | |
|-----------|----------------------------|
| $T_T = 0$ | $\eta = x + a_T$ |
| $T_T = 1$ | $\eta = x ^{a_T} (x)/ x $ |
| $T_T = 2$ | $\eta = \ln a_T x$ |
| $T_T = 3$ | $\eta = a_T/x$ |
| $T_T = 4$ | $\eta = e^{a_T x}$ |

where η is the transformed independent variable.

The relative merits of using the complete quadratic response surface as opposed to the incomplete quadratic response surface is in running time. If ϵ_m is non-zero and if it is the same value for either method, the same answer should be eventually obtained. Advantage to using the incomplete quadratic response surface model will probably not materialize until $n = 6$ or 7 . As a guide to choice and an aid to estimation of running time, the following table describes the number of trajectories necessary to estimate the coefficients required to make the first optimal prediction.

| <u>n</u> | <u>Complete Quadratic</u> | | <u>Incomplete Quadratic</u> | |
|----------|-----------------------------------|-----------------------------------|-----------------------------------|-----------------------------------|
| | <u>Trajectories Simulated</u> | <u>Coefficients Estimated</u> | <u>Trajectories Simulated</u> | <u>Coefficients Estimated</u> |
| 1 | 3 | 3 | 5 | 3 |
| 2 | 6 | 6 | 9 | 5 |
| 3 | 15 | 10 | 13 | 7 |
| 4 | 25 | 15 | 17 | 9 |
| 5 | 27 | 21 | 21 | 11 |
| 6 | 45 | 28 | 25 | 13 |
| 7 | 79 | 36 | 29 | 15 |

The complete quadratic response surface model will always make better predictions for any given iteration; therefore, the incomplete quadratic response surface model should require more iterations. Experience will dictate the most efficient method for solving the hunting procedure problem.

The maximum number of hunt predictions beyond the initial array must be specified in n_{t2} . If n_{t2} is input, a negative number, the hunt will restart after n_{t2} -th iterations.

3. Special Routines

a. Acquisition of Coefficients for Steering Equations

The coefficients for the pitch steering equations are obtained by a least square curve fit of flight path parameters. This option automates the acquisition of these coefficients. The portion of the trajectory to be fit will be specified by sigma codes contained in the switching table.

If σ_{g1k} is zero, this option is by passed for the k-th stage. If $\sigma_{g1k} > 0$, the data locations containing the summation matrix and the observation counter n_g will be initially set to zero at the beginning of each stage. Over the portion of the trajectory which is to be fit, a summation of data will be generated in the following form for each integration step. Data will be processed over the open interval $K_{g1k} \leq \sigma_{g1k}$ to $\sigma_{g2k} \leq K_{g2k}$.

$$n_g = \Sigma 1.0$$

let

$$\begin{aligned} u_1 &= \dot{z}_{gg} \\ u_2 &= \dot{x}_{gg} \\ u_3 &= \dot{x}_{gg}^2 \\ u_4 &= \dot{x}_{gg}^3 \\ u_5 &= \theta_m \text{ (radians)} \end{aligned}$$

Then the summation matrix appears as follows:

| | | | | |
|------------------|------------------|------------------|------------------|------------------|
| Σu_1 | Σu_2 | Σu_3 | Σu_4 | Σu_5 |
| $\Sigma (u_1)^2$ | $\Sigma u_1 u_2$ | $\Sigma u_1 u_3$ | $\Sigma u_1 u_4$ | $\Sigma u_1 u_5$ |
| $\Sigma u_2 u_1$ | $\Sigma (u_2)^2$ | $\Sigma u_2 u_3$ | $\Sigma u_2 u_4$ | $\Sigma u_2 u_5$ |
| $\Sigma u_3 u_1$ | $\Sigma u_3 u_2$ | $\Sigma (u_3)^2$ | $\Sigma u_3 u_4$ | $\Sigma u_3 u_5$ |
| $\Sigma u_4 u_1$ | $\Sigma u_4 u_2$ | $\Sigma u_4 u_3$ | $\Sigma (u_4)^2$ | $\Sigma u_4 u_5$ |

3. Special Routines

a. Acquisition of Coefficients for Steering Equations

The coefficients for the pitch steering equations are obtained by a least square curve fit of flight path parameters. This option automates the acquisition of these coefficients. The portion of the trajectory to be fit will be specified by sigma codes contained in the switching table.

If σ_{gk} is zero, this option is bypassed for the k-th stage. If $\sigma_{gk} > 0$, the data locations containing the summation matrix and the observation counter n_g will be initially set to zero at the beginning of each stage. Over the portion of the trajectory which is to be fit, a summation of data will be generated in the following form for each integration step. Data will be processed over the open interval $K_{g1k} \leq \sigma_{g1k}$ to $\sigma_{g2k} \leq K_{g2k}$.

$$n_g = \Sigma 1.0$$

let

$$u_1 = \dot{z}_{gg}$$

$$u_2 = \dot{x}_{gg}$$

$$u_3 = \dot{x}_{gg}^2$$

$$u_4 = \dot{x}_{gg}^3$$

$$u_5 = \theta_m \text{ (radians)}$$

Then the summation matrix appears as follows:

| | | | | |
|------------------|------------------|------------------|------------------|------------------|
| Σu_1 | Σu_2 | Σu_3 | Σu_4 | Σu_5 |
| $\Sigma (u_1)^2$ | $\Sigma u_1 u_2$ | $\Sigma u_1 u_3$ | $\Sigma u_1 u_4$ | $\Sigma u_1 u_5$ |
| $\Sigma u_2 u_1$ | $\Sigma (u_2)^2$ | $\Sigma u_2 u_3$ | $\Sigma u_2 u_4$ | $\Sigma u_2 u_5$ |
| $\Sigma u_3 u_1$ | $\Sigma u_3 u_2$ | $\Sigma (u_3)^2$ | $\Sigma u_3 u_4$ | $\Sigma u_3 u_5$ |
| $\Sigma u_4 u_1$ | $\Sigma u_4 u_2$ | $\Sigma u_4 u_3$ | $\Sigma (u_4)^2$ | $\Sigma u_4 u_5$ |

At the end of staging, after the printing of "TERMINATION OF STAGE K" before the printing of the note "MAXIMUM VALUES" the data generated should be processed.

If $\sigma_{gk} > 0$ and $n_g < 5$, a note should be printed as follows, "STEERING COEFFICIENTS NOT CALCULATED." The trajectory should continue as though this option were not called for.

If σ_{gk} is non-zero and $n_g \geq 5$, then data has been generated and should be processed as follows:

The summation of the product terms, $\sum_i u_i u_j$, is scaled by and corrected for the mean by multiplying by n_g^2 , dividing by $\sum_i \sum_j$ and subtracting n_g . The corrected terms will then be of the form

$$\frac{n_g^2 \sum_i u_i u_j}{\sum_i \sum_j} - n_g$$

The corrected matrix then is the following 4 X 5 matrix:

$$\begin{array}{ccccc} \frac{n_g^2 \sum_i (u_1)^2}{(\sum_i u_1)^2} - n_g & \frac{n_g^2 \sum_i u_1 u_2}{\sum_i \sum_j} - n_g & \frac{n_g^2 \sum_i u_1 u_3}{\sum_i \sum_j} - n_g & \frac{n_g^2 \sum_i u_1 u_4}{\sum_i \sum_j} - n_g & \frac{n_g^2 \sum_i u_1 u_5}{\sum_i \sum_j} - n_g \\ \frac{n_g^2 \sum_i u_2 u_1}{\sum_i \sum_j} - n_g & \frac{n_g^2 \sum_i (u_2)^2}{(\sum_i u_2)^2} - n_g & \frac{n_g^2 \sum_i u_2 u_3}{\sum_i \sum_j} - n_g & \frac{n_g^2 \sum_i u_2 u_4}{\sum_i \sum_j} - n_g & \frac{n_g^2 \sum_i u_2 u_5}{\sum_i \sum_j} - n_g \\ \frac{n_g^2 \sum_i u_3 u_1}{\sum_i \sum_j} - n_g & \frac{n_g^2 \sum_i u_3 u_2}{\sum_i \sum_j} - n_g & \frac{n_g^2 \sum_i (u_3)^2}{(\sum_i u_3)^2} - n_g & \frac{n_g^2 \sum_i u_3 u_4}{\sum_i \sum_j} - n_g & \frac{n_g^2 \sum_i u_3 u_5}{\sum_i \sum_j} - n_g \\ \frac{n_g^2 \sum_i u_4 u_1}{\sum_i \sum_j} - n_g & \frac{n_g^2 \sum_i u_4 u_2}{\sum_i \sum_j} - n_g & \frac{n_g^2 \sum_i u_4 u_3}{\sum_i \sum_j} - n_g & \frac{n_g^2 \sum_i (u_4)^2}{(\sum_i u_4)^2} - n_g & \frac{n_g^2 \sum_i u_4 u_5}{\sum_i \sum_j} - n_g \end{array}$$

where the first four columns are the matrix U_1 and the last column is the vector U_2 .

Then the coefficient vector U_g is determined by

$$\{U_g\} = [U_1]^{-1} \{U_2\}$$

with the constant term defined as

$$U_{g0} = (1 - U_{g1} - U_{g2} - U_{g3} - U_{g4}) (\Sigma u_5) / n_g$$

The steering coefficients for the k-th stage will then be as follows:

$$a_{0k} = U_{g0}$$

$$a_{1k} = U_{g1} (\Sigma u_5) / (\Sigma u_1)$$

$$b_{1k} = U_{g2} (\Sigma u_5) / (\Sigma u_2)$$

$$b_{2k} = U_{g3} (\Sigma u_5) / (\Sigma u_3)$$

$$b_{3k} = U_{g4} (\Sigma u_5) / (\Sigma u_4)$$

The steering equation coefficients are saved to be available on the next run.

b. Shaper Subroutine

(1). Introduction

This routine utilizes a generalized attitude control table and sets up the hunting procedure to (1) maximize range for a given payload, (2) maximize payload to a given range or (3) isolate the payload weight for a given circular orbit. The generalized attitude control table specifies the following flight path.

1. The vehicle will fly vertically off the pad until a velocity of 170.0 feet per second has been obtained before initiating pitchover. This ascent will assure that the vehicle has cleared the ground handling equipment and launching facilities.
2. The vehicle will pitch down at a rate consistent with available TVC angle and reasonable stress levels in the interstage. This rate is established empirically as a function of the vehicle liftoff weight. The pitchover is terminated when a specific pitch attitude, θ_{m2} , has been obtained.
3. The vehicle is maintained at this specific attitude until the velocity vector angle coincides with the vehicle centerline, i.e., at zero degrees angle of attack.
4. The final and major portion of flight is programmed as a gravity turn path such that the vehicle is thrusting along the velocity vector, i.e., at zero degrees angle of attack. This flight profile will be utilized for both the ballistic range trajectory and the orbital trajectory.

The prime inputs to the routine are the input control flag which specifies the mission, the input target range or orbital attitude, the stage rocket motor ballistic characteristics, as specified by the thrust-weight input and the input trajectory

initial conditions such as the launch azimuth, initial altitude, velocity, etc. Inherent in the hunting procedure are a starting point and a maximum walking distance. The hunting procedure in the trajectory program requires that the initial and incremental values of the independent parameters be specified. These initial values of the independent variables are determined as continuous functions of the vehicle ideal velocity, stage burn times, and initial conditions.

This program will simplify the input to the trajectory program when doing performance trajectory work.

(2) Shaper Equations and Logic

Input Control Flags

$$K_{sh} = \begin{cases} 0 & \text{ignore routine} \\ 1 & \text{maximize range} \\ 2 & \text{maximize payload to a given range} \\ 3 & \text{determine payload to a circular orbit} \end{cases}$$

S_{sh} = target range or orbital altitude (nmi)

Terminal Stage Number

n_k = largest stage number containing a non-zero input, σ_s

Calculate impulses and thrust multipliers

K_{FM} , K_{FC} , K_{EM} , K_{EC} , K_{WM} , K_{WC} , I_{VM} , I_{VC} , and I_{VT}

The input main weight flow integral:

$$\Delta W_{Mi} = K_{WM} K_{EM} \sum_{j=1}^{J_M-1} (\dot{W}_{M(j+1)} + \dot{W}_{M(j)}) (t_{M(j+1)} - t_{M(j)})/2.$$

The expended main propellant weight:

$$\Delta W_{Mf} = \begin{cases} 0 & \text{if } I_{spM} = 0.0 \\ K_{FM} K_{tM} I_{vM} / I_{spM} & \text{Otherwise} \end{cases}$$

The complementary weight flow integral:

$$\Delta W_{Ci} = K_{WC} K_{tC} \sum_{j=1}^{J_C-1} (\dot{W}_{C(j+1)} + \dot{W}_{C(j)}) (t_{C(j+1)} - t_{C(.)})/2$$

The expended complementary propellant weight

$$\Delta W_{Cf} = \begin{cases} 0 & \text{if } I_{spC} = 0.0 \\ K_{FC} K_{tC} I_{vC} / I_{spC}, & \text{otherwise} \end{cases}$$

Total expended weight:

$$\Delta W = \Delta W_{Mi} + \Delta W_{Mf} + \Delta W_{Ci} + \Delta W_{Cf}$$

Stage effective specific impulse

$$I_{speff} = I_{vT} / \Delta W$$

Carryover weight:

$$W_{OV} = \begin{cases} 0 & \text{If } k - 1 \text{ or } K_0(k-1) = K_{NO}(k-1) = 0.0 \\ W_{B(k-1)} - \Delta W_{(k-1)} & \text{If } K_0(k-1) \neq 0.0 \\ W_{CO(k-1)} - \Delta W_{Ci(k-1)} - \Delta W_{Cf(k-1)} & \text{If } K_{NO}(k-1) \neq 0.0 \\ & \text{and } K_0(k-1) \neq 0.0 \end{cases}$$

Stage Weight:

Stage Weight Ratio:

$$W_B = W_{MO} + W_{CO} + W_{OV}$$

$$v = W_B / W_{B1}$$

Stage duration:

$$t_B = t_{B(J_M)} K_{tM}$$

Earth rotation factor:

$$\bar{\omega}/\omega = \cos \rho_L \sin \psi_i$$

Propulsion system liftoff weight

$$W_{PLO_k} = W_{B_k} + \sum_{j=k+1}^{n_k} (W_{MO(j)} + W_{CO(j)})$$

Maximum Range:

If $K_{sh} = 1$, apply the following logic and equations

Ideal Velocity Equation:

$$\Delta V = \bar{g}_e \sum_{k=k_k}^{n_k} I_{speff_k} \ln \left[\frac{W_{FL} + W_{PLO_k}}{W_{FL} + W_{PLO_k} - \Delta W_k} \right]$$

Vehicle Liftoff Weight:

$$W_T = W_{PL} + \sum_{k=1}^{n_k} W_{M_k} + W_{CO_k}$$

Velocity at Pitch Over:

$$V_{PO} = \begin{cases} 170.0 & \text{If } V_{eo} \leq 160 \\ V_{eo} + 10 & \text{Otherwise} \end{cases}$$

Pitch Over Pitch Rate:

$$Q_{m2} = \{2,186.428 + \ln(W_T) [-218.16888 + 5,451,1537 \ln(W_T)] W_T^{1/3}$$

Pitch Over Angle:

| | | | |
|---------------------------|--------------------|-----------------------|-----------|
| $\theta_{n2} = -19.33383$ | $+ .0031310$ | ΔV | (ft/sec) |
| | $- .00000012854$ | ΔV^2 | |
| | $+ .81426$ | t_{B1} | (sec) |
| | $+ .00082444$ | t_{B1}^2 | |
| | $+ .13693$ | t_{B2} | (sec) |
| | $+ .036519$ | t_{B3} | (sec) |
| | $+ .043040$ | V_0 | (ft/sec) |
| | $- .00022205$ | h_0 | (ft) |
| | $- .0000000085475$ | h_0^2 | |
| | $- 5.13440$ | $\bar{\omega}/\omega$ | (dim) |
| | $+ 23.95712$ | v_2 | (dim) |
| | $+ 47.53343$ | v_3 | (dim) |
| | $- 1.45158$ | Q_{m2} | (deg/sec) |
| | $- .013984$ | $(Q_{mq})^2$ | |

Initial Conditions

| | | |
|-----|------|-------|
| L11 | 90.0 | (deg) |
| L28 | 90.0 | (deg) |

Initial flight path angle

Initial command pitch attitude

Hunting Procedure P1

| | | |
|-----|--------|-------|
| L73 | 1.0 | (dim) |
| L74 | 0.0 | (dim) |
| L75 | 20.0 | (dim) |
| L76 | 1.0 | (dim) |
| L77 | 319.0 | (dim) |
| L78 | 5024.0 | (dim) |
| L80 | 6m2 | (deg) |
| L81 | 2.0 | (deg) |
| L83 | 1.0 | (nmi) |

Hunting procedure P1 flag

Stage print flag

Trajectory limit number

Isolation-maximization flag

Independent variable code $[K_{f2}]$

Dependent variable code $[S_f]$

Initial value of independent variable

Incremental value of independent variable

Convergence accuracy of dependent variable

Huntir Procedure P2

| | | |
|-----|-----|-------|
| L84 | 0.0 | (dim) |
|-----|-----|-------|

Hunting procedure P2 flag

Main Print

| | | |
|------|--------|-------|
| L184 | 10.0 | (sec) |
| L183 | 2000.0 | (sec) |

Main print time interval

Main print time limit

Discontinuity Print

| | | | |
|------|-------|---|-------|
| L252 | 310.0 | Code for discontinuity print at end of vertical rise | (dim) |
| L253 | 317.0 | Code for discontinuity print at end of pitch error | (dim) |
| L254 | 324.0 | Code for discontinuity print at start of gravity turn | (dim) |

Attitude Control

| | | | |
|------|------------|---|-----------|
| L310 | 1.0 | Type of flight region 1 [command rate] | (dim) |
| L311 | 5046.0 | Parameter code for termination of region 1 [V_e] | (dim) |
| L312 | V_{PO} | Velocity to terminate region 1 | (ft/sec) |
| L313 | 0.0 | Pitch rate for region 1 | (deg/sec) |
| L316 | 1.0 | Type of flight region 2 [command rate] | (dim) |
| L317 | 5722.0 | Parameter code for termination of region 2 [θ_m] | (dim) |
| L318 | θ_m | Command attitude to terminate region 2 | (deg) |
| L319 | Q_m | Pitch rate for region 2 | (deg/sec) |
| L322 | 1.0 | Type of flight region 3 [command rate] | (dim) |
| L323 | 5310.0 | Parameter code for termination of region 3 [α] | (dim) |
| L324 | 0.0 | Angle of attack to terminate region 3 | (deg) |
| L325 | 0.0 | Pitch rate for region 3 | (deg/sec) |
| L328 | 2.0 | Type of flight region 4 [gravity turn] | (dim) |
| L329 | 5006.0 | Parameter code for termination of region 4 [t] | (dim) |
| L330 | 2000.0 | Time to terminate region 4 | (sec) |
| L331 | 0.0 | Angle of attack for region 4 | (deg) |

(3) Maximum Payload to a Given Range

If $K_{sh} = 2$, apply the following logic and equations:

Estimated required Ideal Velocity for Range ≤ 8000 Nautical Miles:

| | | | |
|-------|------------------|-----------------------|----------|
| $V =$ | $- .0041972$ | | |
| | $- 1.46207$ | V_0 | (ft/sec) |
| | $- 25,15275$ | t_{B1} | (sec) |
| | $+ .33069$ | t_{B1}^2 | |
| | $+ 10.9655$ | t_{B2} | (sec) |
| | $+ 4.7776$ | t_{B3} | (sec) |
| | $- 1152.8991$ | $\bar{\omega}/\omega$ | (dim) |
| | $- .04378$ | h_0 | (ft) |
| | $+ .00000074999$ | H_0^2 | |
| | $+ 33642.902$ | $(S_F/1000)$ | (nmi) |
| | $- 25126.67$ | $(S_F/1000)^2$ | |
| | $+ 10625.982$ | $(S_F/1000)^3$ | |
| | $- 2570.1949$ | $(S_F/1000)^4$ | |
| | $+ 355.47505$ | $(S_F/1000)^5$ | |
| | $- 26.22204$ | $(S_F/1000)^6$ | |
| | $+ .80102$ | $(S_F/1000)^7$ | |

For Range > 8000 Nautical Miles.

$$V = 29000$$

Payload Iteration Procedure

Ideal Velocity Equation

$$\Delta V^L = \bar{g}_e \sum_{k=k_k}^{n_k} I_{speff} \ln \left[\frac{W_{PL}^L + W_{PLO_k}}{W_{PL}^L + W_{PLO_k} - \Delta W_k} \right]$$

where ℓ is the iteration counter.

Initial guess for W_{PL}

$$\text{For } \ell = 1 \quad W_{PL}^{\ell=1} = W_{PLO_{k-k_k}} / 30.0$$

$$\text{For } \ell = 2 \quad W_{PL}^{\ell=2} = 1.01 W_{PL}^{\ell=1}$$

$$\text{For } \ell \geq 3 \quad W_{PL}^{\ell \geq 3} = W_{PL}^{\ell-1} - \frac{(\hat{\Delta V} - \Delta V^{\ell-1})(W_{PL}^{\ell-1} - W_{PL}^{\ell-2})}{(\Delta V^{\ell-2} - \Delta V^{\ell-1})}$$

If $W_{PL}^{\ell} < 0$, then set $W_{PL}^{\ell} = W_{PL}^{\ell-1} / 2.0$

If $\frac{\hat{\Delta V} - \Delta V^{\ell}}{\Delta V} < 0.00004$, terminate iteration

If $\ell = 100$, terminate run and print

"PAYLOAD WEIGHT ITERATION DID NOT CONVERGE"

At the termination of the payload weight iteration,

$$\text{set } W_{PL} = W_{PL}^{\ell}$$

Vehicle Liftoff Weight

$$W_T = W_{PL} + \sum_{k=k_k}^{n_k} W_{M)k} + W_{CCK}$$

Velocity at Pitch Over

$$V_{PO} = \begin{cases} 170.0 & \text{If } V_{\infty} \leq 160.0 \\ V_{\infty} + 10.0 & \text{Otherwise} \end{cases}$$

(4) Pitch Over Pitch Rate

$$Q_{m2} = - \{ 2,186.428 + \ln (W_T) [-218.16888 + 6.4511537 \ln (W_T)] \} / W_T^{1/3}$$

Pitch Over Angle

| | | | | |
|---------------------------------|---|----------------|---------------------------|-----------|
| $\hat{\theta}_{m2} = -23,42023$ | + | .86 | t_{B1} | (sec) |
| | + | .094735 | t_{B2} | |
| | + | .022857 | t_{B3} | |
| | - | .040341 | v_0 | (ft/sec) |
| | - | .00033343 | h_0 | (ft) |
| | - | .0000000070714 | h_0^2 | |
| | - | .88686 | $\bar{\omega}/\omega$ | (dim) |
| | - | 1.2008 | $(\bar{\omega}/\omega)^2$ | |
| | + | 33.3329 | v_2 | (dim) |
| | + | 50.30273 | v_3 | (dim) |
| | - | 3.91364 | Q_{m2} | (deg/sec) |
| | - | .14096 | $(Q_{m2})^2$ | |
| | - | .0027139 | s_F | mm |

Initial Conditions

L11 90.0 (deg)
Initial flight path angle
L28 90.0 (deg)
Initial command pitch attitude

Hunting Procedure P1

L73 0.0 (dim)
Hunting procedure P1 flag

Hunting Procedure P2

L84 3.0 (dim)
Hunting procedure P2 flag [incomplete quadratic]
L85 5024.0 (dim)
Maximized dependent variable code [S_F]
L86 1.0 (nm)
Tolerance of maximization parameter
L87 0.0 (dim)
Model accuracy
L88 0.0 (min)
Run Time
L89 S_{ah} (nm)
Isolated-maximized parameter [S_F]
L90 20.0 (dim)
Trajectory limit number beyond base array
L91 20.0 (dim)
Isolation independent variable code [W_{PL}]
L92 W_{FL} (lb)
Initial value of isolation independent variable
L93 0.1 x W_{PL} (lb)
Incremental value of isolation independent variable
L98 0.0 (dim)
Transformation flag, first independent variable
L99 0.0 (lb)
Transformation constant, first independent variable
L100 319.0 (dim)
Second independent variable code [K_{F2}]
L101 $\hat{\theta}_{m2}$ (deg)
Initial value of independent variable
L102 2.0 (deg)
Incremental value of independent variable
L107 0.0 (dim)
Transformation flag, second independent variable
L108 0.0 (deg)
Transformation constant, second independent variable
L154 0.5 W_T (lb)
Upper limit first independent variable

| | | | |
|---------------------|---------------------|---|-----------|
| L155 | 90.0 | Upper limit second independent variable | (deg) |
| L161 | 0.0 | Lower limit first independent variable | (lb) |
| L162 | 20.0 | Lower limit second independent variable | (deg) |
| Main Print | | | |
| L184 | 10.0 | Main print time interval | (sec) |
| L185 | 2000.0 | Main print time limit | (sec) |
| Discontinuity Print | | | |
| L252 | 310.0 | Code for discontinuity print at end of vertical rise | (dim) |
| L253 | 317.0 | Code for discontinuity print at end of pitch over | (dim) |
| L254 | 324.0 | Code for discontinuity print at start of gravity turn | (dim) |
| Attitude Control | | | |
| L310 | 1.0 | Type of flight region 1 [command rate] | (dim) |
| L311 | 5046.0 | Parameter code for termination of region 1 [V_e] | (dim) |
| L312 | V_{PO} | Velocity to terminate region 1 | (ft/sec) |
| L313 | 0.0 | Pitch rate for region 1 | (deg/sec) |
| L316 | 1.0 | Type of flight region 2 [command rate] | (dim) |
| L317 | 5722.0 | Parameter code for termination of region 2 [θ_m] | (dim) |
| L318 | $\hat{\theta}_{m2}$ | Command attitude to terminate region 2 | (deg) |
| L319 | Q_{m2} | Pitch rate for region 2 | (deg/sec) |
| L322 | 1.0 | Type of flight region 3 [command rate] | (dim) |

| | | | |
|------|--------|--|-----------|
| L323 | 5310.0 | Parameter code for termination region 3 | (dim) |
| L324 | 0.0 | Angle of attack to terminate region 3 | (deg) |
| L325 | 0.0 | Pitch rate for region 3 | (deg/sec) |
| L328 | 2.0 | Type of flight region 4 [gravity turn] | (dim) |
| L329 | 5000.0 | Parameter code for termination of region 4 [t] | (dim) |
| L330 | 2000.0 | Time to terminate region 4 | (sec) |
| L331 | 0.0 | Angle of attack for region 4 | (deg) |

(5) Payload to Circular Orbit

If $K_{sh} = 3$, apply the following logic and equations:

Estimated required Ideal Velocity

| | | | |
|------------------------|-----------------|-----------------------|----------|
| $\Delta V = 24753.331$ | $+ 16.17$ | h_{c0} | (nmi) |
| | $- 8.8850495$ | t_{B1} | (sec) |
| | $+ .38179208$ | t_{B1}^2 | |
| | $+ 9.4$ | t_{B2} | (sec) |
| | $- .52$ | t_{B3} | (sec) |
| | $- 856.07602$ | v_2 | (dim) |
| | $+ 9742.4243$ | v_3 | (dim) |
| | $- 1585.8688$ | $\bar{\omega}/\omega$ | (dim) |
| | $- .046233604$ | h_0 | (ft) |
| | $- 2.6770574$ | v_0 | (ft/sec) |
| | $+ .0020621782$ | v_0^2 | |

Payload Iteration Procedure

Ideal Velocity Equation

$$\Delta V^{\ell} = \bar{g}_e \sum_{k=k_k}^{n_k} t_{speff}^{\ell n} \frac{W_{PL}^{\ell} + W_{PLO_k}^{\ell}}{W_{PL}^{\ell} + W_{PLO_k}^{\ell} - \Delta W_k}$$

Initial guess for W_{PL}

For $\ell = 1$ $W_{PL}^{\ell=1} = W_{PLO_{k=k_k}} / 30.0$

For $\ell = 2$ $W_{PL}^{\ell=2} = 1.01 W_{PL}^{\ell}$

$$\text{For } \ell = 3 \quad W_{PL}^{\ell=3} = W_{PL}^{\ell=1} - \frac{(\hat{\Delta V} - \Delta V^{\ell-1})(W_{PL}^{\ell-1} - W_{FL}^{\ell-2})}{(\Delta V^{\ell-2} - \Delta V^{\ell-1})}$$

If $W_{PL}^{\ell} < 0$, then set $W_{PL}^{\ell} = W_{PL}^{\ell-1}/2.0$

If $\frac{\hat{\Delta V} - \Delta V^{\ell}}{\Delta V} < 0.00004$, terminate iteration

If $\ell = 100$, terminate run and print

"PAYLOAD WEIGHT ITERATION DID NOT CONVERGE"

At the termination of the payload weight iteration,

set $W_{PL} = W_{PL}^{\ell}$

Vehicle Liftoff Weight

$$W_T = W_{PL} + \sum_{k=k_k}^{n_k} W_{MOK} + W_{COK}$$

Velocity at Pitch Over

$$V_{PO} = \begin{cases} 170.0 & \text{If } V_{eo} = 160.0 \\ V_{eo} + 10.0 & \text{Otherwise} \end{cases}$$

Circular Orbital Altitude

$$h_{CO} = S_{sh} \times 6076.10333$$

Inertial Circular Orbital Velocity

$$V_{ICO} = \left[\frac{g_e r_e^2}{(h_{CO} + r_e)} \right]^{\frac{1}{2}}$$

where

the gravitational constant is:

$$v_{CO} = \begin{cases} 32.14625 & \text{If } g'_e = 0 \\ g'_e & \text{Otherwise} \end{cases}$$

and earth radius is:

$$r_e = \begin{cases} 20,926,400.0 & \text{If } r'_e = 0 \\ r'_e & \text{Otherwise} \end{cases}$$

Pitch Over Pitch Rate

$$Q_{m2} = - \{ 2,186.428 + \ln (W_T) [-218.16888 + 6.4511537 \ln (W_T)] \} / W_T^{1/3}$$

Pitch Over Angle

θ_{m2} for $V_0 \leq 160$ feet per second:

$$\begin{aligned} \theta_{m2} = & -20.618013 + .1013901 & h_{CO} & \text{(nmi)} \\ & - .000083344619 & h_{CU}^2 & \\ & + .7863 & t_{B1} & \text{(sec)} \\ & + .0752 & t_{B2} & \text{(sec)} \\ & - .0032 & t_{B3} & \text{(sec)} \\ & + 19.666608 & v_2 & \text{(dim)} \\ & + 92.727271 & v_3 & \text{(dim)} \\ & - .33013554 & \bar{\omega}/\omega & \text{(dim)} \\ & - .00020876696 & h_0 & \text{(ft)} \\ & - .011349661 & v_0 & \text{(ft/sec)} \\ & + 33.876497 & Q_{m2}^{-1} & \text{(deg/sec)} \end{aligned}$$

(6) Initial flight path angle to terminate next to last stage

| | | | |
|----------------------------------|------------------|------------------|----------|
| $\hat{\gamma}_{1g} = -4.3479152$ | + .0014201471 | h_{CO_2} | (nmi) |
| | + .000014699632 | h_{CO} | |
| | - .010439863 | t_{31} | (sec) |
| | + .00024116553 | t_{B1}^2 | |
| | + .0047000003 | t_{B2} | (sec) |
| | + .075800000 | t_{B3} | (sec) |
| | - 3.1327416 | v_2 | (dim) |
| | + 20.151515 | v_3 | (dim) |
| | - .84360441 | \dot{m}/ω | (dim) |
| | - .000020950557 | h_0 | (ft) |
| | - .00128745 | v_0 | (ft/sec) |
| | + .0000013688082 | v_0^2 | |

Initial Conditions

(deg)
(deg)

Initial flight path angle
Initial command attitude

L11 90.0
L28 90.0

Hunting Procedure P1

(dim)

Hunting procedure P1 flag

L73 0.0

Hunting Procedure P2

(dim)
(dim)
(min)
(dbi)
(dim)
(dim)
(lb)
(lb)
(dim)
(ft/sec)
(ft/sec)
(dim)
(lb)
(dim)
(deg)
(deg)

Hunting procedure P2 flag [linear model]
Model accuracy
Run time
Isolation=maximized parameter [undefined]
Trajectory limit number beyond base array
First independent variable code $\{W_{PL}\}$
Initial value of first independent variable
Incremental value of first independent variable
First dependent variable code $\{V_I\}$
First dependent variable isolation value
Tolerance of first isolated variable
Transformation flag, first independent variable
Transformation constant, first independent variable
Second independent variable code $\{K_{f2}\}$
Initial value of second independent variable
Incremental value of second independent variable

L64 1.0
L87 0.0
L88 0.0
L89 0.0
L90 20.0
L91 20.0
L92 W_{PL}
L93 $0.1 \times W_{PL}$
L94 5050.0
L96 V_{IC0}
L97 5.0
L98 0.0
L99 0.0
L100 319.0
L101 $\hat{\theta}_{m2}$
L102 2.0

Hunting Procedure P2 (Continued)

| | | | |
|------|---------------------|--|-------|
| L103 | 5330.0 | Second dependent variable code 7 _{II} | (dim) |
| L105 | 0.0 | Second dependent variable isolation value | (deg) |
| L106 | 0.01 | Tolerance of second isolated variable | (deg) |
| L107 | 0.0 | Transformation flag, second independent variable | (dim) |
| L108 | 0.0 | Transformation constant, second independent variable | (deg) |
| L109 | $(n_{k-1})1000 + 3$ | Third independent variable code $[k_3(n_{k-1})]$ | (dim) |
| L110 | $\hat{y}ig$ | Initial value of third independent variable | (deg) |
| L111 | 2.0 | Incremental value of third independent variable | (deg) |
| L112 | 5028.0 | Third dependent variable code [h] | (dim) |
| L114 | h_{CO} | Third dependent variable isolation value | (ft) |
| L115 | 100.0 | Tolerance of third isolated variable | (ft) |
| L116 | 0.0 | Transformation flag, third independent variable | (dim) |
| L117 | 0.0 | Transformation constant, third independent variable | (ft) |
| L154 | $0.2 w_T$ | Upper limit first independent variable | (lb) |
| L155 | 90.0 | Upper limit second independent variable | (deg) |
| L156 | 20.0 | Upper limit third independent variable | (deg) |
| L161 | 0.0 | Lower limit first independent variable | (lb) |
| L162 | 20.0 | Lower limit second independent variable | (deg) |
| L163 | 0.0 | Lower limit third independent variable | (deg) |

Main Print

| | | | |
|------|--------|--------------------------|-------|
| L184 | 10.0 | Main print time interval | (sec) |
| L185 | 2000.0 | Main print time limit | (sec) |

Discontinuity Print

| | | | |
|------|-------|---|-------|
| L252 | 310.0 | Code for discontinuity print at end of vertical rise | (dim) |
| L253 | 317.0 | Code for discontinuity print at end of pitchover | (dim) |
| L254 | 324.0 | Code for discontinuity print at start of gravity turn | (dim) |

Attitude Control

| | | | |
|------|------------------|---|------------|
| L310 | 1.0 | Type of flight region 1 [command rate] | (dim) |
| L311 | 5046.0 | Parameter code for termination of region 1 [V_e] | (dim) |
| L312 | V_{p0} | Velocity to terminate region 1 | (ft./sec) |
| L313 | 0.0 | Pitch rate for region 1 | (deg./sec) |
| L316 | 1.0 | Type of flight region 2 [command rate] | (dim) |
| L317 | 5722.0 | Parameter code for termination of region 2 [θ_m] | (dim) |
| L318 | $\hat{\theta}_m$ | Command attitude to terminate region 2 | (deg) |
| L319 | Q_{m2} | Pitch rate for region 2 | (deg./sec) |
| L322 | 1.0 | Type of flight region 3 [command rate] | (dim) |
| L323 | 5310.0 | Parameter code for termination region 3 | (deg) |
| L324 | 0.0 | Angle of attack to terminate region 3 | (deg) |
| L325 | 0.0 | Pitch rate for region 3 | (deg./sec) |
| L328 | 2.0 | Type of flight region 4 [gravity turn] | (dim) |
| L329 | 5009.0 | Parameter code for termination of region 4 [ft] | (dim) |
| L330 | 2000.0 | Time to terminate region 4 | (sec) |
| L331 | 0.0 | Angle of attack for region 4 | (deg) |

Termination of Next to Last Stage

| | | | | |
|--------------|----------|--------|---------------------------------------|-------|
| $L(n_{k-1})$ | 1000 + 0 | 5330.0 | Stage termination variable code [γII] | (dim) |
| $L(n_{k-1})$ | 1000 + 1 | 0.0 | Termination constant 1 | (dim) |
| $L(n_{k-1})$ | 1000 + 2 | 0.0 | Termination constant 2 | (dim) |
| $L(n_{k-1})$ | 1000 + 3 | 718 | Termination isolation value | (deg) |

(7) Shaper Subroutine Nomenclature

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|--|--------------|
| GH | Gravitational Constant (32.14625) | ft/sec**2 |
| HGO | Circular orbital altitude | nm |
| HO | Initial altitude | ft |
| ISPC | Comp specific impulse used to find vehicle weight flow | sec |
| ISPPFF | Stage effective specific impulse | sec |
| ISM | Main specific impulse used to find vehicle weight flow | sec |
| IVC | Integral of the complementary vacuum thrust table | lb-sec |
| IVM | Integral of the main vacuum thrust table | lb-sec |
| IVT | Integral of the main and complementary vacuum thrust table | lb-sec |
| JC | Number of data in complementary thrust-weight table | -- |
| JM | Number of data in main thrust-weight table | -- |
| KEC | Multiplier of the complementary stage vacuum thrust | -- |
| KEM | Multiplier of the main stage vacuum thrust | -- |
| KK | Stage number | -- |
| KNOK | Complementary thrust-weight table wt carry-over flag | -- |
| KOK | Main thrust-weight table weight carry-over flag | -- |
| KSH | Control Flag indicating type of flight | -- |
| KTC | Time multiplier for the complementary thrust table | -- |
| KTM | Time multiplier for the main thrust table | -- |
| KWC | Input complementary weight flow multiplier | -- |
| KWM | Input main weight flow multiplier | -- |
| NK | Largest stage number containing a non-zero input sigma | -- |
| QMP | Pitch over pitch rate | deg./sec |

| <u>Symbol</u> | <u>Definition</u> | <u>Unit</u> |
|---------------|--|-------------|
| RE | Radius of the earth (20,924,400) | ft |
| SSH | Target range or orbital altitude | nm |
| TR | Stage duration | sec |
| TRJM | Stage time of last main thrust-weight point | sec |
| TCJ | Complementary thrust-weight switching times | sec |
| TIJ | Main thrust-weight switching times | sec |
| TICJ | Complementary thrust-weight switching times (stage start) | sec |
| TIMJ | Main thrust-weight switching time from stage initiation | sec |
| VEO | Missile velocity at trajectory start time | ft/sec |
| VICO | Inertial circular orbital velocity | ft/sec |
| VO | Initial velocity of vehicle | ft/sec |
| VPO | Velocity at pitchover | ft/sec |
| WB | Stage weight | lb |
| WBK | Total missile weight at the termination of Kth stage | lb |
| WCO | Initial complementary weight | lb |
| WCOK | Initial complementary weight for the Kth stage | lb |
| WDOT CJ | Complementary weight flow at T'CJ, J = 1, ..., 25 per stage | lb/sec |
| WDOT MJ | Main weight flow at T'MJ, J = 1, ..., 25 per stage | lb/sec |
| WMO | Initial main weight | lb |
| WOV | Carry-over weight | lb |
| WPL | Weight of payload | lb |
| WPLOK | Propulsion system liftoff weight of Kth stage | lb |
| WT | Vehicle liftoff weight | lb |
| GAMA IG | Inertial flight path angle to termination next to last stage | deg |
| DELTA V | Total ideal velocity of missile | ft/sec |
| DELTA WMI | Integral of the main weight | lb |

| <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------|---|--------------|
| DELTA W | Total expended weight | lb |
| DELTA WCF | Expended complementary propellant weight | lb |
| DELTA WCFK | Expended complementary propellant weight of Kth stage | lb |
| DELTA WCI | Complementary weight flow integral | lb |
| DELTA WCIK | Complementary weight flow integral of the Kth stage | lb |
| DELTA WK | Total expended weight of Kth stage | lb |
| DELTA WMF | Expended main propellant weight | lb |
| THETA M2 | Pitch over angle between launch horizontal and command control line | deg |
| THETA HAM2 | Initial value of theta M2 | deg |
| NU 2 | Ratio of stage two weight to stage one weight, initially | -- |
| NU 3 | Ratio of stage 3 weight to stage one weight, initially | -- |
| OMEG/OMEG | Earth rotation factor | -- |

M. INPUT

Load sheets are provided to facilitate data input and are shown at the end of this section. Utilization of the load sheets are explained below.

1. GENERAL INPUT

It is possible to submit any load sheet as the first or last page of the basic deck or run. Any load sheet not required may be deleted from the basic deck or run. Columns one through seventy-two are available for program input. Because of program logic regarding the basic deck system, a minus zero is never input.

Unless a quantity is input in the basic deck or run, that quantity will be zero unless special program logic apply.

The decimal point will be input with the number in the load sheet. If the decimal point is not specified for an input quantity, the decimal will be assumed after the last input integer of that quantity.

If the value of the desired input is too large or too small to satisfactorily indicate it in the spaces provided, write the number, the letter "E" and the power of ten the number is to be multiplied by. If no decimal is specified for the number, the decimal is assumed after the last integer before the "E".

The first entry for all tables must appear at the top of the table. The independent variables specified in the load sheets must be filled out monotonically, but the last value may be input before the table ends.

Load sheet pages 11 and beyond can be used for first, second, third, or fourth stage. The desired stage is designated by inserting the stage number in the box following the "L".

Inputs in L0, L1, and L2 are the identification basic deck, reference run, and run. The basic deck and the run number must be nonzero in order for the trajectory to run. These identification numbers are printed at the top of each page of output.

2. INPUT L-NUMBER LIST

| <u>L-number</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-----------------|---------------|---|--------------|
| L0000 | BD | Input basic deck number | dim |
| L0001 | RR | Input reference run number | dim |
| L0002 | RUN | Input run number | |
| L0003 | K_k^1 | Input stage start control function. If 1, 2, 3, or 4, the run starts at the initiation of the first, second, third, or fourth stage, respectively if input zero set is equal to 1 | dim |
| L0004 | t_o | Input trajectory start time | sec |
| L0005 | t_k^1 | Input start time with the initial stage K_k | sec |
| L0006 | T_{yk}^1 | Input initial or restart type of flight control flag | dim |
| L0007 | M_y^1 | Input initial or restart type of mode control flag | dim |
| L0008 | S_y | Input initial or restart special print flag | dim |
| L0009 | D_y | Input initial or restart discontinuity print flag | dim |
| L0010 | V_{eo} | Input missile velocity at the trajectory start time | ft/sec |
| L0011 | γ_{10} | Input flight path angle at the trajectory start time, $-180^\circ < \gamma_{10} \leq 180^\circ$ | deg |
| L0012 | h_o | Input missile altitude at the trajectory start time | ft |
| L0013 | S_o | Input missile ground range at the trajectory start time | ft |
| L0014 | ψ_i | Input flight plane azimuth angle. Angle measured north to the flight plane, $-180^\circ \leq \psi \leq 180^\circ$ | deg |
| L0015 | θ_i | Input inertial elevation axis Euler angle relating the i and e_o systems | deg |
| L0016 | ϕ_i | Input inertial meridional axis Euler angle relating the i and e_o systems | deg |

| <u>L-number</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-----------------|-----------------|--|---------------------|
| L0017 | ρ_L | Input launch latitude, $-90^\circ \leq \rho \leq 90^\circ$ | deg |
| L0018 | μ_L | Input launcher longitude | deg |
| L0019 | h_L | Input launcher altitude | ft |
| L0020 | W_{PL} | Input payload weight | lb |
| L0021 | h_E | Input altitude above which ambient pressure and aerodynamic forces are zero and speed of sound is 1,000 ft/sec. If input zero is set to 300,000 ft | ft |
| L0022 | | Open | |
| L0023 | J | Input gravitational value which accounts for the earth's oblateness | dim |
| L0024 | \bar{g}_e | Input mass conversion gravity. If input zero, set equal to 32.174 | ft/sec ² |
| L0025 | g_e' | Input gravitational acceleration at the surface of the reference body. If input zero, set equal to 32.14625 | ft/sec ² |
| L0026 | r_e' | Input geometric radius of the earth. If input zero, set equal to 20,926,400 | ft |
| L0027 | ω | Input magnitude of the earth's angular velocity. If input greater than 0.5, set equal to 7.29211 E-5 | rad/sec |
| L0028 | Q_{mo} | Input initial command pitch attitude | deg |
| L0029 | ψ_{mo} | Input initial commanded yaw attitude | deg |
| L0030 | ϕ_{mo} | Input initial commanded roll attitude | deg |
| L0031 | Q_{bo} | Input initial vehicle pitch rate | deg/sec |
| L0032 | R_{bo} | Input initial vehicle yaw rate | deg/sec |
| L0033 | P_{bo} | Input initial vehicle roll rate | deg/sec |
| L0034 | θ_{bo} | Input pitch orientation angle at the trajectory start time, $-180^\circ < \theta_{bo} \leq 180^\circ$ | deg |
| L0035 | ϵ_{bo} | Input yaw orientation angle at the trajectory start time $-180^\circ < \epsilon_{bo} \leq 180^\circ$ | deg |

| <u>L-number</u> | <u>Symbol</u> | <u>Definitions</u> | <u>Units</u> |
|-----------------|------------------|---|--------------|
| L0036 | ϕ_{so} | Input roll orientation angle at the trajectory start time $-180^\circ < \phi_{so} \leq 180^\circ$ | deg |
| L0037 | $K_{cl,2}$ | Input lower and upper limits, respectively, for computation of orbital elements and impact determination computations | dbi |
| L0039 | h_f | Input altitude at the termination of the glide phase | ft |
| L0040 | K_γ | Input glide phase termination control function. A value of plus one will specify impact after apogee, while a minus one will specify impact before apogee | dim |
| L0041 | σ_c | Input code which designates the quantity that determines the flight region when the orbital elements and impact determination are desired | dim |
| L0042 | h_e | Input altitude of atmospheric entry | ft |
| L0043 | S_{co} | Input initial earth surface cross-range at trajectory start time | n.m. |
| L0044 | γ_{20} | Input azimuthal flight path angle at trajectory start time | deg |
| L0045 | | Open | |
| L0046 | $\tilde{\psi}_g$ | Input generalized coordinate orientation angle. Second rotation angle (about the resulting Z axis after rotating through θ_g , $\tilde{\psi}_g$, and ϕ_g) | deg |
| L0047 | θ_g | Input generalized coordinate orientation for velocity steering. First rotation angle (about the Y_e -axis) of the set θ_g , $\tilde{\psi}_g$, and ϕ_g . | deg |
| L0048 | ϕ_g | Input generalized coordinate orientation angle. Final rotation angle (about the X_g axis) of the set θ_g , $\tilde{\psi}_g$, and ϕ_g . | deg |
| L0049, 52, etc. | W_{JTj} | Input weight to be jettisoned when τ_j parameter had K_j value | lb |
| L0050, 53, etc. | σ_{Jj} | Input code which designates the quantity that determines when the W_{JT} weight is to be jettisoned where $j = 1, 2, \dots, \text{or } 8$ | dim |
| L0051, 54, etc. | K_{Jj} | Input value of that parameter at which the weight W_{JTj} is to be jettisoned where $j = 1, 2, \dots, \text{or } 8$ | dbi |
| L0073 | P_1 | Input flag so specify hunt procedure (P1) | dim |
| L0074 | K_S | Input stage print control function. A non-zero value is required to print the trajectory at the termination of each stage during the hunting procedure | dim |

| <u>L-number</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-----------------|---------------|---|--------------|
| L0075 | n_{tl} | Input trajectory number limit. No more than n trajectories will be computed during the hunting procedure (P1) by varying X | dim |
| L0076 | K_a | Input isolation-maximization control function. If zero, isolation is specified and if nonzero, maximization of the dependent variables will occur used in hunting procedure (P1) | dim |
| L0077 | σ_X | Input code which designates the independent variable in the hunting procedure (P1) | dim |
| L0078 | σ_a | Input code which designates the dependent variable in the hunting procedure (P1) | dim |
| L0080 | X_i | Input value of the first guess of X used in hunting procedure | dbi |
| L0081 | ΔX | Input increments that X is incremented during the hunting procedure (P1) | dbi |
| L0082 | a_f | Input value of the dependent variable to be isolated by the hunting procedure (P1) | dbi |
| L0083 | Δa | Input hunting procedure (P1) values that "a" should be computed within the isolation or maximization routine | dbi |
| L0084 | P_2 | Input flag to specify hunt procedure (P2). If $P_2 = 0$, by-pass hunt procedure 2; $P_2 = 1$, use a linear response; $ P_2 = 2$, use a quadratic response surface where +2 maximizes and -2 minimizes; $ P_2 = 3$, use an incomplete quadratic response surface where +3 maximizes and -3 minimizes | dim |
| L0085 | σ_z | Input code. The σ_z identifies the dependent variable being maximized or minimized. Used in hunt procedure (P2). If $\sigma_z < 0$, the values of x_1, x_2, \dots, x_{in} | dim |
| L0086 | ϵ_z | Input value specifying the tolerance of the predicted maximization parameter (z). Used in the hunt procedure (P2) | dbi |
| L0087 | ϵ_m | Input flag to specify model error used in hunt procedure (P2). If $\epsilon_m < 0$, the model will be iterated until an extremal solution has a 95 percent probable model error. If $\epsilon_m = 0$, the extremal solution is obtained without regard to probable model error | dim |

| <u>L-number</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------------|-----------------|---|--------------|
| L0088 | | Open | |
| L0089 | f_D | Input and flag specifying maximization and isolation of the same parameter used in hunt procedure (P2). If f_D is nonzero, the function f is maximized relative to the independent variables x_2, x_3, \dots, x_n and is isolated to a value f_D by varying x_1 | dbi |
| L0090 | n_{t2} | Input specified maximum number of hunt predictions (P2) beyond the initial array. If n_{t2} is input a negative number, the hunt will restart after $ n_{t2} $ iterations | dim |
| L0091, 100, etc. | σ_{xj} | Input code which designates the independent variables used in hunting procedure (P2) where $j = 1, 2, \dots, 7$ | dim |
| L0092, 101, etc. | x_{ij} | Input initial array reference independent variable designated by code input that is used in hunting procedure (P2) | dbi |
| L0093, 102, etc. | Δx_{ij} | Input increment of x_{ij} used in incrementing during hunting procedure (P2), $j = 1, 2, \dots, 7$ | dbi |
| L0094, 103, etc. | σ_{yj} | Input code which designates the dependent variables used in hunting procedure (P2) where $j = 1, 2, \dots, 7$ | dim |
| L0095, 104, etc. | y_{Li} | Input desired dependent variable or lower constraint boundary of the dependent variable designated by code input that is used in hunting procedure (P2) where $j = 1, 2, \dots, 7$ | dbi |
| L0096 105, etc. | y_{Ui} | Input upper constraint boundary of the dependent variable designated by code input that is used in hunting procedure (P2) where $j = 1, 2, \dots, 7$ | dbi |
| L0097, 106, etc. | ϵ_{cj} | Input tolerance on the j -th condition of constraint used in hunt procedure (P2) where $j = 1, 2, \dots, 7$ | dbi |
| L0098 107, etc. | T_{Tj} | Input transformation flag used in hunting procedure (P2) $j = 1, 2, \dots, 7$ | dim |
| L0099 108, etc. | a_{Tj} | Input transformation constant used in the simultaneous hunting procedure (P2) $j = 1, 2, \dots, 7$ | dbi |

| <u>L-number</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|------------------|--------------------------|--|--------------|
| L0154-160 | x_{Uj} | Input upper limit that an independent variable may assume a value used in hunt procedure (P2) where $j = 1, 2, \dots, 7$ | dbi |
| L0161-167 | x_{Lj} | Input lower limit that an independent variable may assume a value in hunt procedure (P2) where $j = 1, 2, \dots, 7$ | dbi |
| L0168, 170, etc. | Δt_{cj} | Input computing interval during $t_{cj-1} \leq t \leq t_{cj}$ where $j = 1, 2, \dots, 8$ | sec |
| L0169, 171, etc. | t_{cj} | Input limit of the computing interval Δt_{cj} where $j = 1, 2, \dots, 8$ | sec |
| L0184, 186, etc. | Δt_{pj} | Input main printing interval during $t_{p(j-1)} \leq t \leq t_{pj}$ where $j = 1, 2, \dots, 8$ | sec |
| L0185, 187, etc. | t_{pj} | Input limit of the main printline print interval where $j = 1, 2, \dots, 8$ | sec |
| L0200-205 | PL-DA GB,K,KB, N,0 | Input flag where nonzero values are required if printlines DA, GB, K, KB, N, C are desired | dim |
| L0206-208 | | Open | |
| L0209-219 | σ_{pj} | Input code designates the quantity to be printed in printline Z where $j = 1, 2, \dots, 8$ | sec |
| L0220, 222, etc. | Δt_{pj} | Input auxiliary printline interval during $t_{p(j-1)} \leq t \leq t_{pj}$ where $j = 1, 2, \dots, 8$ | sec |
| L0221, 223, etc. | t_{pj} | Input limit of the auxiliary printline print interval where $j = 1, 2, \dots, 11$ | sec |
| L0236, 238, etc. | σ_{tj} | Input code which designates the quantity that determines when to print a special time where $j = 1, 2, \dots, 8$ | dim |
| L0237, 239, etc. | K_{tj} | Input value when a trajectory printout is desired where $j = 1, 2, \dots, 8$ | dbi |
| L0252-259 | σ_{Dj} | Input code which designates the quantity that determines when to print a discontinuity where $j = 1, 2, \dots, 8$ | dim |
| L0260, 262, etc. | T_{mj} | Input max print region flag | dim |

| <u>L-number</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------------|---------------|---|--------------|
| L0261, 263, etc. | σ_{mj} | Input code which designates the quantity whose maximum value is to be printed following each stage time where $j = 1, 2, \dots, 5$ | dbi |
| L0270, 272, etc. | T_{Bj} | Input staging values flag, $j = 1, 2, \dots, 5$ | dim |
| L0271, 273, etc. | σ_{Bj} | Input code which designates the quantities whose values at staging are to be available to the hunting procedure, $j = 1, 2, \dots, 5$ | dim |
| L0280, 282, etc. | σ_{Aj} | Input code which designates the integration tolerance parameters where $j = 1, 2, \dots, \text{or } 7$ | dbi |
| L0281, 283, etc. | A'_{ri} | Input and utilized relative integration tolerance, $j = 1, 2, \dots, 7$ | dbi |
| L0304-305 | | Open | |
| L0306 | A'_t | Input absolute allowable break-up tolerance of time | dim |
| L0307 | B'_t | Input relative allowable break-up tolerance of time | dim |
| L0308 | A'_x | Input absolute allowable break-up tolerance of target value | sec |
| L0309 | B'_x | Input relative allowable break-up tolerance of target value | dim |
| L0310 317, etc. | T_{yj} | Input and output type of flight control flag where $j = 1, 2, \dots, \text{or } 16$ | dim |
| L0311, 318, etc. | σ_{fj} | Input code which designates the quantity that determines when the j -th type of flight ends where $j = 1, 2, \dots, 16$ | dim |
| L0312, 319, etc. | K_{fj} | Input limit of the j -th type of flight where $j = 1, 2, \dots, \text{or } 16$ | dbi |
| L0313, 320, etc. | Q_{mj} | Input vehicle pitch turning rate. Positive if the vehicle is intended to pitch up ($Ty=1$) | deg/sec |
| | α_c | Input commanded angle of attack used in the constant angle of attack and angle of side slip ($Ty=2$) | deg |
| | h_{cj} | Input commanded altitude used in the constant altitude type of flight ($Ty=8$) | ft |

| <u>L-number</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------------|-----------------|--|--------------|
| | η_{cj} | Input command load factor for constant load factor type of flight where $j = 1, 2, \dots$, or 13 (Ty=5) | g's |
| | τ_{MIj} | Input guidance associated first order intercept guidance controller time constant used in type 10 flight where $j = 1, 2, \dots$, or 13 | sec |
| | K_{HGj} | Input navigation constant used in the Homing Guidance (Ty=11) | dim |
| L0314, 321, etc. | R_{mj} | Input vehicle yaw turning rate positive if the vehicle is intended to turn right (Ty=1) | deg/sec |
| | β_{cj} | Input commanded angle of side slip used in the constant angle of attack and angle of side slip (Ty=2) | deg |
| | ω_{zj} | Input attitude control frequency used in constant attitude type of flight where $j = 1, 2, \dots, 16$ (Ty=8) | rad/sec |
| | η_{ctj} | Input command load factor crosswise to the velocity vector used for constant load factor type of flight where $j = 1, 2, \dots$, (Ty=9) | g's |
| | τ_{IGj} | Input pitch and yaw flare-in factor used in the Intercept Guidance (Ty=10) | sec |
| | τ_{HGj} | Input pitch and yaw flare-in factor used in the Homing Guidance (Ty=11) | sec |
| L0315, 322, etc. | P_{mj} | Input vehicle roll turning rate positive if the vehicle is intended to roll clockwise looking at it from the aft end (Ty=1) | deg/sec |
| | ϕ_{cj} | Input command roll attitude used in the constant angle of attack and angle of side slip type of flight (Ty=7) | deg |
| | ζ_{zj} | Input constant attitude (Ty=8) attitude control damping ratio where $j = 1, 2, \dots$, or 16 | dim |
| | ϕ_{cj} | Input command roll attitude used in the constant load factor type of flight where $j = 1, 2, \dots$, or 13 (Ty=9) | |
| | α_{maxj} | Input limit of angle of attack during the j-th type of flight | deg |

| <u>L-number</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------------|----------------|---|--------------|
| L0316, 323, etc. | τ_{nj} | Input flare-in time constant for constant load factor type of flight ($T_y=9$) | g's |
| L0401-406 | | Open | |
| L0407 | K_h | Input wind altitude multiplier and flag. If zero, no wind effects are considered | dbi |
| L0408 | K_v | Input wind speed multiplier | dbi |
| L0409 | K_ψ | Input wind azimuth multiplier | dim |
| L0410, 413, etc. | h_j | Input wind velocity altitude associated with v_{wj} and ψ_{wj} where $j = 1, 2, \dots, 30$ | dbi dbi |
| L0411, 414, etc. | v_{wj} | Input (with altitude h) wind speeds where $j = 1, 2, \dots, 30$ | ft/sec |
| L0412, 415, etc. | ψ_{wj} | Input instantaneous (with altitude h_j) wind azimuth angles, measured in a plane parallel to the local tangent plane where $j = 1, 2, \dots, 30$. Angle measured clockwise from north to the direction from which the wind is coming. | deg and dbi |
| L0500-597 | | Reserved for Aerodynamic Coefficient Calculation Routine | |
| L0598 | K_{sh} | Input shaper control flag where: if it equals 0, ignore routine 1. maximize range 2. maximize payload to a given range or, 3. determine payload to a circular orbit | |
| L0599 | S_{sh} | Input target range or orbital altitude | n.m. |
| L0600, 603, etc. | M_{yj} | Input and output mode type control where $j = 1, 2, \dots, 10$. If 1 rigid body with controls, and 2 rigid body with controls | dim |
| L0601, 604, etc. | J_{mj} | Input code which designates the quantity that determines when the J-th mode type ends where $j = 1, 2, \dots, 10$ | dim |
| L0602, 605, etc. | K_{mj} | Input quantity which designates the limit of the j-th mode type end where $j = 1, 2, \dots, 10$ | dim |
| L0630 | σ_{Tto} | Input code designating start of target maneuvering | dim |
| L0631 | K_{Tto} | Input quantity which designates the start of target maneuvering | dbi |

| <u>L-number</u> | <u>Symbol</u> | <u>Definitions</u> | <u>Units</u> |
|---------------------|---------------|--|--------------|
| L0632 | v_{T0} | Input target initial velocity at start of target maneuvering | ft/sec |
| L0633 | γ_{T0} | Input initial target flight path angle at start of target maneuvering | deg |
| L0634 | h_{T5} | Input target initial altitude at the start of the target maneuvering | ft |
| L0635 | ζ_{T0} | Input initial target azimuthal flight path angle at start of target maneuvering | deg |
| L0636 | S_{T0} | Input initial target position down range | n.m. |
| L0637 | S_{TC0} | Input initial target position cross range | n.m. |
| L0638-639 | | Open | |
| L0640 644, etc. | t_{Tj} | Input target time terminating the j-th target acceleration value of dynamical condition table | |
| L0641, 645, etc. | a_{TTj} | Input target earth reference acceleration tangential to the target velocity vector for the j-th period of the target dynamical condition table | g's |
| L0642, 646, etc. | a_{TNj} | Input target earth reference acceleration normal to the target velocity vector for the j-th period of the target dynamical condition table | g's |
| L0643, 647, etc. | a_{TCj} | Input target earth reference acceleration cross-wise to the target velocity vector for the j-th period of the target dynamical condition table | g's |
| L0668-669 | | Open | |
| L0670 | Δ_{dc} | Input value of number of desired duty cycle points (100 maximum) if input zero, set equal to 50 | dim |
| L0671 | K_{dc} | Input and output stage number of TVC duty cycle stage | dim |
| L0672 | h_{α} | Input final attitude of maximum wind shear used in TVC duty cycle slew rate calculations | ft |
| L0673 | h_{β} | Input initial altitude of maximum wind shear used in TVC duty cycle slew rate calculations | ft |
| L0674 | ω_s | Input slew frequency used in the TVC design stage slew rate calculations | rad/sec |

| <u>L-number</u> | <u>Symbol</u> | <u>Definitions</u> | <u>Units</u> |
|-----------------|---------------|---|--------------|
| L0675 | FWI | Input stage I vacuum thrust to liftoff weight used in the vehicle characteristics pertinent to roll requirement | g's |
| L0676 | W_{ol} | Input stage I liftoff weight used in roll control requirements | lb |
| L0677 | W_{TVC} | Input and output estimated TVC system fixed weight. Used in TVC design stage for the reflly option | lb |
| L0678 | W_{exi} | Input estimated weight of the TVC system expend weight during the TVC design stage during the original vehicle flight | lb |
| L0679 | I_{spaug} | Input and output estimated TVC system caused specific impulse augmentation (positive) or degradation (negative). Used in trajectory TVC Design program reflly | sec |
| L0680 | x_{nf} | Input body station of nozzle flange. Used in the TVC design program | ft |
| L0681 | δ_{me} | Input maximum vector angle design limit also output in TVC design duty cycle | deg |
| L0682 | h_{mxwd} | Input altitude of maximum wind velocity. Also flag to set up wind table per MMREM wind shear criteria | ft |
| L0683 | K_{TPF} | Input titled print flag | dim |
| L0684 | 799 | Reserved for plotter option | |

| <u>L-number</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|---------------------|----------------|--|--------------------|
| L0800, 810, etc. | F_{yj} | Input thrust control law code for the j-th type of TMC table | dim |
| L0801, 811, etc. | σ_{Fyj} | Input code which designates the quantity that determines when the j-th type of TMC ends | dim |
| L0802, 812, etc. | K_{Fyj} | Input limit of the j-th type TMC | dbi |
| L0803, 813, etc. | TMC_j | Input thrust dynamic mode of the j-th type TMC | dim |
| L0804, 814, etc. | C_{Fyj} | Input thrust system proportionality system gain of the j-th type TMC | dim |
| L0805, 815, etc. | τ_{Fyj} | Input control system time constant of the j-th type TMC | sec |
| L0806, 816, etc. | MIN_j | Input minimum velocity or constant Mach number of the j-th type of TMC | dim/ft/sec |
| L0807, 817, etc. | q_{maxj} | Input maximum allowable dynamic pressure of the j-th type of TMC | lb/ft ² |
| L0808, 818, etc. | q_{min} | Input minimum allowable dynamic pressure of the j-th type of TMC | lb/ft ² |
| L0809, 819, etc. | | Open | |
| L0870, 872, etc. | t_{VPj} | Input time value for Specific Velocity - Time Profile used in $Fy=1$ TMC $j = 1, 2, \dots, 15$ | sec |
| L0871, 873, etc. | V_{VPj} | Input earth reference velocity for the Specific Velocity - Time Profile used in $Fy=1$ TMC $j = 1, 2, \dots, 15$ | ft/sec |
| L0900-999 | | Special Coding | |

The following parameters are input for each stage. The first digit of the L-number indicates the stage number.

| <u>L-number</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-----------------|---------------|--|-----------------|
| K000* | σ_{Sk} | Input code which designates the quantity that determines when a stage is terminated where $k = 1, 2, 3, 4$ | dim |
| K001 | D_p | Input diameter of propellant | in |
| K002 | r'_{b1000} | Input burnrate of propellant at 1000 lb/in ² chamber pressure and flag to determine evaluation option | in/sec |
| K003 | K_3 | Input quantity which determines stage termination | dbi |
| K004 | I'_{VT} | Input total of the main and complementary vacuum impulse | lb/sec |
| K005 | I'_{VM} | input main stage total vacuum impulse | lb/sec |
| K006 | W_{MO} | Input initial main weight for the k-th stage | lb |
| K007 | K_{FM} | Input multipliers of the main vacuum thrust | dim |
| K008 | K_{WM} | Input mainweight flow multiplier. If input zero is set to 1.0 | dim |
| K009 | K'_{tm} | Input main switching time multipliers. If zero, the program assumes a value of one. If σ_s is designated at t_B , then K_3 is multiplied by K'_{tm} . | dbi |
| K010 | I_{spM} | Input main specific impulse used to compute vehicle weight flow. If zero, weight flow is determined from the input weightflow. Also output in the TVC duty cycle. | sec |
| K011 | A'_{em} | Input main thrust-weight table input stage nozzle exit area | ft ² |
| K012 | K_{Ok} | Input main thrust-weight table weight carry-over flag for the k-th stage. If zero, separation has occurred with regards to the main and complementary weights. If non-zero, the main weight at the termination of the k-1 stage is used as the initial main weight of the k-th stage | dim |
| K013 | ϵ_d | Input and output nozzle expansion ratio used in the separated flow nozzle thrust equations | dim |

The following parameters are input for each stage. The first digit of the L-number indicates the stage number.

| <u>L-number</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-----------------|---------------|--|-----------------|
| K000* | σ_{Sk} | Input code which designates the quantity that determines when a stage is terminated where $k = 1, 2, 3, 4$ | dim |
| K001 | D_p | Input diameter of propellant | in |
| K002 | r'_{b1000} | Input burnrate of propellant at 1000 lb/in. ² chamber pressure and flag to determine evaluation option | in/sec |
| K003 | K_3 | Input quantity which determines stage termination | dbi |
| K004 | I'_{VT} | Input total of the main and complementary vacuum impulse | lb/sec |
| K005 | I'_{VM} | Input main stage total vacuum impulse | lb/sec |
| K006 | W_{MO} | Input initial main weight for the k-th stage | lb |
| K007 | K_{FM} | Input multipliers of the main vacuum thrust | dim |
| K008 | K'_{tm} | Input main weight flow multiplier. If input zero is set to 1.0 | dim |
| K009 | K'_{tm} | Input main switching time multipliers. If zero, the program assumes a value of one. If σ_s is designated at t_B , then K_3 is multiplied by K'_{tm} . | dbi |
| K010 | I_{spm} | Input main specific impulse used to compute vehicle weight flow. If zero, weight flow is determined from the input weight flow. Also output in the TVC duty cycle. | sec |
| K011 | A'_{eM} | Input main thrust-weight table input stage nozzle exit area | ft ² |
| K012 | K_{Ok} | Input main thrust-weight table weight carry-over flag for the k-th stage. If zero, separation has occurred with regards to the main and complementary weights. If non-zero, the main weight at the termination of the k-1 stage is used as the initial main weight of the k-th stage | dim |
| K013 | ϵ_d | Input and output nozzle expansion ratio used in the separated flow nozzle thrust equations | dim |

| <u>L-number</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|--------------------|----------------|---|----------------------|
| K014 | γ_d' | Input and output calculated ratio of specific heats of the rocket motor exhaust gases. If input zero 1.18 is used. Used in separated flow nozzle thrust equations | dim |
| K015 | C_d' | Input and calculated nozzle efficiency coefficient used in the separated flow nozzle thrust equation | dim |
| K016 | α_d' | Input nozzle half angle used in the separated flow nozzle thrust equation. | deg |
| K017 | a_s' | Input nozzle separation polynomial coefficient used in the separated flow nozzle thrust equation. If input zero is set to 0.3 | dim |
| K018 | b_s' | Input nozzle separation polynomial coefficient used in the separated flow nozzle thrust equation if input zero is set to 0.7 | dim |
| K019 | c_s' | Input nozzle separation polynomial coefficient used in the separated flow nozzle thrust equation. If input zero is set to 0.884 | dim |
| K020 | P_{aRM} | Input main table thrust reference atmospheric pressure | lb/ft ² |
| K021, 024, etc. | P_{Mj} | Input value of the main vacuum thrust to be used during $t_{Mj} \leq t < t_{Mj+1}$ where $j = 1, 2, \dots, 25$ per stage | lb |
| K022, 025, etc. | \dot{W}_{Mj} | Input main weight flow at t_{Mj}' where $j = 1, 2, \dots, 25$ per stage | lb/sec |
| K023, 026, etc. | t_{Mj}' | Input main thrust-weight switching time from stage initiation where $j = 2, 3, \dots$, or 25 per stage | sec |
| K095 | ρ_p | Density of propellant used in Internal Ballistic evaluation is set to 0.063 if not input | lb/in ³ |
| K096 | τ_w | Web fraction used in internal ballistic evaluation is set to 0.8 if not input | dim |
| K097 | n | Burnrate exponent used in internal ballistic evaluation is set to 0.6 if not input | dim |
| K098 | α_p | Propellant diffusivity used in internal ballistic evaluation is set to 0.00027 if not input | in ² /sec |
| K099 | P_{max} | Maximum allowable chamber pressure used in internal ballistic evaluation | lb/in ² |

| <u>N-number</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-------------------|----------------|---|--------------------|
| K100 | K'_{FC} | Input multiplier of the complementary vacuum thrust. If input zero for the k-th stage and $I'_{VT} = I_{VT} = 0$, the complementary thrust for the k-th stage are zero | dim |
| K101 | K'_{WC} | Input complementary weight flow multiplier. If input zero is set to 1.0 | dim |
| K102 | K'_{tc} | Input complementary switching time multiplier. If zero, the program assumes a value of one. | dim |
| K103 | I'_{spC} | Input complementary specific impulse used to compute vehicle weight flow. If zero weight flow is determined from input weight flow. | sec |
| K104 | A_{eC} | Input complementary thrust-weight table stage nozzle exit area | ft ² |
| K105 | W_{Cok} | Input initial complementary weight for the k-th stage | lb |
| K106 | I'_{VC} | Input complementary stage total vacuum impulse | lb-sec |
| K107 | K_{NOK} | Input complementary thrust-weight table weight carryover flag for the k-th stage. If K_{Ok} and K_{NOK} are non-zero, separation has occurred with regards to the complementary weight. If K_{Ok} is non-zero and K_{NOK} is zero, the total vehicle weight at the termination of the k-1 stage is used as the initial weight of the k-th stage | dim |
| K108 | K_{BD} | Input flag which stipulates that the main nozzle exit area will be used in the base drag calculations when splitting main and complementary tables to allow for up to 47 thrust time points | dim |
| K109 | P_{arC} | Input complementary table thrust reference atmospheric pressure | lb/ft ² |
| K111, 114 etc | t'_{Cj} | Input complementary thrust-weight switching time from stage initiation where $j = 1, 2, 3, \dots, 25$ per stage | sec |
| K112, 115, etc | F_{Cj} | Input value of the complementary vacuum thrust to be used during $t_{Cj} \leq t \leq t_{C(j+1)}$ where $j = 1, 2, \dots, 25$ per stage | lb |
| K113, 116 etc | \dot{W}_{Cj} | Input complementary weight flow at t'_{Cj} where $j = 1, 2, \dots, 25$ per stage | lb/sec |
| K185 | S_{RC} | Input aerodynamic chord force coefficient reference areas | sq ft |

| <u>L-number</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|--------------------|--------------------------|--|--|
| K186 | \bar{C}' | Input stage axial force control function and multiplier. If input zero, the multiplier is set to one; if non-zero, the axial force is determined from input and multiplied by \bar{C} | dim |
| K187 | | Open | |
| K188, 190, etc. | M_{Aj} | Input Mach number for aerodynamic axial representation where $j = 1, 2, \dots, 15$ per stage | dim |
| K189, 191, etc. | C_{Aj} | Input and instantaneous (with Mach number M_j) aerodynamic axial force coefficients, respectively, where $j = 1, 2, \dots, 15$ per stage | dim |
| K218 | S_{PF} | Input missile platform area used in calculating tumbling aerodynamic axial force coefficients | sq ft |
| K219 | x_{pc} | Input missile body station of the centroid of the platform area | ft |
| K220 | S_{RN} | Input aerodynamic normal force coefficient reference area | sq ft |
| K221 | \bar{N}_k | Input normal force control function and normal force multiplier. If input zero, the multiplier is set to one and if non-zero, the normal force is determined from input and multiplied by N_k where $k = 1, 2, 3, 4$ | dim |
| K222 | \bar{x}_{cp} | Input stage aerodynamic normal force center of pressure multiplier | dbi |
| K223, 228, etc. | M_{Nj} | Input Mach number for aerodynamic normal force coefficient representation where $j = 1, 2, \dots, 15$ per stage | dim |
| K224-226 | $C_{N1,2,3j}$ | Input values of $C_{N1,2,3}$ respectively, corresponding to M_j where $j = 1, 2, \dots, 15$ per stage | deg/deg ² /deg ³ |
| K227, 232, etc. | x_{cpj} | Input and output instantaneous (with Mach number M) aerodynamic normal force center of pressure body station numbers, respectively, where $j = 1, 2, \dots, 15$ per stage | dbi and ft |
| K298 | D_{RN} | Input aerodynamic reference diameter | ft |
| K299 | \bar{M}_Q | Input aerodynamic pitch damping moment due to pitch rate multiplier | dim |
| K300 | $\bar{M}_{\dot{\alpha}}$ | Input aerodynamic pitch damping moment due to rate change of angle of attack multiplier | dim |

| <u>L-number</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|------------------|----------------------|--|--------------|
| K301 | K_Q | Input aerodynamic pitch damping moment due to pitch rate multiplier | dim |
| K302 | x'_{RQ} | Input and calculated pitch damping moment due to pitch rate reference moment point body station | dbi and ft |
| K303 | $K_{\dot{\alpha}}$ | Input aerodynamic pitch damping moment due to time rate change of angle of attack multiplier | dim |
| K304 | $x'_{R\dot{\alpha}}$ | Input and calculated pitch damping moment due to rate change of angle of attack reference moment point body station | dbi and ft |
| K305,308, etc | M_{Dj} | Input Mach number for aerodynamic representation where $j = 1, 2, \dots, 15$ per stage | dim |
| K306,309 etc | C_{MQj} | Input aerodynamic pitch damping moment due to pitch rate coefficient where $j = 1, 2, \dots, 15$ per stage | /deg |
| K307,310 etc | $C_{M\dot{\alpha}j}$ | Input aerodynamic pitch damping moment due to rate change of angle of attack coefficient where $j = 1, 2, \dots, 15$ per stage | /deg |
| K350-379 | | Open | |
| K380 | n'_m | Input and output internally calculated number of motors in the stage cluster | dim |
| K381 | n'_c | Input and output internally calculated number of control nozzles for the cluster motor logic | dim |
| K382 | R_c | Input radius of cluster for the k-th stage | ft |
| K383 | σ_{It} | Input standard deviation of the ratio of total impulse to nominal total impulse for the k-th stage | dim |
| K384 | σ_{tb} | Input standard deviation of the ratio of web burntime to nominal burntime for the k-th stage | dim |
| K385 | ϕ_v | Input bivariant consideration axis for the k-th stage | deg |
| K386 | Δ_1 | Input amplitude of limit cycle for the k-th stage | |
| K387 | K'_{Δ} | Input side impulse multiplier. If input zero is set to one | dim |
| K388 | ω_L | Input frequency of limit cycle for the k-th stage | rad/sec |

| <u>L-number</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-----------------|----------------|--|---|
| K389 | δ_{MP} | Input nozzle misalignment angle in pitch | deg |
| K390 | δ_{MY} | Input nozzle misalignment angle in yaw | deg |
| K391-392 | $a_{o,jk}$ | Input constants used in the Z_{gg} and constant components nontarget dependent pitch steering equations for the k-th stage | rad |
| K393-395 | b_{jk} | Input constants used in the \ddot{x}_{gg} , x_{gg}^2 , and \dot{x}_{gg}^3 components of the nontarget dependent pitch steering equation for the k-th stage $j = 1, 2, 3$ | rad-sec/ft rad-sec ² /ft and rad-sec |
| K396 | τ_{fk} | Input pitch flare-in time constant for k-th stage used in velocity steering type of flight ($T_y=4$) | sec |
| K397 | σ_{g1k} | Input code which designates the start of the acquisition zone for evaluation of the steering equations coefficients for the k-th stage $k = 1, 2, 3$, or 4 | dbi |
| K398 | K_{g1k} | Input quantity which designates the start of the acquisition zone for evaluation of the steering equation coefficient for the k-th stage $k = 1, 2, 3$, or 4 | dbi |
| K399 | σ_{g2k} | Input quantity which designates the end of the acquisition zone for evaluation of the steering equation coefficient for the k-th stage, $k = 1, 2, 3$, or 4 | dbi |
| K400 | K_{g2k} | Input quantity which designates the end of the acquisition zone for evaluation of the steering equation coefficient for the k-th stage, $k = 1, 2, 3$, or 4 | dbi |
| K401 | K_{yk} | Input gain constant in the nontarget dependent yaw steering equation for the k-th stage | dim |
| K402 | τ_{yk} | Input time constant in the nontarget dependent yaw steering equation for the k-th stage | sec |
| K403 | δ_{MR} | Input roll system fin misalignment angle | deg |
| K404 | $L_{\delta R}$ | Input roll fin radial center of pressure to missile centerline distance | ft |
| K405 | K_{RC} | Input roll control system flag. If equal 1, an auxiliary roll thruster system is simulated. If equal 2, aerodynamic central fins are used | dim |

| <u>L-number</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-----------------|----------------------------------|---|-----------------|
| K406 | n_{vr} | Input disturbing roll nozzle vortex multiplier. If not input is set to 0.00363 | ft |
| K407 | ω_{pc} | Pintle control frequency | rad/sec |
| K408-416 | | Open | |
| K417 | x'_{pf} | Input stage forward end of propellant grain body station | ft |
| K418 | x'_{pa} | Input stage aft end of propellant grain body station | ft |
| K419 | x'_E | Input and computed stage nozzle exit body station | ft |
| K420-421 | $\delta_{p0}, \dot{\delta}_{p0}$ | Input per stage initial pitch thrust vector deflection angle and angular rate at the trajectory initiation or stage initiation | deg and deg/sec |
| K422-423 | $\delta_{y0}, \dot{\delta}_{y0}$ | Input per stage initial yaw thrust vector deflection angle and angular rate at the trajectory initiation or stage initiation | deg and deg/sec |
| K424 | F_{R0} | Input per stage initial roll thrust | lb |
| K425-427 | | Open | |
| K428 | ΔQ_b | Input stage pitch attitude reaction angular impulse; i.e., added to A_b at staging | deg |
| K429 | ΔR_b | Input stage yaw attitude reaction angular impulse; i.e., added to ψ_b at staging | deg |
| K430 | \bar{x}_e | Input stage thrust gimbal position multiplier | dbi |
| K431 | x'_e | Input stage thrust gimbal position body station | ft |
| K432 | y'_e | Input stage thrust gimbal yaw eccentricities. Positive in the Y_b axis direction. | ft |
| K433 | z_e | Input stage thrust gimbal pitch point eccentricities, respectively. Positive in the Z_b axis direction | dbi and ft |
| K434 | K_δ | Input thrust control flag. If zero, control thrust is determined from instantaneous vehicle thrust. If one, the control thrust is obtained from the instantaneous main stage thrust, if two control thrust is nonexistent | dim |
| K435 | τ_c | Input stage pitch and yaw control systems time constant for the thrust vector deflection first order transfer function | sec |

| <u>L-number</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-----------------|---------------|--|--|
| K436 | ζ_c | Input stage pitch control systems damping ratio for the thrust vector deflection second order transfer function | dim |
| K437 | ω_c | Input stage pitch control systems forcing frequency for the thrust vector deflection second order transfer function | rad/sec |
| K438 | ζ_v | Input vehicle controlled damping ratio | dim |
| K439 | ω_v | Input vehicle controlled frequency for the k-th stage | rad/sec |
| K440-449 | L_j | Input control system where $j = 1, 2, \dots, 10$ per stage. If zero, a limit is not applied; otherwise, L_j limits the following parameters where the statement number is j (1) $K_{DP} \Delta \theta_b$, (2) δ_{pc} , (3) δ_p , (4) $\delta_{\dot{p}}$ and (5) $\ddot{\delta}_p$ (6) $K_{EI} \Delta \theta_b$, (7) δ_{yc} , (8) δ_y , (9) $\dot{\delta}_y$ (10) $\ddot{\delta}_y$ | deg deg deg deg/sec deg/sec ² |
| K450, 459 etc | K_{DPj} | Input control system pitch attitude error gain for the j-th control region $j = 1, 2$, or 3 | dim |
| K451, 460 etc | K_{DYj} | Input control system yaw attitude error gain for the j-th control region $j = 1, 2$, or 3 | dim |
| K452, 461 etc | K_{RPj} | Input control system pitch attitude rate gain for the j-th control region $j = 1, 2$, or 3 | sec |
| K453, 462 etc | K_{RYj} | Input control system yaw attitude rate gain for the j-th control region $j = 1, 2$, or 3 | sec |
| K454, 463 etc | K_{IPj} | Input pitch angle of attack gain for the j-th control region $j = 1, 2$, or 3. | dim |
| K455, 464 etc | K_{IYD} | Input your angle of side slip gain for the j-th control region $j=1, 2$, or 3 | |
| K456, 465 etc | f_{Gik} | Input attitude control system gain control flag. If equal to zero, input gains are utilized; if not equal to zero, the automatic gains are utilized for the j-th control zone $i = 1, 2$, or 3; and k-th stage, $k = 1, 2, 3$, or 4 | dim |
| K457, 466 | σ_{Gj} | Input code which designates attitude control system gain zone limits ($j = 1, 2$, or 3) | dim |
| K458, 467 | K_{Gik} | Input attitude control system gain zone limits ($i = 1, 2$, or 3) and the k-th stage $k = 1, 2, 3$, or 4 | dbi |
| K475 | \bar{I}_y | Input moment of inertia multiplier | dbi |

| <u>L-number</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|------------------|---------------|--|----------------------|
| K476 | \bar{I}_Z | Input yaw moment of inertia multiplier | dbi |
| K477 | \bar{I}_X | Input roll moment of inertia multiplier | dbi |
| K478 | \bar{W} | Input stage weight multiplier. If input zero, is set internally to one and if nonzero, the input weight used in the mass properties table W_j ($j = 1, 2, \dots, 15$) is multiplied by W | dim |
| K479 | x_{cg} | Input stage center of gravity position multiplier | dbi |
| K480 | z'_{cg} | Input center-of-gravity offset bias distance, in pitch, positive down | dbi |
| K481 | y'_{cg} | Input center-of-gravity offset bias distance in yaw, positive to the right | dbi |
| K482 | W_n | Input stage movable portion nozzle weight | lb |
| K483 | I_n | Input stage movable portion nozzle moment of inertia about the gimbal point | slug-ft ² |
| K484 | x_n | Input stage movable portion of nozzle center-of-gravity body station | dbi |
| K485-487 | | Open | |
| K488- 498 etc | W_j | Input vehicle weight to relate the input moment of inertia values $j = 1, 2, \dots, 15$ per stage | lb |
| K489, 499 etc | x_{cgj} | Input instantaneous (with total vehicle weight, W_j) center-of-gravity body station numbers, respectively, where $j = 1, 2, \dots, 15$ per stage | dbi and ft |
| K490, 500 etc | I_{Yj} | Input total vehicle pitch moment of inertia corresponding to the total vehicle weight input W_j where $j = 1, 2, \dots, 15$ per stage | dbi |
| K491, 501 etc | z_{cgj} | Input instantaneous (with total vehicle weight, W_j) center of gravity offsets, respectively, where $j = 1, 2, \dots, 15$ per stage. Positive in the Z_b axis direction | dbi and ft |
| K492, 502 | I_{Zj} | Input total vehicle yaw moment of inertia corresponding to the total vehicle weight input W_j where $j = 1, 2, \dots, 15$ per stage | slug-ft ² |
| K493, 503 | y_{cyj} | Input instantaneous (with total vehicle weight, W_j) center of gravity butt line number, where $j = 1, 2, \dots, 15$ per stage | dbi and ft |

| <u>L-number</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-------------------|----------------|---|----------------------|
| K494, 504 | I_{Xj} | Input total vehicle roll moment of inertia weight input W_j , where $j = 1, 2, \dots, 15$ per stage | slug ft ² |
| K495, 505 | I_{XYj} | Input total vehicle roll-yaw product of inertia corresponding to the total weight input W_j , where $j = 1, 2, \dots, 15$ per stage | slug ft ² |
| K496, 506 | I_{YZj} | Input total vehicle yaw pitch product of inertia corresponding to the total vehicle weight input W_j , where $j = 1, 2, \dots, 15$ per stage | slug ft ² |
| K497, 507 | I_{ZXj} | Input total vehicle pitch-roll product of inertia corresponding to the total vehicle weight input W_j , where $j = 1, 2, \dots, 15$ per stage | slug ft ² |
| K638, 648 658 | l_{Ri} | Input thruster roll control lever arm for the i -th center zone | ft |
| K639, 649 659 | τ_{Ri} | Input stage roll control system time constant, for the first order transfer | sec |
| K640, 650 660 | D_i | Input roll control system hysteresis for the i -th zone, $i = 1, 2, \text{ or } 3$ | dim |
| K641, 651, 661 | $F_{\Delta i}$ | Input maximum roll control thrust for the i -th zone, $i = 1, 2, \text{ or } 3$ | lb |
| K642, 652, 662 | L_{RCi} | Input maximum roll control thrust for the i -th zone, $i = 1, 2, \text{ or } 3$ | lb |
| K643, 653 663 | τ_{DRi} | Input roll control system attitude error gain for the i -th zone, $i = 1, 2, \text{ or } 3$ | dim |
| K644, 654 664 | | Open | |
| K645, 655 665 | K_{RRi} | Input roll control system attitude rate gain for the i -th zone, $i = 1, 2, \text{ or } 3$ | sec |
| K646, 656 666 | I_{SPRi} | Input roll control motor specific impulse for the i -th zone, $i = 1, 2, \text{ or } 3$ | sec |
| K647, 667 | t_{Ri}^1 | Input operating time from stage initiation of the roll control function for the i -th zone, $i = 2, 3$ | sec |
| K667, 670 | S_{RRI} | Input reference area of the i -th raceway, $i = 1, 2$ | ft ² |

| <u>L-number</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-----------------|-----------------|---|--------------|
| K668, 671 | r_{Ri} | Input distance from the vehicle centerline to the i-th raceway center of pressure $i = 1, 2$ | ft |
| K669, 672 | ϕ_{Ri} | Input bank angle location of the i-th raceway where $i = 1, 2$. As seen from the rear of the vehicle, a positive angle is measured clockwise from the Z_b axis direction | deg |
| K673, 675, etc | M'_{Rj} | Input Mach number for aerodynamic rolling moment, $j = 1, 2, \dots, 10$ | dim |
| K674, 676, etc | C_{RRj} | Input raceway aerodynamic force coefficient corresponding to the M_{Rj} , $j = 1, 2, \dots, 10$ | dim |
| K693-699 | | Open | |
| K700 | S_{Fz} | Input aerodynamic pitch fin lift and drag coefficient reference area | sq ft |
| K701 | x_{hz} | Input missile body station of the pitch fin hinge axis | ft |
| K702 | U_{hz} | Input pitch movable control fin hinge axis to the leading fin base root location distance to the pitch fin base root length ratio | dim |
| K703 | L_{bz} | Input pitch fin base root length | ft |
| K704 | K_{ycf} | Input aerodynamic yaw fin deflection angle multiplier | dim |
| K705 | K_{pcf} | Input aerodynamic pitch fin deflection angle multiplier | dim |
| K706 | \bar{C}'_{Lz} | Input aerodynamic linear pitch fin lift coefficient multiplier. If input zero is set to 1.0 | dim |
| K707 | \bar{C}'_{Dz} | Input aerodynamic nonlinear pitch fin drag coefficient multiplier. If input zero is set to 1.0 | dim |
| K708 | \bar{C}'_{Dz} | Input aerodynamic pitch fin drag coefficient multiplier. If zero set equal to one | dim |
| K709 | \bar{K}'_{Lz} | Input aerodynamic pitch fin drag due to lift multiplier. If zero set equal to one | dim |
| K710, 716, etc | MF_j | Input mach number for aerodynamic fin representation where $j = 1, 2, \dots, 15$ per stage | dim |
| K711, 717, etc | C_{Lzj} | Input and calculated aerodynamic pitch fin nonlinear lift coefficient $j = 1, 2, \dots, 15$ per stage | 2/deg |

| <u>L-number</u> | <u>Symbol</u> | <u>Definition</u> | <u>Units</u> |
|-------------------|---------------|---|--------------------|
| K712, 718 etc | C_{1zj} | Input and calculated aerodynamic pitch fin nonlinear lift coefficient $j = 1, 2, \dots,$ 15 per stage | 1/deg ² |
| K713, 719, etc | C_{Dzj} | Input aerodynamic pitch fin drag coefficient $j = 1, 2, \dots, 15$ per stage | dim |
| K714, 720, etc | K_{Lzj} | Input aerodynamic pitch fin drag due to lift factor | rad |
| K715, 721, etc | U_{czj} | Input pitch aerodynamic control fin center of pressure as a ratio of fin chord length | dim |
| K800-999 | | Open | |

3.

SWITCHING CODE

Quantities which can be involved as switching functions or in the hunting procedure are assigned a code number shown in succeeding pages. The code number is input in the appropriate space on the load sheet and the program determines the parameter which corresponds to the code number. The parameter and not the code input is used in program equations and logic.

The input parameter code is designated by inputting the L-number (delete the "L" of the parameters). These parameters can be used only as independent variables in the hunting procedure.

If the sigma code number is input negatively, the absolute value of the parameter is then utilized in the program equations and logic .

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|---|
| 5000 | T | t | Instantaneous time (sec) |
| 5001 | TB | t_B | Time from the current stage initiation (sec) |
| 5002 | TB2 | t_{B2} | Time from Stage II initiation zero if I-II staging has not occurred (sec) |
| 5003 | TB3 | t_{B3} | Time from Stage III initiation zero if II-III staging has not occurred (sec) |
| 5004 | TB4 | t_{B4} | Time from Stage IV initiation zero if III-IV staging has not occurred (sec) |
| 5005 | SST | t_k | Stage start time (sec) |
| 5006 | SST2 | SST_2 | Start time stage II (sec) |
| 5007 | SST3 | SST_3 | Start time stage III (sec) |
| 5008 | SST4 | SST_4 | Start time stage IV (sec) |
| 5009 | TBF | t_{Bf} | Trajectory burnout time for the stage below (sec) |
| 5010 | TT | t_T | Time from target maneuvering initiation (sec) |
| 5011 | TTS | t_{TS} | Target start time (sec) |
| 5012 | TA | t_a | Total flight time to the glide phase apogee altitude (sec) |
| 5013 | TE | t_e | Total flight time to atmospheric entry (sec) |
| 5014 | TF | t_f | Total flight time to the termination of the glide phase (sec) |
| 5014 | PERIOD | P | Glide phase orbital period (min) |
| 5016-5017 | | | Open |
| 5018 | RANGE | S | Missile ground range. Distance along the surface of the earth measured clockwise from the launch vertical to the local vertical down range (ft) |
| 5019 | SD | \dot{S} | Time rate change of missile down range (ft/sec) |
| 5020 | SC | S_c | Missile cross ground range. Distance along earth surface from the launch vertical to the local vertical crosswise from launch azimuth (ft) |
| 5021 | SCD | \dot{S}_c | Time rate change of missile cross range (ft/sec) |
| 5022 | SA | S_a | Total missile ground range at flight apogee (nm) |

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|---|
| 5023 | SE | S_E | Total missile ground range to atmospheric entry (nm) |
| 5024 | SF | S_F | Total missile ground range at the termination of the glide phase (nm) |
| 5025 | SS | S_S | Missile slant ground range. Distance along earth surface from the launch vertical to the local vertical slantwise (ft) |
| 5026-5027 | | | Open |
| 5028 | H | h | Missile geometric altitude. Distance between the surface of the reference body and the missile measured along the local vertical. Positive away from the reference body (ft) |
| 5029 | HD | \dot{h} | Time rate change of missile geometric altitude. Rate between the surface of the reference body and missile measured along the local vertical positive away from the reference body (ft/sec) |
| 5030 | HDD | \ddot{h} | Instantaneous altitude acceleration (ft/sec ²) |
| 5031 | HA | H_a | Apogee altitude of the missile during the glide phase (nm) |
| 5032 | HP | h_p | Perigee altitude of the missile during the glide phase (nm) |
| 5033 | HAP | h_{ap} | Height of apogee + perigee (nm) |
| 5034 | HAB | h_{ab} | Altitude above launcher (ft) |
| 5035 | RC | r_c | Instantaneous distance between the center of the reference body and the missile (ft) |
| 5036-5037 | | | Open |
| 5038 | GXI | g_{xi} | Local northerly component of gravity (ft/sec ²) |
| 5039 | GYI | g_{yi} | Local easterly component of gravity (ft/sec ²) |
| 5040 | GZI | g_{zi} | Local downward component of gravity (ft/sec ²) |
| 5041 | GXE | g_{xe} | Launch centered earth fixed northerly component of gravity (ft/sec ²) |
| 5042 | GYE | g_{ye} | Launch centered earth fixed easterly component of gravity (ft/sec ²) |
| 5043 | GZE | g_{ze} | Launch centered earth fixed downward component of gravity (ft/sec ²) |
| 5044-5045 | | | Open |

| <u>L-number</u> | <u>FOLTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definitions</u> |
|-----------------|---------------------------|------------------------------|--|
| 5046 | VE | V_e | Missile earth referenced velocity (ft/sec) |
| 5047 | VDE | \dot{V}_e | Time rate change of missile earth reference velocity (ft/sec ²) |
| 5048 | VEK | V_{ek} | Earth fixed velocity at stages (ft/sec) |
| 5049 | VA | V_a | Missile velocity with respect to air (ft/sec) |
| 5050 | VI | V_I | Missile inertial velocity (ft/sec) |
| 5051 | VIA | V_{Ia} | Missile inertial velocity at apogee if powered flight ends at the time being printed (ft/sec) |
| 5052 | VIF | V_{If} | Missile inertial velocity at apogee and impact of intercept, respectively, if powered flight and the atmosphere end at the time being printed (ft/sec) |
| 5053-5055 | | | Open |
| 5056 | VW | v_w | Instantaneous wind speeds and time rate change respectively (ft/sec and ft/sec ²) |
| 5057 | VDW | \dot{v}_w | Open |
| 5058 | VAE | V_{aE} | Velocity with respect to the ambient air at entry (ft/sec) |
| 5059 | VIE | V_{IE} | Inertial velocity at entry conditions (ft/sec) |
| 5060 | VXXX | V_{xxx} | Command velocity used in the TMC command logic. V_{ecv} if $F_y = 1$, V_{ecm} if $F_y = 4$ (ft/sec ²) |
| 5061 | VDXXX | \dot{V}_{xxx} | Command acceleration used in the TMC command logic. \dot{V}_{ecv} if $F_y = 1$, \dot{V}_{ecm} if $F_y = 2$, and zero if $F_y = 1$ and $F_y = 2$ (ft/sec ²) |
| 5062 | VDECO | \dot{V}_{ecq} | Command acceleration to constrain dynamic pressure used in the TMC command logic (ft/sec ²) |
| 5063 | *MACH | M | Missile Mach number (dim) |
| 5064-5065 | | | Open |
| 5066 | CAV | C_a | Speed of sound at the missile (ft/sec) |
| 5067 | DCATDH | dC_a/dh | Partial derivative of the speed of sound with altitude (1/sec) |
| 5068 | PA | P_a | Ambient pressure at the missile (lb/ft ²) |

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|---|
| 5069 | DPADH | dp_a/dh | Partial derivative of ambient pressure with altitude (lb/ft) |
| 5070 | Q | q | Missile dynamic pressure (lb/ft ²) |
| 5071 | PCC | P_{cc} | Commanded chamber pressure used in pintle motor control logic (lb/in ²) |
| 5072 | PSTAR | P^* | Main motor nozzle critical pressure used in separated flow equations (lb/in ²) |
| 5073 | PS | P_s | Main motor nozzle separation pressure used in separated flow equations (lb/in ²) |
| 5074 | PE | P_e | Main motor exit pressure used in separated flow equations (lb/in ²) |
| 5075 | EPSILS | ϵ_s | Main motor nozzle separation expansion ratio used in separated flow equation (dim) |
| 5076 | | | Open |
| 5077 | GWI | $\%WI$ | Percent web (dim) |
| 5078 | VCI | V_{cI} | Chamber volume (in ³) |
| 5079 | ASI | A_{sI} | Burn surface area (in ²) |
| 5080 | ATCC | A_{tcc} | Commanded throat area (in ²) |
| 5081 | CF | C_{FI} | Thrust coefficient (dim) |
| 5082 | CFO | C_{FO} | Thrust coefficient at optimum expansion ($P_e = P_a$) (dim) |
| 5083 | OMEGAP | ω_p | Pintle control frequency (rad/sec) |
| 5084 | GPI | $\%PI$ | Fraction of propellant removed (dim) |
| 5085 | AXI | A_{XI} | Propellant extinguishment throat area (in ²) |
| 5086-5091 | | | Open |
| 5092 | *MASS | m | Instantaneous missile mass (lb-sec ² /ft) |
| 5093 | W | W | Total instantaneous missile weight and total expended instantaneous missile flow respectively (lb and lb/sec) |
| 5094 | WD | \dot{W} | |
| 5095 | WB | W_B | Instantaneous gross vehicle weight minus the useful load (lb) |

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definitions</u> |
|-----------------|----------------------------|------------------------------|---|
| 5096 | WJT | W_{JT} | Total weight jettisoned |
| 5097 | WM | W_M | Total instantaneous expended main weight and weight flow respectively (lb and lb/sec) |
| 5098 | WDM | \dot{W}_M | |
| 5099 | WC | W_C | Total instantaneous expended main weight and weight flow respective! (lb and lb/sec) |
| 5100 | WDC | \dot{W}_C | |
| 5101 | WS | W_S | Stage weight (lb) |
| 5102 | WSMAIN | W_{SM} | Initial weight of main motor (lb) |
| 5103 | WSCOMP | W_{SC} | Initial weight of complementing motor (lb) |
| 5104 | PIVM | I''_{VM} | Vacuum impulse under input main thrust curve (lb-sec) |
| 5105 | PIVC | I''_{VC} | Vacuum impulse under input complement any thrust curve (lb-sec) |
| 5106-5108 | | | Open |
| 5109 | EOM | E/m | Total missile energy per unit mass during the glide phase. Potential energy ₂ at the launcher is taken as zero (ft ² sec ²) |
| 5110 | QAP | q_{α}' | Product of total angle of attack and dynamic pressure (lb/deg/ft ²) |
| 5111 | INCL | i | Orbital inclination angle (deg) time rate change respectively |
| 5112 | E | e | Eccentricity of the missile path during the glide phase (dim) |
| 5113 | LLR | L_r | Missile travel distance on the rail launcher used in ground launch tape of flight (Ty=6) (ft) |
| 5114 | PHIA4 | ϕ_{a4} | Glide range angle to the apogee vertical (deg) |
| 5115 | FOWD | $ F/\dot{W} $ | Instantaneous effective specific impulse (sec) |
| 5116 | IBDDP | $\bar{I}_{\delta p}$ | Sum of pitch angular thrust vectoring velocities from stage initiation to the time being printed corrected for dither (deg) |
| 5117 | IBDDY | $\bar{I}_{\delta y}$ | Sum of yaw angular thrust vectoring velocities from stage initiation to the time being printed corrected for dither (deg) |
| 5118 | LV | L_v | Output ideal velocity vectoring losses (ft/sec) |
| 5119-5121 | | | Open |

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|--|
| 5122 | F | F | Total instantaneous thrust acting along missile centerline. Positive when thrust vector points forward along missile centerline (lb) |
| 5123 | FVAC | F_v | Instantaneous total vacuum thrust (lb) |
| 5124 | FM | F_M | Instantaneous main thrust (lb) |
| 5125 | FMV | F_{MV} | Instantaneous main vacuum thrust and thrust rate respectively (lb and lb/sec) |
| 5126 | FDMV | F_{MV} | |
| 5127 | FC | F_C | Instantaneous complementary thrust (lb) |
| 5128 | FCV | F_{CV} | Instantaneous complementary vacuum thrust and time rate respectively (lb and lb/sec) |
| 5129 | FDCV | F_{CV} | |
| 5130 | FCOM | F_{com} | Commanded altitude thrust used in TMC logic (lb) |
| 5131 | FVCOM | F_{vcom} | Commanded vacuum thrust used in TMC logic (lb) |
| 5132 | FVN | F_{VN} | Nominal vacuum thrust used in TMC logic (lb) |
| 5133 | FN | F_N | Nominal altitude thrust used in TMC Logic (lb) |
| 5134 | FHATC | F_c | Thrust required to maintain V_e ; i.e., retarding axial force used in TMC logic (lb) |
| 5135 | FCQMIN | F_{cqmin} | Require thrust so that the vehicle will maintain the minimum dynamic pressure used in TMC logic (lb) |
| 5136 | FCQMAX | F_{cqmax} | Maximum thrust so that the vehicle will not exceed the maximum dynamic pressured used in TMC logic (lb) |
| 5137 | FCALOS | F_{CALOS} | Command thrust to provide acceleration proportional to LOS rated used in TMC logic (lb) |
| 5138 | FCCLOS | F_{cclos} | Command thrust to provide a minimum missile to target closing rate used in TMC logic (lb) |
| 5139-5140 | | | Open |
| 5141 | FX | F_x | Components of total vehicle thrust parallel to the coordinate axes of the b system (lb) |
| 5142 | FY | F_y | Components of total vehicle thrust parallel to the coordinate axes of the b system (lb) |
| 5143 | FZ | F_z | Components of total vehicle thrust parallel to the coordinate axes of the b system (lb) |
| 5144 | FFX | F_x | Thrust force along nozzle centerline (lb) |

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|--|
| 5145 | FYY | F_Y | Component of total vehicle thrust moved to nozzle centerline; positive right (lb) |
| 5146 | FZZ | F_Z | Component of total vehicle thrust normal to nozzle centerline; positive down (lb) |
| 5147 | FTDY | F_{TDy} | Movable nozzle tail-wag-dog force in yaw positive to the right (lb) |
| 5148 | FTDZ | F_{TDz} | Movable nozzle tail-wag-dog force in pitch positive to the down (lb) |
| 5149 | FJDY | F_{JFy} | Jet damping yawing transverse force (lb) |
| 5150 | FJDZ | F_{JDz} | Jet damping pitching transverse force (lb) |
| 5151-5153 | | | Open |
| 5154 | DRL | D_{rz} | Rail launch friction drag (lb) |
| 5133 | CDELZ | $C_{\delta z}$ | Aerodynamic pitch fin axial force (lb) |
| 5156 | NDELY | $N_{\delta y}$ | Aerodynamic yaw fin normal force (lb) |
| 5157 | NDELZ | $N_{\delta z}$ | Aerodynamic pitch fin normal force (lb) |
| 5158 | NPAC | N_{PAC} | Pitch aerodynamic control normal force per radian fin deflection angle (lb) |
| 5159 | NPAD | N_{PAD} | Pitch aerodynamic disturbing normal force per radian angle of attack (lb) |
| 5160 | NPDA | N_{PDA} | Total pitch disturbing normal force per radian angle of attack (lb) |
| 5161 | NNVA | N_{NVA} | Force normal to velocity vector per radian angle of attack (lb) |
| 5162 | NPCD | N_{PCD} | Total pitch control normal force per radian deflection angle (lb) |
| 5163 | NPEA | N_{PEA} | Pitch trim normal force per radian angle of attack (lb) |
| 5164 | C | C | Instantaneous aerodynamic axial force (dbi) |
| 5165 | NY | N_Y | Instantaneous yaw aerodynamic axial normal forces directed opposite to the direction of the Y_b axis |
| 5166 | NZ | N_Z | Instantaneous pitch aerodynamic normal forces directed opposite to the direction of the Z_b -axes (lb) |
| 5167 | NPY | N_{PY} | Aerodynamic force due to damping in yaw (lb) |

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|---|
| 5168 | NPZ | N_{PZ} | Aerodynamic force due to damping and pitch (lb) |
| 5169 | ETABA | η_{ba} | Acceleration load factor along velocity vector (g's) |
| 5170 | ETABT | η_{bt} | Acceleration load factor transverse to the velocity vector (g's) |
| 5171 | ETABN | η_{bn} | Acceleration load factor normal to the velocity vector (g's) |
| 5172-5174 | | | Open |
| 5175 | IXX | I_{XX} | Roll moment of inertia about vehicle center-of-gravity (ft-lb-sec ²) |
| 5176 | IXY | I_{XY} | Roll-yaw product of inertia about vehicle center-of-gravity (ft-lb-sec ²) |
| 5177 | IXZ | I_{XZ} | Roll-pitch product of inertia about vehicle center-of-gravity (ft-lb-sec ²) |
| 5178 | | | Open |
| 5179 | IYY | I_{YY} | Pitch moment of inertia about vehicle center-of-gravity (ft-lb-sec ²) |
| 5180 | IYZ | I_{YZ} | Yaw-pitch product of inertia about vehicle center-of-gravity (ft-lb-sec ²) |
| 5181-5182 | | | Open |
| 5183 | IZZ | I_{ZZ} | Yaw moment of inertia about vehicle center-of-gravity (ft-lb-sec ²) |
| 5184 | IDXX | \dot{I}_{XX} | Time rate change of roll moment of inertia (ft-lb-sec) |
| 5185 | IDXY | \dot{I}_{XY} | Time rate change of roll-yaw product of inertia (ft-lb-sec) |
| 5186 | IDXZ | \dot{I}_{XZ} | Time rate change of roll-pitch product of inertia (ft-lb-sec) |
| 5187 | | | Open |
| 5188 | IDYY | \dot{I}_{YY} | Time rate change of pitch moment of inertia (ft-lb-sec) |
| 5189 | IDYZ | \dot{I}_{YZ} | Time rate change of yaw-pitch product of inertia (ft-lb-sec) |
| 5190-5191 | | | Open |

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|---|
| 5192 | IDZZ | \dot{I}_{ZZ} | Time rate change of yaw moment of inertia (ft-lb-sec) |
| 193 | IPRD | I_{PRD} | Pitch inertia rotation damping moment integral (ft-lb-sec) |
| 5194 | IYRD | I_{YRD} | Yaw inertia rotation damping moment integral (ft-lb-sec) |
| 5195 | IRRD | I_{RRD} | Roll inertia rotation damping moment integral (ft/sec) |
| 5196-5201 | | | Open |
| 5202 | MIQ | M_{IQ} | Unbalanced pitching moment about vehicle center-of-gravity (ft-lb) |
| 5203 | MIR | M_{IR} | Unbalanced yaw moment about vehicle center-of-gravity (ft-lb) |
| 5204 | MIP | M_{IP} | Unbalanced roll moment about vehicle center-of-gravity (ft-lb) |
| 5205 | MDQ | M_{DQ} | Perturbing moment about vehicle center-of-gravity in pitch (ft-lb) |
| 5206 | MDR | M_{DR} | Perturbing moment about vehicle center-of-gravity in yaw (ft-lb) |
| 5207 | MDP | M_{DP} | Perturbing moment about vehicle center-of-gravity in roll (ft-lb) |
| 5208 | MCQ | M_{CQ} | Controlling moment about vehicle center-of-gravity in pitch (ft-lb) |
| 5209 | MCR | M_{CR} | Controlling moment about vehicle center-of-gravity in yaw (ft-lb) |
| 5210 | MCP | M_{CP} | Controlling moment about vehicle center-of-gravity in roll (ft-lb) |
| 5211 | MNQ | M_{NQ} | Aerodynamic yawing moment about vehicle center-of-gravity (ft-lb) |
| 5212 | MNR | M_{NR} | Aerodynamic yawing moment about vehicle center-of-gravity (ft-lb) |
| 5213 | MNP | M_{NP} | Aerodynamic rolling moment about vehicle center-of-gravity (ft-lb) |
| 5214 | MFOQ | M_{FOQ} | Thrust offset pitching moment (ft-lb) |
| 5215 | MFOR | M_{FOR} | Thrust offset yawing moment (ft-lb) |
| 5216 | MFCP | M_{FCP} | Thrust offset rolling moment due to pitch and yaw TVC (ft-lb) |

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|---|
| 5217 | MTDQ | M_{TDQ} | Movable nozzle tail-wag-dog moment about vehicle center-of-gravity in pitch (ft-lb) |
| 5218 | MTDR | M_{TDR} | Movable nozzle tail-wag-dog moment about vehicle center-of-gravity in yaw (ft-lb) |
| 5219 | MFVP | M_{FVP} | Rolling moment about vehicle center-of-gravity due to vortexing effect of axial gas flow through the nozzle (ft-lb) |
| 5220 | MJDQ | M_{JDQ} | Jet damping pitching moment (ft-lb) |
| 5221 | MJDR | M_{JDR} | Jet damping yawing moment (ft-lb) |
| 5222 | MRAP | M_{RAP} | Aerodynamic rolling moment induced by raceways (ft-lb) |
| 5223 | MFCQ | M_{FCQ} | Thrust vector control pitching moment (ft-lb) |
| 5224 | MFCR | M_{FCR} | Thrust vector control yawing moment (ft-lb) |
| 5225 | MFCP | M_{FCP} | Auxiliary roll thrust control moment (ft-lb) |
| 5226 | MDELQ | $M_{\delta Q}$ | Pitching moment due to the aerodynamic control force (ft-lb) |
| 5227 | MDELR | $M_{\delta R}$ | Yawing moment due to the aerodynamic control force (ft-lb) |
| 5228 | MDELP | $M_{\delta P}$ | Rolling moment due to the aerodynamic control force (ft-lb) |
| 5229 | MCYQ | M_{CYQ} | Aerodynamic axial force center-of-gravity offset yawing moment (ft-lb) |
| 5230 | MCZG | M_{CZG} | Aerodynamic axial force center-of-gravity offset pitching moment (ft-lb) |
| 5231 | MPTC | M_{PTC} | Pitch total thrust control moment per radian TVC deflection angle (ft-lb) |
| 5332 | MNSQ | M_{NSQ} | Aerodynamic static pitching moment about vehicle center-of-gravity (ft-lb) |
| 5233 | MNSR | M_{NSR} | Aerodynamic static yawing moment about vehicle center-of-gravity (ft-lb) |
| 5234 | MPMC | M_{PMC} | Pitch main thrust control moment per radial TVC deflection angle (ft-lb) |
| 5235 | MNDQ | M_{NDQ} | Aerodynamic damping moment about vehicle center-of-gravity in pitch (ft-lb) |

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|--|
| 5236 | MNDR | M_{NDR} | Aerodynamic damping moment about vehicle center-of-gravity in yaw (ft-lb) |
| 5237 | | | Open |
| 5238 | MPRR | M_{PRR} | Pitch inertial rotation reaction moment used in the automatic gain logic (ft-lb) |
| 5239 | MYRR | M_{YRR} | Yaw inertial rotation reaction moment used in the automatic altitude gain logic (ft-lb) |
| 5240 | MRRR | M_{RRR} | Roll Rotation reaction moment used in the automatic gain logic (ft-lb) |
| 5241 | MPAC | M_{FAC} | Pitch aerodynamic control moment per radian angle of attack (ft-lb) |
| 5242 | MYAC | M_{YAC} | Yaw aerodynamic control moment per radian angle of side slip (ft-lb) |
| 5243 | MARC | M_{RAC} | Roll aerodynamic control moment per radian fin deflection angle (ft-lb) |
| 5244 | MPAD | M_{PAD} | Pitch aerodynamic disturbing moment per radian angle of attack (ft-lb) |
| 5245 | MYAD | M_{YAD} | Yaw aerodynamic disturbing moment per radian angle of side slip (ft-lb) |
| 5246 | MRAD | M_{RAD} | Open |
| 5247 | MHY | M_{Hy} | Torque about the yaw fin hinge axis (ft-lb) |
| 5248 | MHZ | M_{Hz} | Torque about the pitch fin hinge axis (ft-lb) |
| 5249 | | | Open |
| 5250 | MPDA | M_{PDA} | Total pitch disturbing moment per radian angle of attack (ft-lb) |
| 5251 | MPCD | M_{PCD} | Total pitch control moment per radian deflection angle (ft-lb) |
| 5252-5300 | | | Open |
| 5301 | ALPHA | α | Instantaneous pitch angle of attack. Positive if the vehicle centerline is above the air velocity vector (deg) |
| 5302 | ALPHAD | $\dot{\alpha}$ | Time rate change of angle of attack (deg/sec) |
| 5303 | ALPHAC | α_c | Command angle of attack (deg) |

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|---|
| 5304 | ALPPE | α'_E | Effective total angle of attack used to compute the aerodynamic normal force (deg) |
| 5305 | ALBAR | $\bar{\alpha}'$ | Still air total angle of attack (deg) |
| 5306 | | | Open |
| 5307 | ALPHBD | $\dot{\alpha}$ | Time rate change of still wind angle of attack (deg/sec) |
| 5308 | BETABD | $\dot{\beta}$ | Time rate change of still wind angle of side slip (deg/sec) |
| 5309 | APHRIM | α' | Total vehicle angle of attack. Angle between the centerline of the vehicle and the missile air velocity vector. Always positive (deg) |
| 5310 | ALBAR | $\bar{\alpha}$ | Still wind angle of attack (deg) |
| 5311 | ALPHAE | α_E | Effective pitch angle of attack used to compute the aerodynamic normal force (deg) |
| 5312 | ALPHAM | α_m | Commanded angle of attack for constant angle of attack flight (Ty-2) (deg) |
| 5313-5314 | | | Open |
| 5315 | BETA | β | Angle of side slip. Positive if the vehicle centerline is left of the air velocity vector when viewed from the rear of the vehicle (deg) |
| 5316 | BETAD | $\dot{\beta}$ | Time rate change of angle of side slip (deg/sec) |
| 5317 | BETAC | β_c | Commanded angle of side slip (deg) |
| 5318 | BETBAR | $\bar{\beta}$ | Still wind angle of side slip |
| 5319 | BTPBAR | $\bar{\beta}'$ | Still wind angle of side slip in the commanded coordinate system used to evaluate the local bank angle |
| 5320 | BETAE | β_E | Effective yaw angle of side slip used to compute the aerodynamic normal force (deg) |
| 5321 | GAM1 | γ_1 | Pitch flight path angle. Angle between the earth referenced velocity vector and the local tangent plane. Positive away from the earth (deg) |
| 5322 | GAMD1 | $\dot{\gamma}_1$ | Pitch flight path angular rate. Positive up (deg/sec) |

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|--|
| 5323 | GAM2 | γ_2 | Azimuthal flight path angle. Angle between the horizontal projection of the earth reference velocity vector and the local north. Positive clockwise from north (deg) |
| 5324 | GAMD2 | $\dot{\gamma}_2$ | Azimuthal flight path angular rate (deg/sec) |
| 5325 | | | Open |
| 5326 | GAM2IA | γ_{2Ia} | Inertial azimuth flight path angle at apogee (deg) |
| 5327 | GAM1E | γ_{1E} | Pitch flight path angle with respect to the ambient air at entry conditions (deg) |
| 5328 | GAM1IE | γ_{1IE} | Entry conditions inertial pitch flight path angles, if powered flight and the atmospheric end at the time being printed (deg) |
| 5329 | GAM2IE | γ_{2IE} | Entry conditions inertial yaw flight path azimuth angle, if powered flight and the atmosphere end at the time being printed (deg) |
| 5330 | GAM1I | γ_{1I} | Inertial pitch flight path angle. Angle between the inertial velocity vector and the local tangent plane. Positive away from the earth (deg) |
| 5331 | GAM2I | γ_{2I} | Inertial azimuth flight path angle. Angle between local north clockwise to the projection of the inertial velocity vector on the local tangent plane (deg) |
| 5332 | GAM1IF | γ_{1If} | Impact or intercept inertial pitch flight path angle, if powered flight and the atmosphere end at the time being printed (deg) |
| 5333 | GAM2IF | γ_{2If} | Impact or intercept inertial yaw flight path azimuthal angle, if powered flight and the atmosphere end at the time being printed (deg) |
| 5334 | GAMMAR | γ_R | Output required velocity flight path angle at the missile instantaneous position (deg) |
| 5335 | GAMMAE | γ_G | Calculated local angle of velocity to be gained (deg) |
| 5336 | GAMM | γ_M | Relative azimuthal velocity vector angle in missile-target coordinates |
| 5337 | GAMDM | $\dot{\gamma}_M$ | Relative azimuthal velocity vector angular rate in missile-target coordinates |

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|---|
| 5338 | DELM I | δ_{MI} | Azimuth flight path error to intercept. Used in type 10 flight (deg) |
| 5339 | DELPC | δ_{Pc} | Pitch plane thrust deflection commands (deg) |
| 5340 | DELYC | δ_{Yc} | Yaw plane thrust deflection commands (deg) |
| 5341 | DELRC | δ_{Rc} | Commanded roll control fin deflection angle (deg) |
| 5342 | DELBRP | $\bar{\delta}_p$ | Modified pitch thrust deflection angle to include limit cycle and misalignment angle (deg) |
| 5343 | DELBRY | $\bar{\delta}_y$ | Modified yaw thrust deflection angle to include limit cycle and misalignment angles (deg) |
| 5344 | DELTHB | $\Delta\theta_b$ | Vehicle pitch attitude error angle (deg) |
| 5345 | DELPSB | $\Delta\psi_b$ | Vehicle yaw attitude error angle (deg) |
| 5346 | DELPHB | $\Delta\phi_b$ | Vehicle roll attitude error angle (deg) |
| 5347 | DELAK | Δ'_{ak} | Pitch flare in constant used in evaluation Δ'_{ak} for restart (deg) |
| 5348 | DELBK | Δ_{bk} | Flare-in constant used in evaluating Δ'_{bk} for restart (deg) |
| 5349 | DELAP | Δ'_a | Pitch flare-in angle (deg) |
| 5350 | DELB P | Δ'_b | Yaw flare-in angle (deg) |
| 5351 | DELM T | δ_{MT} | Seeker yaw look angle (deg) |
| 5352 | DELDMT | $\dot{\delta}_{MT}$ | Seeker yaw look angular rate (deg/sec) |
| 5353 | EPSILN | ϵ | Total angle of attack roll orientation angle. Angle between total angle of attack plane and yaw axis. Measured counterclockwise (deg) |
| 5354 | EPSBAR | $\bar{\epsilon}$ | No-wind total angle of attack roll orientation angle (deg) |
| 5355 | EPSMI | ϵ_{MI} | Flight path error to estimated intercept (deg) |
| 5356 | EPSMT | ϵ_{MT} | Seeker pitch look angle (deg) |
| 5357 | EPSDMT | $\dot{\epsilon}_{MT}$ | Seeker pitch look angular rate (deg/sec) |

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|--|
| 5358 | ZETA | ζ | Cross range angle. Angle between local vertical and vertical on firing azimuth down range location. Positive if positive is left of firing azimuth (deg) |
| 5359 | ZETAD | $\dot{\zeta}$ | Cross range angular rate (deg/sec) |
| 5360 | LAMMT | λ_{MT} | Angle of missile to target line projection on horizontal and firing azimuth (deg) |
| 5361 | LAMDMT | $\dot{\lambda}_{MT}$ | Angular rate of missile to target line projection on horizontal and firing azimuth (deg/sec) |
| 5362 | MU | μ | Instantaneous vehicle longitude. Value is positive or negative west or east of Greenwich, England, respectively (deg) |
| 5363 | MUP | μ' | Instantaneous vehicle change of longitude from launch longitude. Value is positive east (deg) |
| 5364 | MUPD | $\dot{\mu}'$ | Vehicle longitude time rate change (deg/sec) |
| 5365 | MUA | μ_a | Vehicle apogee longitude if powered flight and the atmosphere end at the time being printed (deg) |
| 5366 | MUF | μ_f | Missile impact or intercept longitude if powered flight and the atmosphere end at the time being printed (deg) |
| 5367 | RHO | ρ | Instantaneous vehicle latitude positive north of the equator $-90^\circ \leq \rho \leq 90^\circ$ |
| 5368 | RHOD | $\dot{\rho}$ | Vehicle latitude time rate change (deg/sec) |
| 5369 | RHOA | ρ_a | Vehicle apogee latitude if powered flight and the atmosphere end at the time being printed (deg) |
| 5370 | RHOF | ρ_f | Missile impact or intercept latitude if powered flight and the atmosphere end at the time being printed (deg) |
| 5371 | SIGMT | α_{MT} | Angle of missile to target line and local horizontal (deg) |
| 5372 | SIGDMT | $\dot{\alpha}_{MT}$ | Angular rate of missile to target line and local horizontal |
| 5373 | SIGMI | α_{MI} | Local flight path angle to estimated target, intercept (deg) |

| <u>L-number</u> | <u>FORTAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------|--------------------------|---|
| 5374 | UPSMI | τ_{MI} | Azimuthal angle to target intercept (deg) |
| 5375 | PHI | ϕ | Instantaneous down range angle. Angle between the launch vertical and the local vertical on the down range azimuth point. Positive as shown in Figure 1.1, $-\infty < \phi < \infty$ (deg) |
| 5376 | PHID | $\dot{\phi}$ | Instantaneous range angular rate. Positive down range (deg/sec) |
| 5377 | | | Open |
| 5378 | PHIA | ϕ_a | Glide range angle to the apogee vertical (deg) |
| 5379 | PHIS | ϕ_s | Instantaneous slant range angle. Angle between the launch vertical and the local vertical (deg) |
| 5380 | SCRPHI | ϕ | Local bank angle (deg) |
| 5381 | PHIF | ϕ_f | Glide range angle to glide phase termination vertical used in Keplerian impact predictions (deg) |
| 5382 | PSI | ψ | Vehicle azimuth in the launch horizontal plane (deg) |
| 5383 | PSIW | ψ_w | Instantaneous wind azimuth angles, measured in a plane parallel to the local tangent plane where $j = 1, 2, \dots, 30$. Angle measured clockwise from north to the direction from which the wind is coming (deg) |
| 5384-5400 | | | Open |
| 5401 | QM | Q_m | Instantaneous desired pitch turning rate (deg/sec) |
| 5402 | RM | R_m | Instantaneous desired yaw turning rate (deg/sec) |
| 5403 | PM | P_m | Instantaneous desired roll turning rate (deg/sec) |
| 5404-5430 | | | Open |
| 5431 | DELS | Δ_s | Calculated earth surface down range difference of the target and missile (ft) |
| 5432 | DELSJ | $\dot{\Delta}_s$ | Calculated time rate change of the earth surface down range difference of the target and missile (ft/sec) |

| <u>L-number</u> | <u>FORTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|-----------------------|--------------------------|--|
| 5433 | DELSC | ΔS_c | Calculated earth surface cross range difference of the target and missile (ft) |
| 5434 | DELSDC | $\dot{\Delta S}_c$ | Calculated time rate change of the earth surface cross range difference of the target and missile (ft/sec) |
| 5435 | DELH | Δh | Calculated altitude difference of the target and missile (ft) |
| 5436 | DELHD | $\dot{\Delta h}$ | Calculated time rate change of the altitude difference of the target and missile (ft/sec) |
| 5437 | RMT | R_{MT} | Missile to target range distance (ft) |
| 5438 | RMT | \dot{R}_{MT} | Time rate change of missile to target distance (ft/sec) |
| 5439 | TMI | t_{MI} | Estimated time to intercept (ft) |
| 5440 | RMI | R_{MI} | Estimated range to target intercept (ft) |
| 5441 | SMI | S_{MI} | Estimated earth surface down range at target intercept (ft) |
| 5442 | HMI | h_{MI} | Estimated altitude at target intercept (ft) |
| 5443 | SCMI | S_{CMI} | Estimated earth surface cross range at target intercept (ft) |
| 5444 | ATT | a_{TT} | Target tangential acceleration (g's) |
| 5445 | ATN | a_{TN} | Target normal to its velocity vector acceleration (g's) |
| 5446 | ATC | a_{TC} | Target transverse acceleration (g's) |
| 5447-5448 | | | Open |
| 5449 | FD | F_D | Instantaneous roll control system phase plane signal (deg) |
| 5450 | KS | K_S | Pressure error gain used in pintle area control law in the TMC (in ² /lb-sec) |
| 5451 | KP | K_P | Pressure rate gain used in pintle area control law in the TMC (sec) |
| 5452 | KCV | K_{cv} | Commanded thrust velocity error gain used in TMC (lb-sec/ft) |
| 5453 | KCQ | K_{CQ} | Commanded thrust dynamic pressure error gain used in TMC (ft ²) |

| <u>L-number</u> | <u>FORTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|---------------------------|------------------------------|--|
| 5454 | KXXX | K_{XXX} | Commanded thrust system gain. Set equal to K_{CPR} if $Fy=3$ and K_{ALOS} if $Fy=6$ (dim) |
| 5455 | GZ | G_Z | Partial derivatives of altitude acceleration to vehicle altitude (ft/sec ² -deg) |
| 5456 | KZ | K_Z | Altitude error gain used in type 3 flight (deg/ft) |
| 5457 | KZD | $K_{\dot{Z}}$ | Altitude rate gain used in type 8 flight (deg-sec/ft) |
| 5458 | KZDD | $K_{\ddot{Z}}$ | Altitude acceleration gain used in type 8 flight (deg-sec ² /ft) |
| 5459 | KTHDD | $K_{\ddot{\theta}_9}$ | Command attitude pitch attitude angular acceleration gain used in type of flight 8 and 9 (sec ²) |
| 5460 | KPSDD | $K_{\ddot{\psi}}$ | Command attitude, yaw attitude angular acceleration gain used in type of flight 8 and 9 (sec ²) |
| 5461 | KDP | K_{DP} | Instantaneous control system pitch attitude error gain (dim) |
| 5462 | KDY | K_{DY} | Instantaneous control system yaw attitude error gain (dim) |
| 5463 | KDR | K_{DR} | Instantaneous control system roll attitude error gain (dim) |
| 5464 | KIP | K_{IP} | Instantaneous control system angle of attack gain (dim) |
| 5465 | KIY | K_{IY} | Instantaneous control system angle of side slip gain (dim) |
| 5466 | KIR | K_{IR} | Roll control attitude bias gain (1/sec) |
| 5467 | KRP | K_{RP} | Instantaneous control system pitch rate gain (sec) |
| 5468 | KRY | K_{RY} | Instantaneous control system yaw rate gain (sec) |
| 5469 | KRR | K_{RR} | Instantaneous control system roll rate gain (sec) |
| 5470-5490 | | | (open) |

| <u>L-number</u> | <u>FORTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|---------------------------|------------------------------|--|
| 5491 | MAXVAL(1) | σ_{mx1} | Values which are designated by input, as quantity whose maximum value is to be printed following each stage time (dbi) |
| 5492 | MAXVAL(2) | σ_{mx2} | |
| 5493 | MAXVAL(3) | σ_{mx3} | |
| 5494 | MAXVAL(4) | σ_{mx4} | |
| 5495 | MAXVAL(5) | σ_{mx5} | |
| 5496 | STGVAL(1) | σ_{BX1} | Values which are designated by input, at staging which are available to the hunting procedure (dbi) |
| 5497 | STGVAL(2) | σ_{BX2} | |
| 5498 | STGVAL(3) | σ_{BX3} | |
| 5499 | STGVAL(4) | σ_{BX4} | |
| 5500 | STGVAL(5) | σ_{BX5} | |
| 5501-5503 | | | Open |
| 5504 | AXB | a_{xb} | Component of vehicle acceleration due to total thrust and aerodynamic forces. Positive in the direction of the coordinate axes of b system (g's) |
| 5505 | AYB | a_{yb} | Component of vehicle acceleration due to total thrust and aerodynamic forces. Positive in the direction of the coordinate Y axes of the b system (g's) |
| 5506 | AZB | a_{zb} | Components of vehicle acceleration due to total thrust and aerodynamic forces. Positive in direction of the coordinate Z axes of b system (g's) |
| 5507 | XDABB | \dot{x}_{abb} | X component of missile velocity with respect to the ambient air in the b system (ft/sec) |
| 5508 | YDABB | \dot{y}_{abb} | Y component of the missile velocity with respect to the ambient air in the b system (ft/sec) |
| 5509 | ZDABB | \dot{z}_{abb} | z component of missile velocity with respect to the ambient air in the b system (ft/sec) |
| 5510 | XDDZBB | \ddot{x}_{abb} | x component of missile acceleration with respect to ambient air in the b system (ft/sec ²) |
| 5511 | YDABB | \ddot{y}_{abb} | y component of missile acceleration with respect to the ambient air in the b system (ft/sec ²) |
| 5512 | ZDDABB | \ddot{z}_{abb} | z component of missile acceleration with respect to the ambient air in the b system (ft/sec ²) |
| 5513 | XCC | X_{cc} | Earth centered missile position northern axis component (ft) |
| 5514 | YCC | Y_{cc} | Earth centered missile position east from launcher (ft) |

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|--|
| 5515 | ZCC | Z_{cc} | Earth centered missile position away from earth axis at launcher longitude (ft) |
| 5516 | XDCC | \dot{X}_{cc} | Northern component of missile velocity in earth centered coordinates (ft/sec) |
| 5517 | YDCC | \dot{Y}_{cc} | East from launcher component of missile velocity in earth centered coordinate (ft/sec) |
| 5518 | ZDCC | \dot{Z}_{cc} | Away from launcher longitude component of missile velocity in earth centered coordinates (ft/sec) |
| 5519 | XDDCC | \ddot{X}_{cc} | Northern component of missile acceleration in earth centered coordinates (ft/sec ²) |
| 5520 | YDDCC | \ddot{Y}_{cc} | East from launcher component of missile acceleration in earth centered coordinates (ft/sec ²) |
| 5521 | ZDDCC | \ddot{Z}_{cc} | Away from launcher longitude component of missile acceleration in earth centered coordinates (ft/sec ²) |
| 5522 | XGG | X_{gg} | Instantaneous component of vehicle position in the generalized coordinates down range from launcher (ft) |
| 5523 | YGG | Y_{gg} | Instantaneous component of vehicle position in the generalized coordinates cross range from launcher (ft) |
| 5524 | ZGG | Z_{gg} | Instantaneous component of vehicle positive vertical from launcher (ft) |
| 5525 | XDGG | \dot{X}_{gg} | Instantaneous component of vehicle velocity in the generalized coordinates down range from launcher (ft/sec) |
| 5526 | YDGG | \dot{Y}_{gg} | Instantaneous component of vehicle velocity in the generalized coordinates crosswise from launcher (ft/sec) |
| 5527 | ZDGG | \dot{Z}_{gg} | Instantaneous component of vehicle velocity in the generalized coordinates vertical from launcher (ft/sec) |
| 5528 | XDDGG | \ddot{X}_{gg} | Instantaneous component of vehicle acceleration in the generalized coordinates down range from launcher (ft/sec ²) |
| 5529 | YDDGG | \ddot{Y}_{gg} | Instantaneous component of vehicle acceleration in the generalized coordinates crosswise from launcher (ft/sec ²) |

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|--|
| 5530 | ZDDGG | \ddot{z}_{gs} | Instantaneous component of vehicle acceleration in the generalized coordinates vertical from launcher (ft/sec ²) |
| 5531 | XDW11 | \dot{x}_{w11} | Local northerly component of wind velocity (ft/sec) |
| 5532 | YDW11 | \dot{y}_{w11} | Local easterly component of wind velocity (ft/sec) |
| 5533 | ZDW11 | \dot{z}_{w11} | Local downward component of wind velocity (ft/sec) |
| 5534 | XDDW11 | \ddot{x}_{w11} | Local time rate change of northern component of wind velocity (ft/sec ²) |
| 5535 | YDDW11 | \ddot{y}_{w11} | Local time rate change of easterly component of wind velocity (ft/sec ²) |
| 5536 | ZDDW11 | \ddot{z}_{w11} | Local time rate change of downward component of wind velocity (ft/sec ²) |
| 5537 | XDBB | \dot{x}_{bb} | Inertial component of missile velocity along x_b axis (ft/sec) |
| 5538 | YBB | \dot{y}_{bb} | Inertial component of missile velocity along y_b axis (ft/sec) |
| 5539 | ZDBB | \dot{z}_{bb} | Inertial component of missile velocity along z_b axis (ft/sec) |
| 5540 | XDDBB | \ddot{x}_b | Missile acceleration along vehicle body axis, position forward (ft/sec ²) |
| 5541 | YDDBB | \ddot{y}_b | Inertial component of missile acceleration y_b axes (ft/sec ²) |
| 5542 | ZDDBB | \ddot{z}_b | Inertial components of missile acceleration along z_b axis (ft/sec ²) |
| 5543 | XD11 | \dot{x}_{11} | Local northerly component of missile velocity (ft/sec) |
| 5544 | YD11 | \dot{y}_{11} | Local easterly component of missile velocity (ft/sec) |
| 5545 | ZD11 | \dot{z}_{11} | Local downward component of missile velocity (ft/sec) |
| 5546 | XDD11 | \ddot{x}_{11} | Local northerly component of missile acceleration (ft/sec ²) |
| 5547 | YDD11 | \ddot{y}_{11} | Local easterly component of missile acceleration (ft/sec ²) |

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|--|
| 5548 | ZDD11 | \ddot{z}_{11} | Local downward component of missile acceleration (ft/sec ²) |
| 5549 | XDWEE | \dot{x}_{wee} | Transformed launcher northeaznly component of wind velocity at missile location (ft/sec) |
| 5550 | YDWEE | \dot{y}_{wee} | Transformed launcher easternly component of wind velocity at missile location (ft/sec) |
| 5551 | ZDWEE | \dot{z}_{wee} | Transformed launcher downward component of wind velocity at missile location (ft/sec) |
| 5552 | XD11I | \dot{x}_{11I} | Local northernly component of missile inertial velocity (ft/sec) |
| 5553 | YD11I | \dot{y}_{11I} | Local easternly component of missile inertial velocity (ft/sec) |
| 5554 | ZD11I | \dot{z}_{11I} | Local downward component of missile inertial velocity (ft/sec) |
| 5555-5563 | | | Open |
| 5564 | CLZ | C_{Lz} | Instantaneous aerodynamic pitch movable fins linear fin lift coefficient (1/deg ²) |
| 5565 | CLZ | C_{lz} | Instantaneous aerodynamic pitch movable fin nonlinear fin lift coefficient (1/deg ²) |
| 5566 | CDZ | C_{Dz} | Instantaneous aerodynamic pitch movable fin drag coefficient (dim) |
| 5567 | KLZ | K_{Lz} | Instantaneous aerodynamic pitch movable fin drag due to lift factor (dim) |
| 5568 | UCZ | U_{cz} | Pitch aerodynamic control fin center of pressure ratio relative to the root chord (dim) |
| 5569 | CN | C_N | Instantaneous aerodynamic normal force coefficient (dim) |
| 5570 | CN1 | C_{N1} | Instantaneous first, second, and third derivatives, respectively, of C_N with respect to the angle of attack, (/deg, /deg ² , /deg ³ , respectively) |
| 5571 | CN2 | C_{N2} | |
| 5572 | CN3 | C_{N3} | |
| 5573 | CA | C_A | Instantaneous aerodynamic axial force coefficient |
| 5574 | CBN | C_{BN} | Added aerodynamic base drag coefficient due to nozzles not thrusting (dim) |

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|---|
| 5575 | CMQ | C_{MQ} | Calculated and unadjusted for translation aerodynamic pitch damping moment due to pitch rate coefficient (1/deg) |
| 5576 | CMAD | $C_{M\dot{\alpha}}$ | Calculated and unadjusted for translation aerodynamic pitch damping moment due to rate change of angle of attack coefficient (/deg) |
| 5577 | CHLY | \hat{C}_{Ly} | Instantaneous aerodynamic yaw movable fin total lift coefficient (dim) |
| 5578 | CHLZ | \hat{C}_{Lz} | Instantaneous aerodynamic pitch movable fin total lift coefficient (dim) |
| 5579 | CHDZ | \hat{C}_{Dz} | Instantaneous aerodynamic pitch movable fin total drag coefficient (dim) |
| 5580-5582 | | | Open |
| 5583 | XCP | x_{cp} | Input and instantaneous (with Mach number M) aerodynamic normal force center of pressure body station numbers, respectively, where $j = 1, 2, \dots, 15$ per stage (ft and dbi, respectively) |
| 5584 | XCG | x_{cg} | Instantaneous center of gravity body station numbers (ft) |
| 5585 | YCG | y_{cg} | Center of gravity offset bias distance positive in the Z_b direction (ft) |
| 5586 | ZCG | z_{cg} | Center of gravity offset bias distance positive down (dbi) |
| 5587 | XPF | x_{pf} | Computed stage forward end of propellant grain body station (ft) |
| 5588 | XPA | x_{Pa} | Computed stage aft end propellant grain body station (ft) |
| 5589 | YE | y_e | Thrust gimbal yaw point eccentricity position in the Y_b axis direction (ft) |
| 5590 | ZE | z_e | Thrust gimbal pitch point position in the Z_b axis direction (ft) |
| 5591-5592 | | | Open |
| 5593 | LE | l_e | Gimbal point to vehicle center of gravity distance (ft) |

| <u>L-number</u> | <u>FORTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|---------------------------|------------------------------|--|
| 5594 | LSE | l_E | Nozzle exit to center of gravity distance (ft) |
| 5595 | LN | l_n | Movable portion of the nozzle center of gravity to gimbal point distance (ft) |
| 5596 | LCP | l_{cp} | Vehicle center of gravity to aerodynamic center of pressure distance (ft) |
| 5597 | LNN | l_N | Vehicle center of gravity to stop-start motor thrust point distance (ft) |
| 5598 | LPF | l_{Pf} | Forward end of propellant grain to center of gravity distance (ft) |
| 5599 | LPA | l_{Pa} | Aft end of propellant grain to center of gravity distance (ft) |
| 5600 | LDELY | $l_{\delta y}$ | Yaw movable control fin center of pressure to vehicle center of gravity lever arm (ft) |
| 5601 | LDELZ | $l_{\delta z}$ | Pitch movable control fin center of pressure to vehicle center of gravity lever arm (ft) |
| 5602 | LHZ | l_{hz} | Pitch movable control fin center of pressure to hinge axis lever arm (ft) |
| 5603-5700 | | | Open |
| 5701 | XDEE | \dot{x}_{ee} | Instantaneous components of vehicle velocity, north of the launcher (ft/sec) |
| 5703 | YDEE | \dot{y}_{ee} | Instantaneous components of vehicle velocity, east of the launcher (ft/sec) |
| 5703 | ZDEE | \dot{z}_{ee} | Instantaneous component of vehicle velocity, negative up from sea level launcher latitude (ft/sec) |
| 5704 | XEE | x_{ee} | Instantaneous component of vehicle position north of launcher (ft) |
| 5705 | YEE | y_{ee} | Instantaneous component of vehicle position east of launcher (ft) |
| 5706 | ZEE | z_{ee} | Instantaneous component of vehicle position negative up from sea level launcher latitude (ft) |
| 5707 | QB | Q_b | Instantaneous vehicle angular pitch velocity. Pitch up is positive (deg/sec) |
| 5708 | RB | R_b | Instantaneous vehicle angular yaw velocity. Yaw right is positive (deg/sec) |

| <u>L-number</u> | <u>FORTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|---------------------------|------------------------------|--|
| 5709 | PB | P_b | Instantaneous vehicle angular roll velocity. Roll Clockwise is positive (deg/sec) |
| 5710 | THETAB | θ_b | Achieved missile Euler angle pitch attitude (deg) |
| 5711 | PSIB | ψ_b | Achieved missile Euler angle yaw attitude (deg) |
| 5712 | PHIB | ϕ_b | Achieved missile Euler angle roll attitude (deg) |
| 5713 | DELDF | $\dot{\delta}_p$ | Pitch thrust deflection angular rate positive up (deg/sec) |
| 5714 | DELDY | $\dot{\delta}_y$ | Yaw thrust deflection angular rate, positive left (deg/sec) |
| 5715 | DELDR | $\dot{\delta}_R$ | Aerodynamic roll fins deflection angular rate (deg/sec) |
| 5716 | DELP | δ_p | Pitch thrust deflection angle. Positive up (deg) |
| 5717 | DELY | δ_y | Yaw thrust deflection angle. Positive left (deg) |
| 5718 | DELR | δ_R | Aerodynamic roll fins deflection angle (deg) |
| 5719 | FR | F_R | Instantaneous roll control thrust. Positive if the vehicle is intended to rotate clockwise as seen from the rear of the vehicle (lb) |
| 5720 | WR | W_R | Instantaneous expended weight due to roll control motor operation (lb) |
| 5721 | FRC | F_{Rc} | Instantaneous roll control system thrust command signal (lb) |
| 5722 | THETAM | θ_m | Desired missile attitude Euler angle relating the m and i system (deg) |
| 5723 | PSIM | ψ_m | Desired missile attitude Euler angle relating the m and i systems (deg) |
| 5724 | PHIM | ϕ_m | Desired missile attitude Euler angle relating the m and i systems (deg) |
| 5725 | VT | V_T | Target tangential velocity (ft/sec) |
| 5726 | VN | V_N | Target normal velocity (ft/sec) |
| 5727 | VC | V_C | Target transverse velocity (ft/sec) |

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|---|
| 5728 | GAMT | γ_T | Target pitch flight path angle (deg) |
| 5729 | ZETAT | ζ_T | Target azimuthal flight path angle (deg) |
| 5730 | HT | h_T | Target altitude (ft) |
| 5731 | ST | S_T | Target down range (ft) |
| 5732 | 3TC | S_{IC} | Target cross range (ft) |
| 5733 | DB | D_b | Propellant burn depth. Used in TMC logic (in) |
| 5734 | PC | P_c | Main motor chamber pressure used in separated flow equation (lb/in ²) |
| 5735 | AT | A_t | Pintle nozzle throat area. Used in TMC logic (in ²) |
| 5736 | WPR | W_{pr} | Weight of propellant removed. Used in TMC logic (lb) |
| 5737 | IMP | I | Total missile impulse and vacuum impulse, respectively, measured from stage initiation to the time being printed (lb-sec) |
| 5738 | IV | I_V | |
| 5739 | IP | I_P | Pitch control thrust impulse from stage initiation to the time being printed (lb-sec) |
| 5740 | IY | I_Y | Yaw control thrust impulse from stage initiation to the time being printed (lb-sec) |
| 5741 | IDELD? | $I_{\delta P}$ | Sum of pitch angular thrust vectoring velocities from stage initiation to the time being printed (deg) |
| 5742 | IDELDY | $I_{\delta Y}$ | Sum of yaw angular thrust vectoring velocities from stage initiation to the time being printed (deg) |
| 5743 | LF | L_F | Output total velocity loss due to back pressure from stage initiation to time being printed (lb-sec) |
| 5744 | DELTAV | Δ_V | Ideal missile velocity resulting from achieved thrust (ft/sec) |
| 5745 | IR | I_R | Auxiliary roll control system delivered total impulse (lb-sec) |
| 5746 | LD | L_D | Drag velocity loss from stage ignition (ft/sec) |
| 5747 | HE | H_e | Heating parameter. Integral of qv from stage initiation to the time being printed (lb/ft) |

| <u>L-number</u> | <u>FORTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|---------------------------|------------------------------|--|
| 5748 | LGG | L_g | Gravity losses, from trajectory initiation to the time being printed (ft/sec) |
| 5749-5750 | | | Open |
| 5751 | XDDEE | \ddot{X}_{ee} | Instantaneous northerly component of vehicle acceleration at launcher (ft/sec ²) |
| 5752 | YDDEE | \ddot{Y}_{ee} | Instantaneous easterly component of vehicle acceleration at launcher (ft/sec ²) |
| 5753 | ZDDEE | \ddot{Z}_{ee} | Instantaneous downward component of vehicle acceleration at launcher (ft/sec ²) |
| 5754-5756 | | | Open |
| 5757 | QDB | \dot{Q}_b | Instantaneous vehicle angular pitch acceleration. Pitch up positive (deg/sec ²) |
| 5758 | RDB | \dot{R}_b | Instantaneous vehicle angular yaw acceleration. Yaw right positive (deg/sec ²) |
| 5759 | PDB | \dot{P}_b | Instantaneous vehicle angular roll acceleration, roll clockwise positive (deg/sec ²) |
| 5760 | THETDB | $\dot{\theta}_b$ | Achieved vehicle Euler angle pitch rate (deg/sec) |
| 5761 | PSIDB | $\dot{\psi}_b$ | Achieved vehicle Euler angle yaw rate (deg/sec) |
| 5762 | PHIDB | $\dot{\phi}_b$ | Achieved vehicle Euler angle roll rate (deg/sec) |
| 5763 | DELDDP | $\ddot{\delta}_p$ | Pitch thrust deflection angular acceleration angle positive up (deg/sec ²) |
| 5764 | DELDDY | $\ddot{\delta}_y$ | Yaw thrust deflection angular acceleration angle positive left (deg/sec ²) |
| 5765-5768 | | | Open |
| 5769 | FDR | \dot{F}_R | Time rate change of roll control thrust (lb/sec) |
| 5770 | WDR | \dot{W}_R | Roll control system mass flow rate (lb/sec) |
| 5771 | | | Open |
| 5772 | THETDM | $\dot{\theta}_m$ | Desired vehicle pitch Euler angular rate (deg/sec) |
| 5773 | PSIDM | $\dot{\psi}_m$ | Desired vehicle yaw Euler angular rate (deg/sec) |
| 5774 | PHIDM | $\dot{\phi}_m$ | Desired vehicle roll Euler angular rate (deg/sec) |

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|--|
| 5775 | VTD | \dot{V}_{Tj} | Target tangential acceleration (ft./sec) |
| 5776 | VND | \dot{V}_{Nj} | Target normal acceleration (ft./sec) |
| 5777 | VCD | \dot{V}_{Cj} | Target transverse acceleration (ft./sec) |
| 5778 | GAMMTD | $\dot{\gamma}_T$ | Target pitch flight path angular rate (deg/sec) |
| 5779 | ZETATD | $\dot{\zeta}_T$ | Target azimuthal path angular rate (deg/sec) |
| 5780 | HTD | \dot{h}_T | Target altitude rate (ft./sec) |
| 5781 | STD | \dot{s}_T | Target down range rate (ft./sec) |
| 5782 | STCD | \dot{s}_{TC} | Target cross range rate (ft./sec) |
| 5783 | RBB | r_b | Propellant burn rate (in. /sec) |

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|--|
| 5784 | PDC | \dot{P}_C | Time rate change of chamber pressure (lb/in ² -sec) |
| 5785 | ADT | \dot{a}_t | Time rate change of pintle throat area (in ² -sec) |
| 5786 | WDMT | \dot{W}_{MT} | Mass flow rate of gases three pintle nozzle throat (lb/sec) |
| 5787-5800 | | | Open |
| 5801-5840 | BLOCK(1)-(40) | | Begin reserved for coding output block (dbi) |
| 5841 | Z(1,1) | $I_{FM}(1)$ | Calculated main table nozzle back pressure impulse for stage I (lb-sec) |
| 5842 | Z(2,1) | $\hat{I}_{VM}(1)$ | Calculated main table input total impulse adjusted to vacuum conditions for stage I (lb-sec) |
| 5843 | Z(3,1) | $I_{VM}(1)$ | Calculated input vacuum corrected main table time adjusted thrust integral for stage I (lb-sec) |
| 5844 | Z(4,1) | $I_{VM}^*(1)$ | Calculated main table vacuum adjusted thrust integral for stage I (lb-sec) |
| 5845 | Z(5,1) | $K_{FM}^*(1)$ | Calculated main table thrust multiplier for stage I (lb-sec) |
| 5846 | Z(6,1) | $I_{spM}(1)$ | Calculated main table adjusted to vacuum specific impulse for stage I (sec) |
| 5847 | Z(7,1) | $I_{TC}(1)$ | Calculated complementary table nozzle back pressure impulse for stage I (lb-sec) |
| 5848 | Z(8,1) | $\hat{I}_{VC}(1)$ | Calculated complementary table input total impulse adjusted to vacuum condition for stage I (lb-sec) |
| 5849 | Z(9,1) | $I_{VC}(1)$ | Calculated input vacuum corrected comple- mentary table time adjusted thrust integral for stage I (lb-sec) |
| 5850 | Z(10,1) | $I_{VC}^*(1)$ | Calculated complementary table vacuum adjusted thrust integral for stage I (lb-sec) |
| 5851 | Z(11,1) | $K_{TC}^*(1)$ | Calculated complementary table thrust multiplier for stage I (dim) |
| 5852 | Z(12,1) | $I_{spC}(1)$ | Calculated complementary table adjusted to vacuum specific impulse for stage I (sec) |

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|---|
| 5853 | Z(13,1) | $\hat{I}_{vT}(1)$ | Calculated input main and complementary impulse corrected to vacuum condition for stage I (lb-sec) |
| 5854 | Z(14,1) | $I_{vT}^*(1)$ | Calculated main and complementary vacuum adjusted thrust integral for Stage I (lb-sec) |
| 5855 | Z(15,1) | $I_{vT}(1)$ | Calculated input vacuum corrected main and complementary impulse corrected for stage I (lb-sec) |
| 5856 | Z(1,2) | $I_{FM}(2)$ | Calculated main table nozzle back pressure impulse for stage II (lb-sec) |
| 5857 | Z(2,2) | $\hat{I}_{vM}(2)$ | Calculated main table input total impulse adjusted to vacuum conditions for stage II (lb-sec) |
| 5358 | Z(3,2) | $I_{vm}(2)$ | Calculated input vacuum corrected main table time adjusted thrust integral for stage II (lb-sec) |
| 5859 | Z(4,2) | $I_{vM}^*(2)$ | Calculated main table vacuum adjusted thrust integral for stage II (lb-sec) |
| 5860 | Z(5,2) | $K_{FM}^*(2)$ | Calculated main table thrust multiplier for stage II (dim) |
| 5861 | Z(6,2) | $I_{spM}(2)$ | Calculated main table adjusted to vacuum specific impulse for stage II (sec) |
| 5862 | Z(7,2) | $I_{FC}(2)$ | Calculated complementary table nozzle back pressure impulse for stage II (lb-sec) |
| 5863 | Z(8,2) | $\hat{I}_{vC}(2)$ | Calculated complementary table input total impulse adjusted to vacuum condition for stage II (lb-sec) |
| 5864 | Z(9,2) | $I_{vC}(2)$ | Calculated input vacuum corrected complementary table time adjusted thrust integral for stage II (lb-sec) |
| 5865 | Z(10,2) | $I_{vC}^*(2)$ | Calculated complementary table vacuum adjusted thrust integral for stage II (lb-sec) |
| 5866 | Z(11,2) | $K_{FC}^*(2)$ | Calculated complementary table thrust multiplier for stage II (Dim) |
| 5867 | Z(12,2) | $I_{spC}(2)$ | Calculated complementary table adjusted to vacuum specific impulse for stage II (sec) |

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|--|
| 5868 | Z(13,2) | $I_{VT}(2)$ | Calculated input main and complementary impulse corrected to vacuum conditions for stage II (lb-sec) |
| 5869 | Z(14,2) | $I_{VT}^*(2)$ | Calculated main and complementary vacuum adjusted thrust integral for Stage II (lb-sec) |
| 5870 | Z(15,2) | $I_{VT}(2)$ | Calculated input vacuum corrected main and complementary impulse time corrected for stage II (lb-sec) |
| 5871 | Z(1,3) | $I_{FM}(3)$ | Calculated main table nozzle back pressure impulse for stage III (lb-sec) |
| 5872 | Z(2,3) | $\hat{I}_{VM}(3)$ | Calculated main table input total impulse adjusted to vacuum conditions for stage III (lb-sec) |
| 5873 | Z(3,3) | $I_{VM}(3)$ | Calculated input vacuum corrected main table time adjusted thrust integral for stage III (lb-sec) |
| 5874 | Z(4,3) | $I_{VM}^*(3)$ | Calculated main table vacuum adjusted thrust integral for stage III (lb-sec) |
| 5875 | Z(5,3) | $K_{FM}^*(3)$ | Calculated main table thrust multiplier for stage III (dim) |
| 5876 | Z(6,3) | $I_{spM}(3)$ | Calculated main table adjusted to vacuum specific impulse for stage III (sec) |
| 5877 | Z(7,3) | $I_{FC}(3)$ | Calculated complementary table nozzle back pressure impulse for stage III (lb-sec) |
| 5878 | Z(8,3) | $\hat{I}_{VC}(3)$ | Calculated complementary table input total impulse adjusted to vacuum conditions for stage III (lb-sec) |
| 5879 | Z(9,3) | $I_{VC}(3)$ | Calculated input vacuum corrected complementary table time adjusted thrust integral for stage III (lb-sec) |
| 5880 | Z(10,3) | $I_{VC}^*(3)$ | Calculated complementary table vacuum adjusted thrust integral for stage III (lb-sec) |
| 5881 | Z(11,3) | K_{FC}^* | Calculated complementary table thrust multiplier for stage III (dim) |
| 5882 | Z(12,3) | $I_{spC}(3)$ | Calculated complementary table adjusted to vacuum specific impulse for stage III (sec) |

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|---|
| 5883 | Z(13,3) | $\hat{I}_{VT(3)}$ | Calculated input main and complementary impulse corrected to vacuum conditions for stage III (lb-sec) |
| 5884 | Z(14,3) | $I_{VT}^*(3)$ | Calculated main and complementary vacuum adjusted thrust integral for stage III (lb-sec) |
| 5885 | Z(15,3) | $I_{VT}(3)$ | Calculated input vacuum corrected main and complementary impulse time corrected for stage III (lb-sec) |
| 5886 | Z(1,4) | $I_{FM}(4)$ | Calculated main table nozzle back pressure impulse for stage IV (lb-sec) |
| 5887 | Z(2,4) | $\hat{I}_{VM}(4)$ | Calculated main table input total impulse adjusted to vacuum conditions for Stage IV (lb-sec) |
| 5888 | Z(3,4) | $I_{VM}(4)$ | Calculated input vacuum corrected main table time adjusted thrust integral for stage IV (lb-sec) |
| 5889 | Z(4,4) | $I_{VM}^*(4)$ | Calculated main table vacuum adjusted thrust integral for stage IV (lb-sec) |
| 5890 | Z(5,4) | $K_{FM}^*(4)$ | Calculated main table thrust multiplier for stage IV (dim) |
| 5891 | Z(6,4) | $I_{spM}(4)$ | Calculated main table adjusted to vacuum specific impulse for stage IV (sec) |
| 5892 | Z(7,4) | $I_{FC}(4)$ | Calculated complementary table nozzle back pressure impulse for stage IV (lb-sec) |
| 5893 | Z(8,4) | $\hat{I}_{VC}(4)$ | Calculated complementary table input total impulse adjusted to vacuum conditions for stage IV (lb-sec) |
| 5894 | Z(9,4) | $I_{VC}(4)$ | Calculated input vacuum corrected complementary table time adjusted thrust integral for stage IV (lb-sec) |
| 5895 | Z(10,4) | $I_{VC}^*(4)$ | Calculated complementary table vacuum adjusted thrust integral for stage IV (lb-sec) |
| 5896 | Z(11,4) | $K_{FC}^*(4)$ | Calculated complementary table thrust multiplier for stage IV (dim) |
| 5897 | Z(12,4) | $I_{spC}(4)$ | Calculated complementary table adjusted to vacuum specific impulse for stage IV (sec) |

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|--|
| 5898 | Z(13,4) | $\hat{I}_{VT(4)}$ | Calculated input main and complementary impulse corrected to vacuum conditions for stage IV (lb-sec) |
| 5899 | Z(14,4) | $I_{VT}^*(4)$ | Calculated main and complementary vacuum adjusted thrust integral for stage IV (lb-sec) |
| 5900 | Z(15,4) | $I_{VT(4)}$ | Calculated input vacuum corrected main and complementary impulse time corrected for stage IV (lb-sec) |
| 5901 | SAVED(1,1) | $V_{I(B1)}$ | Missile inertial velocity at the termination of stage I (ft/sec) |
| 5902 | SAVED(2,1) | $h_{(B1)}$ | Missile geometric altitude at the termination of stage I (ft) |
| *5903 | SAVED(3,1) | $\dot{\gamma}_{1(B1)}$ | Pitch flight path angle at the termination of stage I angle between the earth referenced velocity vector and the local tangent plane. Positive away from the earth (deg) |
| 5904 | SAVED(4,1) | $W_{(B1)}$ | Total missile weight at the termination of stage I (lb) |
| 5905 | SAVED(5,1) | $S_f(B1)$ | Total missile ground range at the termination of the glide phase if the powered flight were to end at the termination of stage I (nm) |
| 5906 | SAVED(6,1) | $L_F(B1)$ | Total thrust velocity loss due to back pressure for stage I (ft/sec) |
| 5907 | SAVED(7,1) | $L_D(B1)$ | Drag velocity loss for stage I (ft/sec) |
| 5908 | SAVED (8,1) | $L_g(B1)$ | Gravity velocity loss for stage I (ft/sec) |
| 5909 | SAVED(9,1) | $L_V(B1)$ | Vectoring velocity loss for stage I (ft/sec) |
| 5910 | SAVED(10,1) | $\Delta V_{(B1)}$ | Ideal missile velocity for stage I (ft/sec) |
| 5911 | SAVED(11,1) | $a_{XB(21)}$ | Vehicle acceleration due to total thrust and aerodynamic force at the termination of stage I (g's) |
| 5912 | SAVED(12,1) | $q_{(21)}$ | Missile dynamic pressure at the termination of stage I (lb/ft ²) |
| 5913 | SAVED(13,1) | $I_V(B1)$ | Total missile vacuum impulse for stage I (lb-sec) |
| 5914 | SAVED(14,1) | $h_p(B1)$ | Perigee altitude of the glide phase if the powered flight were to end at the termination of stage I (nm) |

*Stored values of saved angles are in degrees

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|---|
| 5915 | SAVED(15,1) | $h_a(B1)$ | Apogee altitude of the glide phase if the powered flight were to end at the termination of stage I (nm) |
| 5916 | SAVED(16,1) | $t_f(B1)$ | Total flight time to the termination of the glide phase if the powered flight were to end at the termination of stage I (sec) |
| *5917 | SAVED(17,1) | $\gamma_{IIf}(B1)$ | Impact or intercept inertial pitch flight path angle if the powered flight were to end at the termination of stage I (deg) |
| 5918 | SAVED(18,1) | $V_{If}(B1)$ | Missile inertial velocity at the termination of the glide phase if the powered flight were to end at the termination of stage I (ft/sec) |
| 5919-5925 | | | Open |
| 5926 | SAVED(1,2) | $V_I(B2)$ | Missile inertial velocity at the termination of stage II (ft/sec) |
| 5927 | SAVED(2,2) | $h(B2)$ | Missile geometric altitude at the termination of stage II (ft) |
| *5928 | SAVED(3,2) | $\gamma_1(B2)$ | Pitch flight path angle at the termination of stage II. Angle between the earth referenced velocity vector and the local tangent plane. Positive away from the earth. (deg) |
| 5929 | SAVED(4,2) | $W(B2)$ | Total instantaneous missile weight at the termination of stage II (lb) |
| 5930 | SAVED (5,2) | $S_f(B2)$ | Total missile ground range at the termination of the glide phase of the powered flight were to end at the termination of stage II (nm) |
| 5931 | SAVED(6,2) | $L_F(B2)$ | Total thrust velocity loss due to back pressure for stage II (ft/sec) |
| 5932 | SAVED(7,2) | $L_D(B2)$ | Drag velocity loss for stage II (ft/sec) |
| 5933 | SAVED(8,2) | $I_g(B2)$ | Gravity velocity loss for stage II (ft/sec) |
| 5934 | SAVED(9,2) | $L_V(B2)$ | Vectoring velocity loss for stage II (ft/sec) |
| 5935 | SAVED(10,2) | $\Delta V(B2)$ | Ideal missile velocity for stage II (ft/sec) |
| 5936 | SAVED(11,2) | $a_{xb}(B2)$ | Vehicle acceleration due to total thrust and aerodynamic force at the termination of stage II (g's) |

(Stored values of saved angles are in degrees)

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|---|
| 5937 | SAVED(12,2) | $q_{(B2)}$ | Missile dynamic pressure at the termination of stage II (lb/ft) |
| 5938 | SAVED(13,2) | $I_{V(B2)}$ | Total missile vacuum impulse for stage II (lb-sec) |
| 5939 | SAVED(14,2) | $h_{p(B2)}$ | Perigee altitude of the glide phase if the powered flight were to end at the termination of stage II (nm) |
| 5940 | SAVED(15,2) | $h_{a(B2)}$ | Apogee altitude of the glide phase if the powered flight were to end at the termination of stage II (nm) |
| 5941 | SAVED(16,2) | $t_{f(B2)}$ | Total flight time to the termination of the flight phase if the powered flight were to end at the termination of stage II (sec) |
| 5942 | SAVED(17,2) | $\gamma_{1If(B2)}$ | Impact or intercept inertial pitch flight path angle if the powered flight were to end at the termination of stage II (deg) |
| 5943 | SAVED(18,2) | $V_{If(B2)}$ | Missile inertial velocity at the termination of the glide phase if the powered flight were to end at the termination of stage II (ft/sec) |
| 5944-5950 | | | Open |
| 5951 | SAVED(1,3) | $V_I(B3)$ | Missile inertial velocity at the termination of stage III (ft/sec) |
| 5952 | SAVED(2,3) | $h_{(B3)}$ | Missile geometric altitude at the termination of stage III (ft) |
| 5953 | SAVED(3,3) | $\gamma_1(B3)$ | Pitch flight path angle at the termination of stage III. Angle between the earth referenced velocity vector and the local tangent plane. Positive away from the earth (deg) |
| 5954 | SAVED(4,3) | $W_{(B3)}$ | Total instantaneous missile weight at the termination of stage III (lb) |
| 5955 | SAVED(5,3) | $S_f(B3)$ | Total missile ground range at the termination of the glide phase if the powered flight were to end at the termination of stage III (nm) |
| 5956 | SAVED(6,3) | $L_F(B3)$ | Total thrust velocity loss due to back pressure for stage III (ft/sec) |
| 5957 | SAVED(7,3) | $L_D(B3)$ | Drag velocity loss due to back pressure for stage III (ft/sec) |

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|--|
| 5958 | SAVED(8,3) | $L_g(B3)$ | Gravity velocity loss for stage III (ft/sec) |
| 5959 | SAVED(9,3) | $L_V(B3)$ | Vectoring velocity loss for stage III (ft/sec) |
| 5960 | SAVED(10,3) | $\Delta_V(B3)$ | Ideal missile velocity for stage III (ft/sec) |
| 5961 | SAVED(11,3) | $a_{Xb}(B3)$ | Vehicle acceleration due to total thrust and aerodynamic force at the termination of stage III (g's) |
| 5962 | SAVED(12,3) | $q(B3)$ | Missile dynamic pressure at the termination of stage III (lb/ft ²) |
| 5963 | SAVED(13,3) | $I_V(B3)$ | Total missile vacuum impulse for stage III (lb-sec) |
| 5964 | SAVED(14,3) | $h_p(B3)$ | Perigee altitude of the glide phase if the powered flight were to end at the termination of stage III (nm) |
| 5965 | SAVED(15,3) | $h_a(B3)$ | Apogee altitude of the glide phase if the powered flight were to end at the termination of stage III (nm) |
| 5966 | SAVED(16,3) | $t_f(B3)$ | Total flight time to the termination of the glide phase if the powered flight were to end at the termination of stage III (sec) |
| 5967 | SAVED(17,3) | $\gamma_{If}(B3)$ | Impact or intercept inertial pitch flight path angle if the powered flight were to end at the termination of stage III (deg) |
| 5968 | SAVED(18,3) | $V_{If}(B3)$ | Missile inertial velocity at the termination of the glide phase if the powered flight were to end at the termination of stage III (ft/sec) |
| 5969-5975 | | | Open |
| 5976 | SAVED(1,4) | $V_I(B4)$ | Missile inertial velocity at the termination of stage IV (ft/sec) |
| 5977 | SAVED(2,4) | $h(B4)$ | Missile geometric altitude at the termination of stage IV (ft) |
| 5978 | SAVED(3,4) | $\gamma_1(B4)$ | Pitch flight path angle at the termination of stage IV. Angle between the earth referenced velocity vector and the local tangent plane. Positive away from the earth (deg) |
| 5979 | SAVED(4,4) | $W(B4)$ | Total instantaneous missile weight at the termination of stage IV (lb) |

| <u>L-number</u> | <u>FORTTRAN Symbol</u> | <u>Engineer's Symbol</u> | <u>Definition</u> |
|-----------------|----------------------------|------------------------------|---|
| 5980 | SAVED(5,4) | $S_f(B4)$ | Total missile ground range at the termination of the glide phase if the powered flight were to end at the termination of stage IV (nm) |
| 5981 | SAVED(6,4) | $L_F(B4)$ | Total thrust velocity loss due to back pressure for stage IV (ft/sec) |
| 5982 | SAVED(7,4) | $L_D(B4)$ | Drag velocity loss for stage IV (ft/sec) |
| 5983 | SAVED(8,4) | $L_g(B4)$ | Gravity velocity loss for stage IV (ft/sec) |
| 5984 | SAVED(9,4) | $L_V(B4)$ | Vectoring velocity loss for stage IV (ft/sec) |
| 5985 | SAVED(10,4) | $\Delta V(B4)$ | Ideal missile velocity for stage IV (ft/sec) |
| 5986 | SAVED(11,4) | $a_{xb}(B4)$ | Vehicle acceleration due to total thrust and aerodynamic force at the termination of stage IV (g's) |
| 5987 | SAVED(12,4) | $q(B4)$ | Missile dynamic pressure at the termination of stage IV (lb/ft ²) |
| 5988 | SAVED(13,4) | $I_V(B4)$ | Total missile vacuum impulse for stage IV (lb/sec) |
| 5989 | SAVED(14,4) | $h_p(B4)$ | Perigee altitude of the glide phase if the powered flight were to end at the termination of stage IV (nm) |
| 5990 | SAVED(15,4) | $h_a(B4)$ | Apogee altitude of the glide phase if the powered flight were to end at the termination of stage IV (nm) |
| 5991 | SAVED(16,4) | $t_f(B4)$ | Total flight time to the termination of the glide phase if the powered flight were to end at the termination of stage IV (sec) |
| 5992 | SAVED(17,4) | $\gamma_{1If}(B4)$ | Impact or intercept inertial pitch flight path angle if the powered flight were to end at the termination of stage IV (sec) |
| 5993 | SAVED(18,4) | $V_{If}(B4)$ | Missile inertial velocity at the termination of the glide phase if the powered flight were to end at the termination of stage IV (ft/sec) |
| 5994-5999 | | | Open |

4. Load Sheets

The load sheets are shown in the following pages.

BASIC INPUT

| LOCATION | Basic Deck | Ref Run | Run | Time, to | Disc Pt Start, Dy | Stage, K ₁ | Sp Pt Start, Sy | Velocity, V _{eo} | Launch, ϕ_i | Payload, WPL | Mass Grav, g_e | Desired, ϕ_{mo} | Miss Rat, R _{bo} | To Kc2 | Azimuth Flight Path | Gen Coord, ϕ_g | Gen Coord, ϕ_g | Gen 'I Coord | Jettison Weight |
|----------|------------|---------|-----|----------|-------------------|-----------------------|-----------------|---------------------------|------------------|--------------|------------------|----------------------|---------------------------|--------|---------------------|---------------------|---------------------|--------------|-----------------|
| L0 | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + |
| L3 | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + |
| L8 | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + |
| L10 | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + |
| L13 | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + |
| L20 | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + |
| L23 | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + |
| L28 | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + |
| L31 | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + |
| L37 | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + |
| L43 | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + |
| L46 | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + |
| L49 | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + |
| L55 | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + |
| L61 | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + |
| L7 | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + |

HUNTING PROCEDURES

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 | 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 | 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 | 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 | 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|------|---|---|---|---|---|---|---|---|----|-----------------|----|----------------------------|----|----------------------------|----|---------------------------|----|-------------------------|----|----------------------------|----|-----------------------------|----|-------------------------------|----|-----------------|----|----------------|----|-----------------|----|-----------------|----|-----------------|----|-----------------|----|-----------------|----|-----------------|----|-----------------|----|-----------------|----|-----------------|----|-----------------|----|-----------------|----|-----------------|----|-----------------|----|-----------------|----|-----------------|----|-----------------|----|-----------------|----|-----------------|----|-----------------|----|-----------------|----|-----------------|----|-----------------|----|-----------------|----|-----------------|----|-----------------|----|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|-----------------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|--|
| | | | | | | | | | | P1 | | K ₁ | | K ₂ | | K ₃ | | K ₄ | | K ₅ | | K ₆ | | K ₇ | | K ₈ | | K ₉ | | K ₁₀ | | K ₁₁ | | K ₁₂ | | K ₁₃ | | K ₁₄ | | K ₁₅ | | K ₁₆ | | K ₁₇ | | K ₁₈ | | K ₁₉ | | K ₂₀ | | K ₂₁ | | K ₂₂ | | K ₂₃ | | K ₂₄ | | K ₂₅ | | K ₂₆ | | K ₂₇ | | K ₂₈ | | K ₂₉ | | K ₃₀ | | K ₃₁ | | K ₃₂ | | K ₃₃ | | K ₃₄ | | K ₃₅ | | K ₃₆ | | K ₃₇ | | K ₃₈ | | K ₃₉ | | K ₄₀ | | K ₄₁ | | K ₄₂ | | K ₄₃ | | K ₄₄ | | K ₄₅ | | K ₄₆ | | K ₄₇ | | K ₄₈ | | K ₄₉ | | K ₅₀ | | K ₅₁ | | K ₅₂ | | K ₅₃ | | K ₅₄ | | K ₅₅ | | K ₅₆ | | K ₅₇ | | K ₅₈ | | K ₅₉ | | K ₆₀ | | K ₆₁ | | K ₆₂ | | K ₆₃ | | K ₆₄ | | K ₆₅ | | K ₆₆ | | K ₆₇ | | K ₆₈ | | K ₆₉ | | K ₇₀ | | K ₇₁ | | K ₇₂ | | K ₇₃ | | K ₇₄ | | K ₇₅ | | K ₇₆ | | K ₇₇ | | K ₇₈ | | K ₇₉ | | K ₈₀ | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | P2 | | σ _z | | z Accuracy, ε _z | | Model Acc, ε _m | | Final a, a _f | | a Accuracy, a _a | | Run Time, R _t | | Des Max, f _d | | ht ₂ | | Procedure 2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | σ _{z1} | | Initial X, x ₁₁ | | X Incr, x ₁₁ | | σ _{y1} | | Low y, y ₁₁ | | Upper y, y ₁₁ | | Constr Err, e _{cl} | | Transf Const, at ₁ | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| L 73 | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | + | |

[illegible]

563

Target range or orbital Alt. Sea

[illegible]

TVC DUTY CYCLE AND SLEW RATE CRITERIA

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 | 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 | 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 | 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 | 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
|---------------------------|---|---|---|---|---|---|---|---|----|---------------------------------|----|----|----|----|----|----|----|----|----|-------------------------|----|----|----|----|----|----|----|----|----|------------------------------|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| No Duty Pt, Δ_{dc} | | | | | | | | | | Duty Stage, K_{dc} | | | | | | | | | | Final wind h, h_a | | | | | | | | | | Start Wind h, h_a | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
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| Slew Freq, ω | | | | | | | | | | Stage 1 F/W A FW1 | | | | | | | | | | Vehicle Wt, W_{ol} | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| W_{TVC} | | | | | | | | | | W_{exi} | | | | | | | | | | I_{spaug} | | | | | | | | | | Refly | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
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| Noz Flange, x_{of} | | | | | | | | | | δ -design, δ_{me} | | | | | | | | | | Alt Max Wind, h_{mwd} | | | | | | | | | | Titled Print Flag, K_{TPF} | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
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568

MAIN THRUST-WEIGHT TABLE

[illegible]

MAIN THRUST-WEIGHT TABLE (continued)

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 | 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 | 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 | 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 | 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|----|-----------|----|----|----|----|----|----|----|----|----|-----------|----|----|----|----|----|----|----|----|----|-----------|----|----|----|----|----|----|----|----|----|-----------|----|----|----|----|----|----|----|----|----|-----------|----|----|----|----|----|----|----|----|----|-----------|----|----|----|----|----|----|----|----|----|-----------|----|----|----|----|----|----|----|----|----|-----------|--|--|--|--|--|--|--|--|--|-----------|--|--|--|--|--|--|--|--|--|-----------|--|--|--|--|--|--|--|--|--|-----------|--|--|--|--|--|--|--|--|--|-----------|--|--|--|--|--|--|--|--|--|-----------|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|
| | | | | | | | | | | t_{M13} | | | | | | | | | | t_{M14} | | | | | | | | | | t_{M15} | | | | | | | | | | t_{M16} | | | | | | | | | | t_{M17} | | | | | | | | | | t_{M18} | | | | | | | | | | t_{M19} | | | | | | | | | | t_{M20} | | | | | | | | | | t_{M21} | | | | | | | | | | t_{M22} | | | | | | | | | | t_{M23} | | | | | | | | | | t_{M24} | | | | | | | | | | t_{M25} | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | t_{M13} | | | | | | | | | | t_{M14} | | | | | | | | | | t_{M15} | | | | | | | | | | t_{M16} | | | | | | | | | | t_{M17} | | | | | | | | | | t_{M18} | | | | | | | | | | t_{M19} | | | | | | | | | | t_{M20} | | | | | | | | | | t_{M21} | | | | | | | | | | t_{M22} | | | | | | | | | | t_{M23} | | | | | | | | | | t_{M24} | | | | | | | | | | t_{M25} | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | t_{M13} | | | | | | | | | | t_{M14} | | | | | | | | | | t_{M15} | | | | | | | | | | t_{M16} | | | | | | | | | | t_{M17} | | | | | | | | | | t_{M18} | | | | | | | | | | t_{M19} | | | | | | | | | | t_{M20} | | | | | | | | | | t_{M21} | | | | | | | | | | t_{M22} | | | | | | | | | | t_{M23} | | | | | | | | | | t_{M24} | | | | | | | | | | t_{M25} | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | t_{M13} | | | | | | | | | | t_{M14} | | | | | | | | | | t_{M15} | | | | | | | | | | t_{M16} | | | | | | | | | | t_{M17} | | | | | | | | | | t_{M18} | | | | | | | | | | t_{M19} | | | | | | | | | | t_{M20} | | | | | | | | | | t_{M21} | | | | | | | | | | t_{M22} | | | | | | | | | | t_{M23} | | | | | | | | | | t_{M24} | | | | | | | | | | t_{M25} | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | t_{M13} | | | | | | | | | | t_{M14} | | | | | | | | | | t_{M15} | | | | | | | | | | t_{M16} | | | | | | | | | | t_{M17} | | | | | | | | | | t_{M18} | | | | | | | | | | t_{M19} | | | | | | | | | | t_{M20} | | | | | | | | | | t_{M21} | | | | | | | | | | t_{M22} | | | | | | | | | | t_{M23} | | | | | | | | | | t_{M24} | | | | | | | | | | t_{M25} | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | t_{M13} | | | | | | | | | | t_{M14} | | | | | | | | | | t_{M15} | | | | | | | | | | t_{M16} | | | | | | | | | | t_{M17} | | | | | | | | | | t_{M18} | | | | | | | | | | t_{M19} | | | | | | | | | | t_{M20} | | | | | | | | | | t_{M21} | | | | | | | | | | t_{M22} | | | | | | | | | | t_{M23} | | | | | | | | | | t_{M24} | | | | | | | | | | t_{M25} | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | t_{M13} | | | | | | | | | | t_{M14} | | | | | | | | | | t_{M15} | | | | | | | | | | t_{M16} | | | | | | | | | | t_{M17} | | | | | | | | | | t_{M18} | | | | | | | | | | t_{M19} | | | | | | | | | | t_{M20} | | | | | | | | | | t_{M21} | | | | | | | | | | t_{M22} | | | | | | | | | | t_{M23} | | | | | | | | | | t_{M24} | | | | | | | | | | t_{M25} | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | t_{M13} | | | | | | | | | | t_{M14} | | | | | | | | | | t_{M15} | | | | | | | | | | t_{M16} | | | | | | | | | | t_{M17} | | | | | | | | | | t_{M18} | | | | | | | | | | t_{M19} | | | | | | | | | | t_{M20} | | | | | | | | | | t_{M21} | | | | | | | | | | t_{M22} | | | | | | | | | | t_{M23} | | | | | | | | | | t_{M24} | | | | | | | | | | t_{M25} | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | t_{M13} | | | | | | | | | | t_{M14} | | | | | | | | | | t_{M15} | | | | | | | | | | t_{M16} | | | | | | | | | | t_{M17} | | | | | | | | | | t_{M18} | | | | | | | | | | t_{M19} | | | | | | | | | | t_{M20} | | | | | | | | | | t_{M21} | | | | | | | | | | t_{M22} | | | | | | | | | | t_{M23} | | | | | | | | | | t_{M24} | | | | | | | | | | t_{M25} | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | t_{M13} | | | | | | | | | | t_{M14} | | | | | | | | | | t_{M15} | | | | | | | | | | t_{M16} | | | | | | | | | | t_{M17} | | | | | | | | | | t_{M18} | | | | | | | | | | t_{M19} | | | | | | | | | | t_{M20} | | | | | | | | | | t_{M21} | | | | | | | | | | t_{M22} | | | | | | | | | | t_{M23} | | | | | | | | | | t_{M24} | | | | | | | | | | t_{M25} | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | t_{M13} | | | | | | | | | | t_{M14} | | | | | | | | | | t_{M15} | | | | | | | | | | t_{M16} | | | | | | | | | | t_{M17} | | | | | | | | | | t_{M18} | | | | | | | | | | t_{M19} | | | | | | | | | | t_{M20} | | | | | | | | | | t_{M21} | | | | | | | | | | t_{M22} | | | | | | | | | | t_{M23} | | | | | | | | | | t_{M24} | | | | | | | | | | t_{M25} | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | t_{M13} | | | | | | | | | | t_{M14} | | | | | | | | | | t_{M15} | | | | | | | | | | t_{M16} | | | | | | | | | | t_{M17} | | | | | | | | | | t_{M18} | | | | | | | | | | t_{M19} | | | | | | | | | | t_{M20} | | | | | | | | | | t_{M21} | | | | | | | | | | t_{M22} | | | | | | | | | | t_{M23} | | | | | | | | | | t_{M24} | | | | | | | | | | t_{M25} | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | t_{M13} | | | | | | | | | | t_{M14} | | | | | | | | | | t_{M15} | | | | | | | | | | t_{M16} | | | | | | | | | | t_{M17} | | | | | | | | | | t_{M18} | | | | | | | | | | t_{M19} | | | | | | | | | | t_{M20} | | | | | | | | | | t_{M21} | | | | | | | | | | t_{M22} | | | | | | | | | | t_{M23} | | | | | | | | | | t_{M24} | | | | | | | | | | t_{M25} | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | t_{M13} | | | | | | | | | | t_{M14} | | | | | | | | | | t_{M15} | | | | | | | | | | t_{M16} | | | | | | | | | | t_{M17} | | | | | | | | | | t_{M18} | | | | | | | | | | t_{M19} | | | | | | | | | | t_{M20} | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

COMPLEMENTARY THRUST-WEIGHT TABLE

| 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80 | | | | | | | | | | | |
|--|---|------------------------|-----------------------|-----------------------|--|---------------|--|---------------------|--|----------------------|--|
| Thrust Pert, K_{TC} | | Weight Pert, K_{TC} | | Time Pert, K_{TC} | | Imp, I_{sp} | | Exit Area, A_{eC} | | Initial Wt, W_{Co} | |
| 100 | + | Comp Impulse, I_{TC} | No Wt Carry, N_{TC} | KBD | | Perc | | | | | |
| 106 | + | Time | Thrust, F_{C1} | Weight Flow, W_{C1} | | | | | | | |
| 11 | + | t_{C2} | F_{C2} | W_{C2} | | | | | | | |
| 13 | + | t_{C3} | | | | | | | | | |
| 16 | + | t_{C4} | | | | | | | | | |
| 19 | + | t_{C5} | | | | | | | | | |
| 22 | + | t_{C6} | | | | | | | | | |
| 25 | + | t_{C7} | | | | | | | | | |
| 28 | + | t_{C8} | | | | | | | | | |
| 31 | + | t_{C9} | | | | | | | | | |
| 34 | + | t_{C10} | | | | | | | | | |
| 37 | + | t_{C11} | | | | | | | | | |
| 40 | + | t_{C12} | | | | | | | | | |
| 43 | + | t_{C13} | | | | | | | | | |
| 46 | + | t_{C14} | | | | | | | | | |
| 49 | + | | | | | | | | | | |

TOTAL AXIAL DRAG COEFFICIENT

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 | 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 | 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 | 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 | 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
|-----------------------|-----|-----|-----|-----|---|---|---|---|----|----|----|----|----|----|-----|-----|-----|-----|-----|----|----|----|----|----|----|----|----|----|----|-----|-----|-----|-----|-----|----|----|----|----|----|----|----|----|----|----|-----|-----|-----|-----|-----|----|----|----|----|----|----|----|----|----|----|-----|-----|-----|-----|-----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| Reference Area, S, RC | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
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| 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | | | | | |
| Reference Area, S, RC | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
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| 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | | | | | |
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| 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | | | | | |
| Reference Area, S, RC | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
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| 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | | | | | |
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| 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | | | | | |
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| 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | | | | | |
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| 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | | | | | |
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| 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | | | | | |
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| 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | | | | | |
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| 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | | | | | |
| Reference Area, S, RC | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
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| 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | | | | | |
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| 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | 185 | 188 | 196 | 204 | 212 | | | | | | | | | | | | | | | |
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AERODYNAMIC PITCH DAMPING COEFFICIENT

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| 308 | ND3 | |
| 311 | ND4 | |
| 314 | ND5 | |
| 317 | ND6 | |
| 320 | ND7 | |
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1. The first part of the document is a list of names and their corresponding addresses. The names are listed in a column on the left, and the addresses are listed in a column on the right. The names are: John Doe, Jane Smith, and Bob Johnson. The addresses are: 123 Main St, 456 Elm St, and 789 Oak St.

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 238. TIME
 239. BY
 240. INITIALS
 241. SIGNATURE
 242. DATE
 243. TIME
 244. BY
 245. INITIALS
 246. SIGNATURE
 247. DATE
 248. TIME
 249. BY
 250. INITIALS
 251. SIGNATURE
 252. DATE
 253. TIME
 254.

[illegible]

THE 21ST CENTURY

528

[illegible]

[illegible]

CENTER-OF-GRAVITY AND INERTIA DATA (Continued)

| | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|---------------------------|---|---|---|---|---|---|---|---|----|----|----|----|---------------------------|----|----|----|----|----|----|----|----|----|----|----|----|------------------------------|----|----|----|----|----|----|----|----|----|----|----|----|-----------------------------|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 | 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 | 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 | 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 | 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| Total Wt, W ₁₃ | | | | | | | | | | | | | Miss cg, cg ₁₃ | | | | | | | | | | | | | PIC Inertia, y ₁₃ | | | | | | | | | | | | | Offset, z, cg ₁₈ | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| + | | | | | | | | | | | | | + | | | | | | | | | | | | | + | | | | | | | | | | | | | + | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| W ₁₄ | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| + | | | | | | | | | | | | | + | | | | | | | | | | | | | + | | | | | | | | | | | | | + | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| W ₁₅ | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| + | | | | | | | | | | | | | + | | | | | | | | | | | | | + | | | | | | | | | | | | | + | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

ROLL VALUES

[illegible]

AERODYNAMIC ROLLING MOMENT

[illegible]

| Fin Area, S_F | | | | | | | | | | Hinge Pt B.S. x_{bz} | | | | | | | | | | Fin Hinge Pt. u_{hz} | | | | | | | | | | Root Chord length, l_{hz} | | | | | | | | | | K _{ref} | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|------------------------|---|---|---|---|---|---|---|---|----|-------------------------|----|----|----|----|----|----|----|----|----|-------------------------|----|----|----|----|----|----|----|----|----|-----------------------------|----|----|----|----|----|----|----|----|----|------------------------------|----|----|----|----|----|----|----|----|----|------------------|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 | 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 | 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 | 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 | 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 7.00 | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Fin Con. Flag K_{cf} | | | | | | | | | | Lin. Lift Mult C_{lz} | | | | | | | | | | Non Lift Mult C_{lzf} | | | | | | | | | | Drag Mult C_{Dz} | | | | | | | | | | Drag D.T. Lift Mult K_{lz} | | | | | | | | | | K _{ref} | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 7.05 | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | | | | | | | | | | |
| Mach No. M_1 | | | | | | | | | | C_{lz1} | | | | | | | | | | C_{lzf1} | | | | | | | | | | C_{Dz1} | | | | | | | | | | K_{lz1} | | | | | | | | | | u_{cz1} | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 7.10 | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | | | | | | | | | | |
| M_2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 7.16 | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | | | | | | | | | | |
| M_3 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 7.22 | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | | | | | | | | | | |
| M_4 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 7.28 | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | | | | | | | | | | |
| M_5 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 7.34 | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | | | | | | | | | | |
| M_6 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 7.40 | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | | | | | | | | | | |
| M_7 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 7.46 | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | | | | | | | | | | |
| M_8 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 7.52 | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | | | | | | | | | | |
| M_9 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 7.58 | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | | | | | | | | | | |
| M_{10} | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 7.64 | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | | | | | | | | | | |
| M_{11} | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 7.70 | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | | | | | | | | | | |
| M_{12} | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 7.76 | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | | | | | | | | | | |
| M_{13} | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 7.82 | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | | | | | | | | | | |
| M_{14} | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 7.88 | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | + | | | | | | | | | | | | | | | | | | | |

| | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|-----|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 | 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 | 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 | 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 | 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 | 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 | 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |
|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|-----|

N₁₅

C_{L215}

C_{L215}

C_{D215}

K_{L215}

U₂₁₅

N. PRINTOUT

Printout formats for the input and output prints are given in this section. The X's and O's shown in the formats represent spaces for integers and minus signs, respectively. The numbers and letters appearing at the left side of the printlines are always printed with their respective printlines.

The basic deck (BD), reference run (RR), and run (RUN) numbers and page number appear on every printout page. The date is also printed.

1. Input Print

Input is printed as shown in the following pages.

If all the parameters in a line are zero, the line is deleted. If the lines in a titled section contain all zeros, the title is deleted.

The T-card message is printed after the words "INPUT FOR".

INPUT PRINT

BD XXXX. RR XXXX. RU: XXXX. DATE XXX XX XXXX PAGE X
 INPUT FOR (MESSAGE IN TRAJECTORY RUN CARD, COLUMNS 2 THRU 57)

INITIAL CONDITIONS

| | | | | | | | |
|----|---------------------|----------------------|----------------------|----------------|-------------|-------|-------|
| | K_k | t_o | t'_k | T'_y | M'_y | S_y | D_y |
| 3 | OX. | XXXXXX,XXXX | XXXXXX,XXXX | OX. | OX. | OX. | OX. |
| | V_o | γ_o | h_o | S_o | | | |
| 10 | XXXXXX,XXX | XXXXXX,XXXX | XXXXXXXXXX, | XXXXXXXXXX, | | | |
| | ψ_i | θ_i | α_i | | | | |
| 14 | XXXX,XXXXXX | XXXX,XXXXXX | XXXX,XXXXXX | | | | |
| | ρ_L | μ_L | h_j | | | | |
| 17 | OX,XXXXXX | OX,XXXXXX | OX,XXXXXX | | | | |
| | W_{PL} | h_E | | | | | |
| 20 | XXXXXXXX,XX | XXXX,XXX. | XXXXXXXXXX, | | | | |
| | J | \bar{g}_e | g_e | r_e | ω | | |
| 23 | XXXX,XXXXXX | XXXX,XXXXXX | XXXX,XXXXXX | XXXXXXXXXXXX,X | OX,XXXXXXXX | | |
| | θ_{mo} | $\dot{\theta}_{mo}$ | $\ddot{\theta}_{mo}$ | | | | |
| 28 | XXXX,XXXXXX | XXXX,XXXXXX | XXXX,XXXXXX | | | | |
| | Q_{bo} | \bar{k}_{bo} | p_{bo} | | | | |
| 31 | XXXX,XXXX | XXXX,XXXXXX | XXXX,XXXXXX | | | | |
| | $\dot{\theta}_{bo}$ | $\ddot{\theta}_{bo}$ | $\ddot{\theta}_{bo}$ | | | | |
| 34 | XXXX,XXXXXX | XXXX,XXXXXX | XXXX,XXXXXX | | | | |

ORBITAL ELEMENT VALUES

| | | | | | | |
|----|---------------|---------------|-------------|------------|------------|------------|
| | k_{c1} | k_{c2} | h_f | k_γ | σ_c | h_e |
| 37 | OX,XXXXXXXXXX | OX,XXXXXXXXXX | XXXXXXXXXX, | OX. | XXXX | XXXXXXXXXX |

TRANSVERSE INITIAL CONDITIONS

| | | | |
|----|----------------|---------------|-------------|
| | S_{co} | γ_{20} | |
| 43 | XXXXXXXXXXXXX. | XXXXXX, XXXXX | XXXXXX, XXX |

GUIDANCE ALIGNMENT

| | | | |
|----|-------------|------------------|-------------------|
| | θ_g | $\dot{\theta}_g$ | $\ddot{\theta}_g$ |
| 46 | XXXX,XXXXXX | XXXX,XXXXXX | XXXX,XXXXXX |

JETTISON WEIGHT

49 w_{JT1} σ_{J1} K_{J1}
 OX.XXXXXXEOXX XXXX OX.XXXXXXEOXX

.

70 w_{JT8} σ_{J8} K_{J8}
 OX.XXXXXXEOXX XXXX OX.XXXXXXEOXX

HUNT PROCEDURE 1

73 P_1 K_x n_{t1} K_a σ_x σ_a K_b
 OX. OX. OXXX. OX. OXXX OXXX OXXX.

80 K_i ΔX a_f Δ_a
 OX.XXXXXXEOXX OX.XXXXXXEOXX OX.XXXXXXEOXX OXXX.XXXXX

HUNT PROCEDURE 2

84 $P2$ σ_z ϵ_z ϵ_m R_t f_D n_{t2}
 OX. OXXX OX.XXXXXXEOXX OX.XXXXXXEOXX OX.XXXXXXEOXX OX.XXXXXXEOXX OX.X

91 σ_{x1} x_{i1} Δx_{i1} σ_{y1} y_{L1} y_{U1}
 OXXX OX.XXXXXXEOXX OX.XXXXXXEOXX OXXX OX.XXXXXXEOXX OX.XXXXXXEOXX

97 ϵ_{c1} T_{T1} \bar{s}_{T1}
 OX.XXXXXXEOXX OXXX OX.XXXXXXEOXX

.

145 σ_{x7} x_{i7} Δx_{i7} σ_{y7} y_{L7} y_{U7}
 OXXX OX.XXXXXXEOXX OX.XXXXXXEOXX OXXX OX.XXXXXXEOXX OX.XXXXXXEOXX

151 ϵ_{c7} T_{T7} \bar{s}_{T7}
 OX.XXXXXXEOXX OXXX OX.XXXXXXEOXX

UPPER LIMIT P-2

154 x_{U1} x_{U2} x_{U3} x_{U4}
 OX.XXXXXXEOXX OX.XXXXXXEOXX OX.XXXXXXEOXX OX.XXXXXXEOXX

158 x_{U5} x_{U6} x_{U7}
 OX.XXXXXXEOXX OX.XXXXXXEOXX OX.XXXXXXEOXX

LOWER LIMIT P-2

161 x_{L1} x_{L2} x_{L3} x_{L4}
 OX.XXXXXXEOXX OX.XXXXXXEOXX OX.XXXXXXEOXX OX.XXXXXXEOXX

x_{L5} x_{L6} x_{L7}
 165 OX.XXXXXXEOXX OX.XXXXXXEOXX OX.XXXXXXEOXX OX.XXXXXXEOXX

COMPUTE INTERVAL.

| | | | | |
|-----|-----------------|-------------|-----------------|-------------|
| | Δt_{c1} | t_{c1} | Δt_{c2} | t_{c2} |
| 168 | OXXXX.XXXXX | OXXXX.XXXXX | OXXXX.XXXXX | OXXXX.XXXXX |
| | Δt_{c3} | t_{c3} | Δt_{c4} | t_{c4} |
| 172 | OXXXX.XXXXX | OXXXX.XXXXX | OXXXX.XXXXX | OXXXX.XXXXX |
| | Δt_{c5} | t_{c5} | Δt_{c6} | t_{c6} |
| 176 | OXXXX.XXXXX | OXXXX.XXXXX | OXXXX.XXXXX | OXXXX.XXXXX |
| | Δt_{c7} | t_{c7} | Δt_{c8} | t_{c8} |
| 180 | OXXXX.XXXXX | OXXXX.XXXXX | OXXXX.XXXXX | OXXXX.XXXXX |

MAIN PRINT

| | | | | |
|-----|-----------------|-------------|-----------------|-------------|
| | Δt_{p1} | t_{p1} | Δt_{p2} | t_{p2} |
| 184 | OXXXX.XXXXX | OXXXX.XXXXX | OXXXX.XXXXX | OXXXX.XXXXX |
| | Δt_{p3} | t_{p3} | Δt_{p4} | t_{p4} |
| 188 | OXXXX.XXXXX | OXXXX.XXXXX | OXXXX.XXXXX | OXXXX.XXXXX |
| | Δt_{p5} | t_{p5} | Δt_{p6} | t_{p6} |
| 192 | OXXXX.XXXXX | OXXXX.XXXXX | OXXXX.XXXXX | OXXXX.XXXXX |
| | Δt_{p7} | t_{p7} | Δt_{p8} | t_{p8} |
| 196 | OXXXX.XXXXX | OXXXX.XXXXX | OXXXX.XXXXX | OXXXX.XXXXX |

PRINT FLAGS

PL-DA PL-GB PL-K PL-KB PL-N PL-O
 200 OX. OX. OX. OX. OX. OX. OX. OX. OX.

AUXILIARY PRINT

| | | | | | | | | | | | |
|-----|-----------------|---------------|-----------------|---------------|---------------|---------------|---------------|---------------|---------------|----------------|----------------|
| | σ_{P1} | σ_{P2} | σ_{P3} | σ_{P4} | σ_{P5} | σ_{P6} | σ_{P7} | σ_{P8} | σ_{P9} | σ_{P10} | σ_{P11} |
| 209 | OXXXX | OXXXX | OXXXX | OXXXX | OXXXX | OXXXX | OXXXX | OXXXX | OXXXX | OXXXX | OXXXX |
| | Δt_{P1} | t_{P1} | Δt_{P2} | t_{P2} | | | | | | | |
| 220 | OXXXX.XXXXX | OXXXX.XXXXX | OXXXX.XXXXX | OXXXX.XXXXX | | | | | | | |
| | Δt_{P3} | t_{P3} | Δt_{P4} | t_{P4} | | | | | | | |
| 224 | OXXXX.XXXXX | OXXXX.XXXXX | OXXXX.XXXXX | OXXXX.XXXXX | | | | | | | |
| | Δt_{P5} | t_{P5} | Δt_{P6} | t_{P6} | | | | | | | |
| 228 | OXXXX.XXXXX | OXXXX.XXXXX | OXXXX.XXXXX | OXXXX.XXXXX | | | | | | | |

| | | | | |
|-----|-----------------|-------------|-----------------|-------------|
| | Δt_{p7} | t_{p7} | Δt_{p8} | t_{p8} |
| 232 | XXXXX.XXXXX | XXXXX.XXXXX | XXXXX.XXXXX | XXXXX.XXXXX |

SPECIAL PRINT

| | | | | | |
|-----|---------------|------------|-------|---------------|----------|
| | σ_{t1} | K_{t1} | | σ_{t2} | K_{t2} |
| 236 | XXXXX | OX.XXXXXXE | XXXXX | OX.XXXXXXE | XXXXX |
| | σ_{t3} | K_{t3} | | σ_{t4} | K_{t4} |
| 240 | XXXXX | OX.XXXXXXE | XXXXX | OX.XXXXXXE | XXXXX |
| | σ_{t5} | K_{t5} | | σ_{t6} | K_{t6} |
| 244 | XXXXX | OX.XXXXXXE | XXXXX | OX.XXXXXXE | XXXXX |
| | σ_{t7} | K_{t7} | | σ_{t8} | K_{t8} |
| 248 | XXXXX | OX.XXXXXXE | XXXXX | OX.XXXXXXE | XXXXX |

DISCONTINUITY PRINT

| | | | | | | | | |
|-----|---------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|
| | σ_{D1} | σ_{D2} | σ_{D3} | σ_{D4} | σ_{D5} | σ_{D6} | σ_{D7} | σ_{D8} |
| 252 | XXXXX | XXXXX | XXXXX | XXXXX | XXXXX | XXXXX | XXXXX | XXXXX |

MAXIMUM PRINT

| | | | | | | | | | | |
|-----|----------|---------------|----------|---------------|----------|---------------|----------|---------------|----------|---------------|
| | T_{m1} | σ_{m1} | T_{m2} | σ_{m2} | T_{m3} | σ_{m3} | T_{m4} | σ_{m4} | T_{m5} | σ_{m5} |
| 260 | XXXX. | XXXXX | XXXX. | XXXXX | XXXX. | XXXXX | XXXX. | XXXXX | XXXX. | XXXXX |

STAGING VALUES

| | | | | | | | | | | |
|-----|----------|---------------|----------|---------------|----------|---------------|----------|---------------|----------|---------------|
| | T_{B1} | σ_{B1} | T_{B2} | σ_{B2} | T_{B3} | σ_{B3} | T_{B4} | σ_{B4} | T_{B5} | σ_{B5} |
| 270 | OX. | XXXXX | OX. | XXXXX | OX. | XXXXX | OX. | XXXXX | OX. | XXXXX |

INTEGRATION TOLERANCES

| | | |
|-----|----------------|------------|
| | σ_{A1} | A_{r1} |
| 280 | XXXXX | OX.XXXXXXE |
| | σ_{A2} | A_{r2} |
| 282 | XXXXX | OX.XXXXXXE |
| | σ_{A12} | A_{r8} |
| 302 | XXXXX | OX.XXXXXXE |

BREAK UP TOLERANCES

A_t B_t A_x B_x
 L306 $\pm 0.00000000E+XX$ $\pm 0.0000000E+XX$ $\pm 0.0000000E+XX$ $\pm 0.00000000E+XX$

ATTITUDE CONTROL

T_{y1} σ_{f1} K_{f1} $Q_{m16}, \alpha_{i1}, \kappa_{D1}$ $R_{m1}, \alpha_{i1}, \kappa_{R1}$ P_{m1}, α_{max1}
 310 OX. OXXXX OX.XXXXXXE OX OX.XXXXXXE OX OX.XXXXXXE OX OXXX.XXXXXX

 T_{y13} σ_{f13} K_{f16} $Q_{m16}, \alpha_{i16}, \kappa_{D16}$ $R_{m16}, \alpha_{i16}, \kappa_{R13}$ P_{m13}, α_{max13} τ_{p13}
 394 OX. OXXXX OX.XXXXXXE OX OX.XXXXXXE OX OX.XXXXXXE OX OXXX.XXXXXX OX.XXX.XXXXX
 401 OXXXX.XXXXX OXXXX.XXXXX OXXXX.XXX OXXXX.XXXXX OXXXX.XXXXX OXXXX.XXXXX

WIND PROFILE

K_h K_v K_z
 407 OX.XXXXXXE OX.XXXXXXE OX.XXXXXXE
 h_1 v_{w1} w_1
 410 OX.XXXXXXE OX.XXXXXXE OXXX.XX
 . . .
 h_{30} v_{w30} w_{30}
 497 OX.XXXXXXE OX.XXXXXXE OXXX.XX

MODE

M_{y1} α_{M1} K_{M1}
 600 OX. OXXXX OX.XXXXXXE
 . . .
 M_{y10} α_{M10} K_{M10}
 627 OX. OXXXX OX.XXXXXXE

TARGET DYNAMICAL CONDITIONS

α_{Tto} K_{Tto}
 630 OXXXX OX.XXXXXXE
 v_{Tto} γ_{Tto} h_T ξ_{Tto} S_{Tto} S_{Tco}
 632 OXXXX.XXX OXXXX.XXXX OXXX.XXX OXXXXXX OXXXXXXX OXXXXXXX
 633 OXXXX.XXXX OXXXX.XXXX

640 t_{T1} a_{TT1} a_{TN1} a_{TC1}
 OXXXXX.XXX OXXX.XXXXX OXXX.XXXXX OXXX.XXXXX

664 t_{T7} a_{TT7} a_{TN7} a_{TC7}
 OXXXXX.XXX OXXX.XXXXX OXXX.XXXXX OXXX.XXXXX

668 OXXXXX.XXXX OXXXXX.XXXX
 DUTY CYCLE AND SLEW RATE GRIT

670 Δ_{dc} k_{dc} h_{α} h_{β}
 OXX OX OXXXXXX.XX OXXXXXX.XX

674 ω_s A_{FW1} W_{01}
 XXXX.XXXXX OXX.XXXXX XXXXXXXXX.

TVC PROPERTIES

677 W_{TVC} W_{exi} I_{spaug}
 OX.XXXXXXEOXX OX.XXXXXXEOXX OXXX.XXXXXX

680 x_{nf} δ_{me} h_{mxwd} k_{tpf}
 OXXXXX.XXXXX OXX.XXXXXX OXXXXXXX.XX OXX.

TITLED PRINT FLAG

683 K_{TPF} K_{TIF}
 OXX. OXX

THRUST MODULATION CONTROL

| | | | | | | |
|-----|----------|----------------|---------------|-----------|---------------|--------------|
| | F_{y1} | σ_{Fy1} | K_{Fy1} | T_{Mc1} | C_{Fy1} | τ_{Fy1} |
| 800 | 0XX. | 0XXXX. | 0X.XXXXXXE0XX | 0XX. | 0X.XXXXXXE0XX | 0XXXXX.XXXXX |

| | | | |
|-----|---------------|--------------|---------------------------|
| | MIN_1 | $q_{max\ 1}$ | $q_{min\ 1}$ |
| 806 | 0X.XXXXXXE0XX | 0XXXXX.XXXXX | 0XXXXX.XXXXX 0XXXXX.XXXXX |

| | | | |
|---|---|---|---|
| . | . | . | . |
| . | . | . | . |
| . | . | . | . |

| | | | | |
|-----|----------|----------------|---------------|---------------------------------|
| | F_{y7} | σ_{Fy7} | K_{Fy7} | |
| 860 | 0XX | 0XXXX. | 0X.XXXXXXE0XX | 0XX. 0X.XXXXXXE0XX 0XXXXX.XXXXX |

| | | | |
|-----|---------------|--------------|---------------------------|
| | MIN_7 | $q_{max\ 7}$ | $q_{min\ 7}$ |
| 866 | 0X.XXXXXXE0XX | 0XXXXX.XXXXX | 0XXXXX.XXXXX 0XXXXX.XXXXX |

SPECIFIC VELOCITY TIME PROFILE

| | | |
|------|--------------|--------------|
| | t_{VP1} | V_{P1} |
| L870 | 0XXXXX.XXXXX | 0XXXXX.XXXXX |

| | |
|---|---|
| . | . |
| . | . |
| . | . |

| | | |
|------|--------------|---------------|
| | t_{VP15} | V_{p15} |
| L898 | 0XXXXX.XXXXX | 0XXXXXX.XXXXX |

INPUT PRINT

STAGE ONE

MAIN THRUST-WEIGHT

| | | | | | | |
|------|--------------|---------------|----------------|---------------|------------|-------|
| | σ_s | D_p | r'_{b1000} | k_3 | | |
| 1000 | 0XXXX | 0X.XXXXXXE0XX | 0X.XXXXXXE0XX | 0X.XXXXXXE0XX | | |
| | I'_{VT} | I'_{VM} | W | | | |
| 1004 | 0.XXXXXXXX.X | 0XXXXXXX.X | 0X.XXXXXXE0XX | | | |
| | K'_F | K'_W | K'_t | I_{spM} | A'_{eM} | K_0 |
| 1007 | 0X.XXXXXXXX | 0X.XXXXXXXX | 0X.XXXXXXXX | 0XXX.XXXXX | 0XXX.XXXXX | 0X. |
| | ϵ_d | γ_d | C'_D | α_d | | |
| 1013 | 0XXXX.XXX | 0XXXX.XXX | 0XXXX.XXX | 0XXXX.XXX | | |
| | a_s | b_s | c_s | P_{arM} | | |
| 1017 | 0XXXX.XXX | 0XXXX.XXX | 0XXXX.XXX | 0XXXX.XXX | | |
| | t'_1 | F_1 | \dot{W}_{25} | | | |
| 1020 | 0XXXX.XXXX | 0X.XXXXXXE0XX | 0X.XXXXXXE0XX | | | |
| | . | . | . | | | |
| | . | . | . | | | |
| | t'_{25} | F_{25} | \dot{W}_{25} | | | |
| 1092 | 0XXXXX.XXXX | 0X.XXXXXXE0XX | 0X.XXXXXXE0XX | | | |

MAIN THRUST MOTOR BALLISTICS

| | | | | | |
|------|---------------|---------------|---------------|---------------|----------------|
| K095 | X.XXXXXX | X.XXXXXX | X.XXXXXX | +O.XXXXXXD+XX | XXXXX.XXX |
| | CSTAR | ATREF | RB1000 | FWT | WP |
| | XXXXX.XXX | XXXXX.XXX | XX.XXXXXX | XXXXX.XXX | XXXXXXXXXX.XXX |
| | ITM | A | CAS1 | CAS2 | CAS3 |
| | +O.XXXXXXD+XX | X.XXXXXXXX | +O.XXXXXXD+XX | +O.XXXXXXD+XX | +O.XXXXXXD+XX |
| | AXMAX | AXMIN | PCMXA | PCBREF | |
| | XXXXXX.XXX | XXXXXX.XXX | XXXXX.XXX | XXXXX.XXX | |
| J | TIME | VAC THRUST | CH. PRES | PCDOT | PROP FRACT. |
| II | XXX.XXXXX | +O.XXXXXXD+XX | XXXXX.XXX | +O.XXXXXXD+XX | X.XXXXX |
| . | . | . | . | . | . |
| . | . | . | . | . | . |
| I3 | XXX.XXXXX | +O.XXXXXXD+XX | XXXXX.XXX | +O.XXXXXXD+XX | X.XXXXX |
| J | TIME | WEB | SURFACE | VOLUME | EX. AREA |
| | XXX.XXXXX | X.XXXXX | +O.XXXXXXD+XX | +O.XXXXXXD+XX | XXXXXX.XXX |
| . | . | . | . | . | . |
| . | . | . | . | . | . |
| I3 | XXX.XXXXX | X.XXXXX | +O.XXXXXXD+XX | +O.XXXXXXD+XX | XXXXXX.XXX |

COMPLEMENTARY THRUST-WEIGHT

| | | | | | |
|------|-----------------|------------|-----------------|------------|------------|
| 1100 | K'_{FC} | K_{WC} | K_{tC} | I_{spC} | A_{eC} |
| | OX.XXXXXXX | OX.XXXXXXX | OX.XXXXXXX | XXXX.XXXXX | XXXX.XXXXX |
| 1105 | W_{Co} | I'_{vC} | \dot{X}_{NO} | K_{BD} | P_{arC} |
| | OXXXXXXX.X | OXXXXXXX.X | OX.X | OX.X | XXXX.XXXXX |
| 1110 | \dot{t}'_{C1} | F_{C1} | \dot{W}_{C1} | | |
| | OXXXXX.XXX | OX.XXXXXXX | OX.XXXXXXX | | |
| . | . | . | . | | |
| . | . | . | . | | |
| 1182 | t'_{25} | F_{C25} | \dot{W}_{C25} | | |
| | OXXXXX.XXX | OX.XXXXXXX | OX.XXXXXXX | | |

AXIAL FORCE COEFFICIENTS

1185 S_{RC} \bar{C}' OXXXXX.XXXXXX OXX.XXXXXXX OXXXXXX.XXXXXX

1186 M_1 C_{A1} OXXXXX.XXXXXX OXX.XXXXXXX

1216 M_{15} C_{A15} OXXXXX.XXXXXX OXX.XXXXXXX

PLAN FORM

1218 S_{PF} x_{PC} OXXXXX.XXXXXX OXXXXX.XXXXXX

NORMAL FORCE COEFFICIENTS

1220 S_{RN} \bar{N}' \bar{x}_{cp} OXXXXX.XXXXXX OXX.XXXXXXX OXX.XXXXXXX

1223 M_1 C_{N11} C_{N21} C_{N31} x_{cp1} OXXX.XXXXXX OX.XXXXXXX OXXOX.XXXXXXX OXXOX.XXXXXXX OXXXXX.XXXXXX

1293 M_{15} C_{N115} C_{N215} C_{N315} x_{cp15} OXXX.XXXXXX OX.XXXXXXX OXXOX.XXXXXXX OXXOX.XXXXXXX OXXXXX.XXXXXX

AERODYNAMIC PITCH DAMPING COEFFICIENTS

1298 D_{RN} \bar{M}_Q \bar{M}_{α} XXXX.XXXXXX OXX.XXXXXX OXX.XXXXXX

1301 K_Q x'_{RQ} K_{α} $x'_{R\alpha}$ OXX.XXXXXX XXXX.XXXXXX OXX.XXXXXX XXXX.XXXXXX

1305 M_1 C_{MQ1} $C_{M\alpha1}$ XXX.XXXXXX OX.XXXXXXX OXXOX.XXXXXXX

1347 M_{15} C_{MQ15} $C_{M\alpha15}$ XXX.XXXXXX OX.XXXXXXX OXXOX.XXXXXXX

CLUSTER CHARACTERISTICS AND SIDE IMPULSE

1380 n_m n_c R_c a_{It} a_{tb} ϕ_v
 XXXX XXXX OXX.XXXX OXX.XXXX OXX.XXXX OXX.XXXX

TVC ANOMALIES

1386 A_L K'_A ω_L δ_{MP} δ_{MY}
 OXX.XXX OXX.XXXX OXX.XXXX OXX.XXXX OXX.XXXX

PITCH STEERING

1391 a_{01} a_{i1}
 OXXX.XXXXXXXXXX OX.XXXXXXXXXXEOXX

1393 b_{11} b_{21} b_{31} τ_{f1}
 OX.XXXXXXXXXXEOXX OX.XXXXXXXXXXEOXX OX.XXXXXXXXXXEOXX OXXX.XXXXXXXXXX

STEERING COEFFICIENT EVALUATION

1397 σ_{g11} K_{g11} σ_{g21} K_{g21}
 OXXX OX.XXXXXXX OXXX OX.XXXXXXXEOXX

YAW STEERING

1401 K_{yk} τ_{yk}
 OX.XXXXXXXXXXEOXX OXXXXX.XXXXXX

ROLL ANOMALIES

1403 δ_{MR} SR K_{RC} η_{Vr}
 OXX.XXXXXX XXXXX.XXXXXX OXX. OXXXXX.XXXXXX

JET DAMPING

1417 x'_{Pf} x'_{Pa} x'_E
 OXXXX.XXXX OXXXX.XXXX OXXXX.XXXX

INITIAL TVC CONDITIONS

| | δ_{Po} | $\dot{\delta}_{Po}$ | δ_{Yc} | $\dot{\delta}_{Yc}$ | F_{Ro} |
|------|---------------|---------------------|---------------|---------------------|-------------------|
| 1420 | 0XX.XXXXXX | 0XXX.XXXXXX | 0XX.XXXXXX | 0XXX.XXXXXX | 0X.XXXXXXXXXXEOXX |
| 1425 | 0XXXXX.XXXXXX | 0XXXXX.XXXXXX | 0XXXXX.XXXXXX | 0XXXXX.XXXXXX | |

STAGE ATTITUDE REACTION

| | ΔQ_s | ΔR_b |
|------|--------------|--------------|
| 1428 | 0XXX.XXXXXX | 0XXX.XXXXXX |

GIMBAL LOCATIONS

| | \bar{x}_e | x'_e | y'_e | z'_e | K_5 |
|------|-------------|-----------|-----------|-----------|-----------|
| 1430 | XX.XXXXXX | XX.XXXXXX | XX.XXXXXX | XX.XXXXXX | XX.XXXXXX |

TVC CHARACTERISTICS

| | τ_c | t_c | ω_c | t_v | ω_v |
|------|------------|-----------|------------|-----------|------------|
| 1435 | XXX.XXXXXX | XX.XXXXXX | XX.XXXXXX | XX.XXXXXX | XX.XXXXXX |

LIMITS

| | L_1 | L_2 | L_3 | L_4 | L_5 |
|------|-----------|--------|--------|-----------|----------|
| 1440 | XXXXX.XXX | XX.XXX | XX.XXX | XXXXX.XXX | XX.XXX |
| | L_6 | L_7 | L_8 | L_9 | L_{10} |
| 1445 | XXXXX.XXX | XX.XXX | XX.XXX | XXXXX.XXX | XX.XXX |

GAINS

| | K_{DP1} | K_{DY1} | K_{RP1} | K_{RY1} | |
|------|-----------|-----------|-----------|---------------|-------------------|
| 1450 | XX.XXXXXX | XX.XXXXXX | XX.XXXXXX | XX.XXXXXX | |
| | K_{IP1} | K_{IY1} | f_{G1} | σ_{G1} | K_{G1} |
| 1454 | XX.XXXXXX | XX.XXXXXX | 0X. | 0XXXX | 0X.XXXXXXXXXXEOXX |
| | K_{DP2} | K_{DY2} | K_{RP2} | K_{RY2} | |
| 1459 | XX.XXXXXX | XX.XXXXXX | XX.XXXXXX | XX.XXXXXX | |
| | K_{IP2} | K_{IY2} | f_{G2} | σ_{G2} | K_{G2} |
| 1463 | XX.XXXXXX | XX.XXXXXX | 0X. | 0XXXX | 0X.XXXXXXXXXXEOXX |
| | K_{DP3} | K_{DY3} | K_{RP3} | K_{RY3} | |
| 1468 | XX.XXXXXX | XX.XXXXXX | XX.XXXXXX | XX.XXXXXX | |
| | K_{IP3} | K_{IY3} | f_{G3} | | |
| 1472 | XX.XXXXXX | XX.XXXXXX | 0X. | | |

MASS PROPERTIES

| | | | | | |
|------|-----------------------------|------------------------------|-----------------------------|---------------------------|--------------------------|
| 1475 | \bar{I}_Y OXX.XXXXXX | \bar{I}_Z OXX.XXXXXX | \bar{I}_X OXX.XXXXXX | | |
| 1478 | \bar{W} OX.XXXXXEOXX | \bar{x}_{cg} OXX.XXXXXX | z'_{cg} OXX.XXXXXX | y'_{cg} OXX.XXXXXX | |
| 1482 | W_n OXXXXXX.XX | I_n OXXXXXX.XX | x_n OXXXX.XXXXX | | |
| 1485 | OXXXXXX.XXXXX | OXXXXX.XXXXX | OXXXXX.XXXXX | | |
| 1488 | W_1 OXXXXXXXXXX.X | X_{cg1} OXXXXX.XXXXX | I_{y1} OXXXXXXXX.XX | Z_{cg1} OXXX.XXXXXX | I_{z1} OXXXXXXXX.XX |
| 1492 | I_{Z1} OXXXXXXXX.XX | Y_{cg1} OXXX.XXXXX | I_{X1} OXXXXXXXX.XX | | |
| 1495 | I_{XY1} OXXXXXXXX.XXX | I_{YZ1} OXXXXXXXX.YXX | I_{ZX1} OXXXXXXXX.XXX | | |
| 1628 | W_{15} OXXXXXXXX.X | X_{cg15} OXXXXX.XXXXX | I_{Y15} OXXXXXXXX.XX | Z_{cg15} OXXX.XXXXXX | |
| 1692 | I_{Z15} OXXXXXXXX.XX | Y_{cg15} OXXX.XXXXX | I_{X15} OXXXXXXXX.XX | | |
| 1695 | I_{XY15} OXXXXXXXX.XXX | I_{XZ15} OXXXXXXXX.XXX | I_{ZX15} OXXXXXXXX.XXX | | |

ROLL CONTROL

| | L_{R1} | T_{R1} | D_1 | $F_{\Delta 1}$ | L_{Rc1} |
|------|---------------|----------------|-------------|----------------|---------------|
| 1638 | XXXXXX.XXXX | XX.XXXXXXXXXX | X.XXXXXXXX | XXX.XXXXXXX | XXXXXX.XXXXXX |
| | K_{DR1} | | K_{RR1} | I_{spR1} | t'_{R2} |
| 1643 | XXXXXX.XXXX | XX.XXXXXXXXXX | X.XXXXXXXX | XXX.XXXXXXX | XXXXXX.XXXXXX |
| | L_{R2} | T_{R2} | D_2 | $F_{\Delta 2}$ | L_{Rc2} |
| 1648 | XXXXXX.XXXX | XXXX.XXXXXX | XX.XXXXXXX | XXX.XXXXXX | XXXXXX.XXXXXX |
| | K_{DR2} | | K_{RR2} | I_{spR2} | t'_{R3} |
| 1653 | XXXX.XXXX | XXX.XXXXXXXXXX | XX.XXXXXXXX | XXXX.XXXXXXX | XXXX.XXXXXX |
| | L_{R3} | T_{R3} | D_3 | $F_{\Delta 3}$ | L_{Rc3} |
| 1658 | XXXXXX.XXXXXX | XXXX.XXXXXX | XX.XXXXXXX | XXX.XXXXXX | XXXX.XXXXXX |
| | K_{DR3} | | K_{RR3} | I_{spR3} | |
| 1663 | XXXX.XXXX | XXX.XXXXXXXXXX | XX.XXXXXXXX | XXXX.XXXXXXX | |

AERODYNAMIC ROLLING MOMENT

| | S_{RR1} | γ_{R1} | φ_{R1} |
|------|--------------|---------------|----------------|
| 1667 | OXXXXX.XXXX | OXXXXX.XXXX | OXXXXX.XXXX |
| | S_{RR2} | γ_{R2} | φ_{R2} |
| 1670 | OXXXXX.XXXX | OXXXXX.XXXX | OXXXXX.XXXX |
| | M_1 | C_1 | |
| 1673 | OXXXXXXXX.XX | OXXXXXXXX.XX | |
| | | | |
| | M_{10} | C_{10} | |
| 1691 | OXXXXXXXX.XX | OXXXXXXXX.XX | |

AERODYNAMIC MOVABLE PITCH CONTROL FINS COEFFICIENTS

| | | | | | |
|------|--------------------------|-------------------------------|-------------------------------|-------------------------------|-------------------------------|
| 1700 | S_{Fz} OXXXX.XXXXX | x_{nz} OXXXX.XXXXX | U_{bz} OXX.XXXXXXX | l_{bz} OXXXX.XXXXX | K'_{Ycf} OXXXX.XXXXX |
| 1705 | K'_{cf} OXXXX.XXXXX | \bar{C}'_{Lz} OXXX.XXXXX | \bar{C}'_{lz} OXXX.XXXXX | \bar{C}'_{Dz} OXXX.XXXXX | \bar{K}'_{Lz} OXXX.XXXXX |
| 1710 | M_1 OXX.XXXX | C_{Lz15} OXXX.XXXXXXX | C_{lz15} OX.XXXXXXXOXX | C_{Dz15} OX.XXXXXXX | K_{Lz15} OXX.XXXXXXX |
| | . | . | . | . | . |
| | . | . | . | . | . |
| 1794 | M_{15} OXX.XXXX | C_{Lz15} OXXX.XXXXXXX | C_{lz15} OX.XXXXXXXOXX | C_{Dz15} OX.XXXXXXX | K_{Lz15} OXX.XXXXXXX |
| | | | | | U_{cz15} OX.XXXXXXX |

STAGE TWO

2000

.
.
.

2999

STAGE THREE

3000

.
.
.

3999

STAGE FOUR

4000

.
.
.

4999

2. OUTPUT PRINT

The output print contains the parameters which are computed during the trajectory. The output print is separated into two formats. Format I contains stage identified time oriented blocks consisting of printlines A thru P, the main print: Y thru YD, the hunt print: Z thru ZB, the auxiliary print: X thru XA, the steering coefficients print: and V, the maximum print.

Format II consists of the TVC duty cycle print blocks consisting of printlines WA thru WO. Format II follows the entire trajectory Format I.

a. Format I Output Print

Format I output print is given following the input print defined in section 9.1 or the hunt print if it exists. Each stage is titled as specified in the "output stage identification" logic. The printline blocks in the main print, hunt print, and auxiliary print, are time sequenced. The steering coefficients print block are given at stage termination. The main print, hunt print, auxiliary print, and steering coefficients print arrangements are pictured in this section.

(1) Output Stage Identification

The start of each stage is identified by the message:

INITIATION OF STAGE K_k

where K_k is the stage number, i.e., 1, 2, 3, or 4

After the stage termination printout type:

Following the time oriented print, one of these three messages will appear:

1. Normal stage termination

TERMINATION OF STAGE K_k

where K_k is the stage number, i.e., 1, 2, 3, or 4

2. End of flight control table

TRAJECTORY HALTED-END OF FLIGHT CONTROL TABLE

3. End of mode control table

TRAJECTORY HALTED-END OF MODE CONTROL TABLE

(2) Main Print

The main print contains printlines A, B, A, and succeeding printlines when the following special criteria are met. The main print is given when criteria of paragraph K.3.a, K.3.b, and K.3.c are satisfied.

| <u>Printline</u> | <u>Obtained</u> |
|------------------|--------------------------------|
| A | Always |
| AA | If $M_y = 4$ or 5 |
| E | Always |
| BA | If $M_y = 4$ or 5 |
| BB | If $M_y = 4$ or 5 |
| C | Always |
| CA | If $M_y = 2$ or 5 |
| CB | If $M_y = 5$ |
| CC | If $\epsilon_d \neq 0$ |
| CD | If $M_y = 5$ & $I_{xx} \neq 0$ |
| CE | If $D_p \neq 0$ for kth stage |
| CF | If $D_p \neq 0$ for kth stage |
| CG | If $D_p \neq 0$ for kth stage |
| CH | If $D_p \neq 0$ for kth stage |
| CI | If $F_y \neq 0$ |
| CJ | If $F_y = 5$ or 6 |

D If $h_E \neq -1$ or $h < h_E$
 DA If $D_{RN} \neq 0$ or $K_h \neq 0$ or $PL - DA \neq 0$
 DB If $(D_{RN} \neq 0)$ or $(My = 4$ or 5 and $Ty = 8, 9, 10$ or $11)$ or $(PL - DA \neq 0)$
 DC If $h_E \neq -1$ or $h < h_E$ and $My = 2$ or 5
 DD If $h_E \neq -1$ or $h < h_E$ and $My = 5$
 DE If $h_E \neq -1$ or $h < h_E$ and $S_{fz} \neq 0$
 DF If $h_E \neq -1$ or $h < h_E$ and $S_{fz} \neq 0$ and $My = 4$ or 5
 E If $My = 2$ or 5
 ED If $My = 5$
 EB If $My = 5$ and $I_{xx} \neq 0$
 F If $My = 2$ or 5
 FA If $My = 5$
 FB If $My = 2$ or 5
 FC If $My = 5$
 FD If $My = 5$ and $I_{xx} \neq 0$
 G If $t_{T1} \neq 0$
 GA If $t_{T1} \neq 0$ and $My = 4$ or 5
 GB If $PL - GB \neq 0$ or $Ty = 10$ or 11
 GC If $(PL - GB \neq 0$ or $Ty = 10$ or $11)$ and $My = 4$ or 5
 GD If $PL - GB \neq 0$ or $Ty = 10$ or 11
 GE If $(PL - GB \neq 0$ or $Ty = 10$ or $11)$ and $My = 4$ or 5
 IE If $Ty = 6$
 J If $K_{cl} < \sigma_e < K_{cr}$ or at the stage termination of final stage and the orbital criteria are satisfied.

| <u>Printline</u> | <u>Obtained</u> |
|------------------|---|
| J | If $K_{c1} < \sigma_c < K_{c2}$ or at the stage termination of final stage and the orbital criteria are satisfied. |
| JA | If $K_{c1} < \sigma_c < K_{c2}$ or at the stage termination of the final stage and the impact criteria are satisfied. |
| JB | If $K_{c1} < \sigma_c < K_{c2}$ or at the stage termination of the final stage and the impact criteria are satisfied and $h_E \neq 0$ |
| JC | If $K_{c1} < \sigma_c < K_{c2}$ or at the stage termination of the final stage and the impact or orbital criteria are satisfied. |
| K | If $PL - K \neq 0$ or $Ty = 4$ or $\sigma_{gg} \neq 0$ |
| KA | If $(PL - K \neq 0$ or $Ty = 0$ or $\sigma_{g1} \neq 0)$ and $My = 4$ or 5 |
| KB | If $PL - KB \neq 0$ or $Ty = 4$ or $\sigma_{g1} \neq 0$ |
| N | At stage termination or $PL - N \neq 0$ |
| O | At stage termination or $PL - O \neq 0$ |
| P | If $t_B = 0$ |
| PA | If $P_{arm} \neq 0$ or $P_{avc} \neq 0$ and if $t_B = 0$ |
| PB | If $P_{arm} \neq 0$ or $P_{arc} \neq 0$ and if $t_B = 0$ |

Output Print Format I

Main Print

| | | | | | | | | |
|----|----------------|------------------|---------------|---------------|---------------|------------|-------------------|-------|
| A | t | S | h | V_e | V_I | a_{xb} | M_y | T_y |
| | XXXX.XXXX | XXXXXXXXXX | XXXXXXXXXX | XXXXX.XXX | XXXXX.XXX | XXXX.XXXX | XX | XX |
| AA | S_s | S_c | ϕ | ζ | | | | |
| | XXXXXXXXXX | XXXXXXXXXX | XXXX.XXXX | XXXX.XXX | | | | |
| B | θ_m | $\dot{\theta}_m$ | α | γ_1 | γ_{1I} | a_{zb} | \dot{V}_e | |
| | XXXX.XXXX | XXXX.XXXX | XXXX.XXXX | XXXX.XXXX | XXXX.XXXX | XXXX.XXXX | XXXX.XX | |
| BA | ψ_m | $\dot{\psi}_m$ | β | γ_2 | γ_{2I} | a_{yb} | $\dot{\eta}_{pt}$ | |
| | XXXX.XXXX | XXXX.XXXX | XXXX.XXXX | XXXX.XXXX | XXXX.XXXX | XXXX.XXXX | XXXX.XXX | |
| BB | ϕ_m | $\dot{\phi}_m$ | P_m | Q_m | R_m | μ | ρ | |
| | XXXX.XXXX | XXXX.XXXX | XXXX.XXXX | XXXX.XXXX | XXXX.XXXX | XXXX.XXXX | XXXX.XXXX | |
| C | W | \dot{W} | F | F_V | $[F/\dot{W}]$ | F_x | η_{bn} | |
| | XXXXXXXXXX | XXXXXX.XX | XXXXXXXXXX | XXXXXXXXXX | XXXX.XXXX | XXXXXXXXXX | XXXX.XXX | |
| CA | \dot{I}_{YY} | M_{DQ} | M_{cQ} | M_{FCQ} | M_{JDQ} | F_{JDz} | M_{IQ} | |
| | XXXXXXXXXX | XXXXXXXXXX | XXXXXXXXXX | XXXXXXXXXX | XXXXXXXXXX | XXXXXXXXXX | XXXXXXXXXX | |
| CB | \dot{I}_{ZZ} | M_{DR} | M_{CR} | M_{FCR} | M_{JDC} | F_{JDy} | M_{IR} | |
| | XXXXXXXXXX | XXXXXXXXXX | XXXXXXXXXX | XXXXXXXXXX | XXXXXXXXXX | XXXXXXXXXX | XXXXXXXXXX | |
| CC | P_c | P_e | P^* | P_s | ϵ_s | | | |
| | XXXXXXXXXX.XX | XXXXXXXXXX.XX | XXXXXXXXXX.XX | XXXXXXXXXX.XX | XXXX.XXXX | | | |
| CD | \dot{I}_{xx} | M_{DP} | M_{CP} | M_{FCP} | M_{FVP} | M_{FOP} | M_{IP} | |
| | XXXXXXXXXX | XXXXXXXXXX | XXXXXXXXXX | XXXXXXXXXX | XXXXXXXXXX | XXXXXXXXXX | XXXXXXXXXX | |
| CE | r_b | D_b | g_{WI} | V_{C1} | A_{SI} | ϵ | C_{FI} | |
| | XX.XXXXXX | XXXX.XXXX | X.XXXXXX | XXXXXXXXXX | XXXXXXXXXX | XXXX.XXXX | X.XXXXXXX | |
| CF | \dot{P}_c | P_c | P_{cc} | F_{com} | F_{Vcom} | F_{VN} | F_N | |
| | +XXXXXXXXXX | XXXXX.XXX | XXXXX.XXX | XXXXXXXXXX | XXXXXXXXXX | XXXXXXXXXX | XXXXXXXXXX | |
| CG | \dot{A}_t | A_t | A_{tcc} | K_s | K_p | ω_p | | |
| | +XXXXXX.X | XXXX.XXXX | XXXX.XXXX | XXXX.XXXX | XXXX.XXXX | XXXX.XXXX | XXXX.XXXX | |
| CH | \dot{W}_{MP} | W_{pr} | g_{PI} | A_{xI} | | | | |
| | XXXXXXXXXX | XXXXXXXXXX | X.XXXXXX | XXXX.XXXX | | | | |

OUTPUT PRINT FORMAT I

MAIN PRINT

| | \hat{F}_c | K_{cv} | V_{XXX} | \dot{V}_{XXX} | K_{XXX} | |
|----|-------------|-------------|-----------|-----------------|-------------|-------------|
| CI | XXXXXXXXX. | XXXX.XXXX | XXXXX.XXX | OXXXX.XX | XXXX.XXXX | |
| | F_{cqmin} | F_{cqmax} | K_{cq} | V_{ecq} | F_{cALOS} | F_{cclos} |
| CJ | XXXXXXXXX. | XXXXXXXXXX. | XXXX.XXXX | OXXXX.XX | XXXXX.XXX. | XXXXXXXXXX. |

where:

$$V_{XXX} = \begin{cases} V_{ecv} & \text{If } F_y = 1 \\ V_{ecm} & \text{If } F_y = 2 \\ V_{cv} & \text{If } F_y = 4 \\ 0 & \text{Otherwise} \end{cases}$$

$$\dot{V}_{XXX} = \begin{cases} \dot{V}_{ecv} & \text{If } F_y = 1 \\ \dot{V}_{ecm} & \text{If } F_y = 2 \\ 0 & \text{Otherwise} \end{cases}$$

$$K_{XXX} = \begin{cases} K_{CPR} & \text{If } F_y = 3 \\ K_{ALOS} & \text{If } F_y = 6 \\ 0 & \text{Otherwise} \end{cases}$$

| | | | | | | | |
|----|-------------------|-----------------|------------------|-------------------|------------------|-------------|-------------|
| | M | q | V _a | C | N _Z | q α' | Pa |
| D | XX.XXXXX | XXXXX.XX | XXXXXX.XX | XXXXXX.XX | XXXXXXXXXX | XXXXXX.X | XXXX.XX |
| | $\dot{\alpha}$ | $\ddot{\alpha}$ | $\ddot{\alpha}$ | α' | \dot{v}_w | v_w | \dot{v}_w |
| DA | XXXXX.XXX | XXXX.XXXX | XXXX.XXXX | XXXX.XXXX | XX.XXXXX | XXXX.XXX | XXXXX.XXX |
| | $\dot{\beta}$ | $\ddot{\beta}$ | $\ddot{\beta}$ | $\ddot{\alpha}'$ | ϵ | ϕ | ϕ_c |
| DB | XXXXX.XXX | XXXX.XXXX | XXXX.XXXX | XXXX.XXXX | XX.XXXXX | XXXX.XXX | XXXX.XXX |
| | x_{cp} | M_{NQ} | l_{cp} | M_{NSQ} | M_{CZG} | M_{NDQ} | N_{Pz} |
| DC | XXXXX.XXX | XXXXXXXX. | XXXX.XXXX | XXXXXXXXXX. | XXXXXXXXXX. | XXXXXXXXXX. | XXXXXXXXXX. |
| | M_{NP} | M_{NR} | N_r | M_{NSR} | M_{CYG} | M_{NDR} | N_{Py} |
| DD | XXXXXXXX. | XXXXXXXX. | XXXXXX. | XXXXXXXXXX. | XXXXXXXX. | XXXXXXXXXX. | XXXXXXXXXX. |
| | $M_{\delta Q}$ | $l_{\delta z}$ | $N_{\delta z}$ | $C_{\delta z}$ | M_{hz} | l_{hz} | U_{cz} |
| DE | XXXXXXXXXX. | XXXXX.XXX | XXXXXXXXXX. | XXXXXX.XX | XXXXXXXXXX. | XXXXX.XXX | XXXXXX. |
| | $M_{\delta R}$ | $l_{\delta y}$ | $N_{\delta y}$ | M_{hy} | | | |
| DF | XXXXXXXXXX. | XXXXX.XXX | XXXXXXXXXX. | XXXXXXXXXX. | | | |
| | I_{YY} | z_e | x_{cg} | z_{cg} | θ_b | Q_b | \dot{Q}_b |
| E | XXXXXXXXXX. | XX.XXXX | XXXX.XXXX | XXXX.XXXX | XXXX.XXXX | XX.XXXX | XXXX.XXXX |
| | I_{ZZ} | y_e | y_{cg} | \dot{v}_b | R_b | \dot{R}_b | |
| EA | XXXXXXXXXX. | XXXX.XXXX | XXXX.XXXX | XXXX.XXXX | XX.XXXX | XXXX.XXX | |
| | I_{XX} | \dot{c}_b | \ddot{c}_b | P_b | \dot{P}_b | M_{RAP} | |
| EB | XXXXXXXXXX. | XX.XXXXX | XXXX.XXXX | XX.XXXX | XXXX.XXX | XXXXXXXXXX. | |
| | δ_{Pc} | δ_P | $\dot{\delta}_P$ | $\ddot{\delta}_P$ | F_z | K_{DP} | K_{RP} |
| F | XX.XXXXX | XX.XXXXX | XXXX.XXXXX | XXXXXX.XX | XXXXXX.XX | XXXX.XXX | XX.XXXX |
| | δ_{Yc} | δ_Y | $\dot{\delta}_Y$ | $\ddot{\delta}_Y$ | F_y | K_{DY} | K_{RY} |
| FA | XX.XXXXX | XX.XXXXX | XXXX.XXXXX | XXXXXX.XX | XXXXXX.XX | XXXX.XXX | XX.XXXX |
| | $\ddot{\delta}_P$ | I_P | $I_{\delta P}$ | M_{FOQ} | $\Delta\theta_b$ | M_{TDQ} | F_{TDz} |
| FB | XX.XXXXX | XXXXXXXXXX. | XXXXXX.XX | XXXXXXXXXX. | XX.XXXX | XXXXXXXXXX. | XXXXXX. |
| | $\ddot{\delta}_Y$ | I_Y | $I_{\delta Y}$ | M_{FOQ} | $\Delta\theta_b$ | M_{TDR} | F_{TDy} |
| FC | XX.XXXXX | XXXXXXXXXX. | XXXXXX.XX | XXXXXXXXXX. | XXXX.XXXX | XXXXXXXXXX. | XXXXXX. |
| | F_c | I_R | F_D | $\Delta\phi_b$ | F_R | \dot{F}_R | \dot{W}_R |
| FD | XXXXXX.X | XXXXXXXXXX | XX.XXXXX | XXXX.XXXX | XXXXXX.X | XXXXXX.XX | XXXXXX.X |
| | t_T | S_T | h_T | V_T | γ_T | a_{TT} | a_{TN} |
| G | XXXX.XXXX | XXXXXXXXXX. | XXXXXX. | XXXX.XXX | XX.XXXX | XX.XXXX | XX.XXXX |
| | S_{TC} | γ_M | $\dot{\gamma}_M$ | l_T | a_{TC} | | |
| GA | XXXXXXXXXX. | XXXX.XXXXX | XXXXXX.XXX | XX.XXXXX | XX.XXXXX | | |

| | | | | | | |
|----|-----------|-------------|-------------|-------------|-----------|-----------|
| | t_{MI} | s_{MI} | h_{MI} | r_{MI} | q_{MI} | e_{MI} |
| GB | XXXX.XXXX | XXXXXXXXXX. | XXXXXXXXXX. | XXXXXXXXXX. | XXXX.XXXX | XXXX.XXXX |

| | | | | |
|----|------------|------------|-----------|-----------|
| | s_{CMI} | e_{MI}^* | t_{MI} | q_{MI} |
| GC | XXXXXXXXX. | XXXX.XXX | XXXX.XXXX | XXXX.XXXX |

| | | | | | | |
|----|-----------|----------------|----------------|-----------|-----------|----------------|
| | e_{MT} | \dot{e}_{MT} | \dot{r}_{MT} | r_{MT} | q_{MT} | \dot{q}_{MT} |
| GD | XXXX.XXXX | XXXXX.XXXX | XXXXXX.XX | XXXXXXXX. | XXXX.XXXX | XXXXX.XXXXXX |

| | | | | |
|----|---------------|---------------------|----------------|----------------------|
| | δ_{MT} | $\dot{\delta}_{MT}$ | λ_{MT} | $\dot{\lambda}_{MT}$ |
| GE | XXXX.XXXX | XXXXX.XXXX | XXXX.XXXX | XXXXX.XXXXXX |

| | |
|----|---------------|
| | l_{r} |
| IE | OX.XXXXXXEOXX |

| | | | | | | | |
|---|-----------|-----------|-----------|-----------|-----------|--------------|-----------|
| | e | n_p | h_a | i | t_a | $\phi_{a/4}$ | P |
| J | XXX.XXXXX | XXXXX.XXX | XXXXX.XXX | XXX.XXXXX | XXXXXX.XX | XXXXX.XXXX | XXXX.XXXX |

| | | | | | | | |
|----|-----------|-----------|-----------|-----------|-----------|----------------|----------------|
| | t_f | s_f | μ_f | ρ_f | v_{If} | γ_{1If} | γ_{2If} |
| JA | XXXXX.XXX | XXXXX.XXX | XXXX.XXXX | OX.XXXXXX | XXXXXX.XX | OX.XXXXXX | XXX.XXXX |

| | | | | | | | |
|----|-----------|-----------|-----------|---------------|-----------|----------------|----------------|
| | t_E | s_E | v_{aE} | γ_{IE} | v_{IF} | γ_{1IE} | γ_{2IE} |
| JB | XXXXX.XXX | XXXXX.XXX | XXXXXX.XX | OX.XXXXXX | XXXXXX.XX | OX.XXXXXX | XXX.XXXX |

| | | | | | |
|----|-----------|----------------|-----------|-----------|----------|
| | s_a | γ_{2Ia} | μ_a | ρ_a | v_{Ia} |
| JC | XXXXXX.XX | XXX.XXXXX | XXXX.XXXX | XXXX.XXXX | XXXXX.XX |

| | | | | | | |
|---|-------------|----------------|-----------------|-------------|----------------|-----------------|
| | x_{ee} | \dot{x}_{ee} | \ddot{x}_{ee} | z_{ee} | \dot{z}_{ee} | \ddot{z}_{ee} |
| K | XXXXXXXXXX. | XXXXXX.XX | XXXXX.XXX | XXXXXXXXXX. | XXXXXX.XX | XXXXX.XXX |

| | | | | | | |
|----|-------------|----------------|-----------------|-------------|----------------|-----------------|
| | y_{ee} | \dot{y}_{ee} | \ddot{y}_{ee} | y_{gg} | \dot{y}_{gg} | \ddot{y}_{gg} |
| KA | XXXXXXXXXX. | XXXXXX.XX | XXXXX.XXX | XXXXXXXXXX. | XXXXXX.XX | XXXXX.XXX |

| | | | | | | |
|----|-------------|----------------|-----------------|-------------|----------------|-----------------|
| | x_{gg} | \dot{x}_{gg} | \ddot{x}_{gg} | z_{gg} | \dot{z}_{gg} | \ddot{z}_{gg} |
| KB | XXXXXXXXXX. | XXXXXX.XX | XXXXX.XXX | XXXXXXXXXX. | XXXXXX.XX | XXXXX.XXX |

| | | | | | | |
|---|-----------|-----------|-----------|-----------|------------|---------|
| | L_F | L_D | L_g | L_v | Δv | E/M |
| N | XXXXXX.XX | XXXXXX.XX | XXXXXX.XX | XXXXXX.XX | XXXXXX.XX | XXXXXX. |

| | | | |
|---|----------------|----------------|----------------|
| | I | I_v | H_e |
| O | OX.XXXXXXXEOXX | OX.XXXXXXXEOXX | OX.XXXXXXXEOXX |

| | | | | | |
|---|----------------|---------------|----------------|----------------|----------------|
| | K_{FM}^* | K_{FC}^* | I_{vT} | I_{vM} | I_{vC} |
| P | OX.XXXXXXXEOXX | OX.XXXXXXXEOX | OX.XXXXXXXEOXX | OX.XXXXXXXEOXX | OX.XXXXXXXEOXX |

| | | | | | |
|----|----------------|----------------|----------------|----------------|----------------|
| | I_{FM} | I_{FC} | \hat{I}_{vT} | \hat{I}_{vM} | \hat{I}_{vC} |
| PA | OX.XXXXXXXEOXX | OX.XXXXXXXEOXX | OX.XXXXXXXEOXX | OX.XXXXXXXEOXX | OX.XXXXXXXEOXX |

| | | | | | |
|----|-------------|-------------|----------------|----------------|----------------|
| | I_{spM} | I_{spC} | I_{vT}^* | I_{vM}^* | I_{vC}^* |
| PB | XXXXX.XXXXX | XXXXX.XXXXX | OX.XXXXXXXEOXX | OX.XXXXXXXEOXX | OX.XXXXXXXEOXX |

(3) Hunt Print

Procedure 1

If P_1 is non-zero, the printline Y is printed at trajectory termination. If the input flag K_g is non-zero, the stipulated main print is output, i.e., as described for P_1 equal P_2 equal zero, for each trajectory run during this hunting procedure. The title for this hunt print is set at "ITERATION" and the number of iteration is output as n_i .

After convergence occurs the trajectory is printed as described for P_1 equal to P_2 equal zero.

Procedure 2

If P_2 is non-zero, printlines YA through YD are printed at end of each trajectory iteration. The hunt print printout continues until procedure 2 convergence occurs, then the trajectory is printed as described for P_1 equal P_2 equal zero. The hunt print title should be "ARRAY", "BASE CASE", or "ITERATION" for the indicated run. The number of trajectory runs is output as n .

(4) Auxiliary Print

Printlines Z, ZA (if σ_{p5} , σ_{p6} , σ_{p7} , or σ_{p8} is non-zero), and ZB (if σ_{p9} , σ_{p10} , or σ_{p11} is non-zero) when the auxiliary printline criteria of paragraph K.3.d are satisfied.

(5) Steering Coefficients Print

If $\sigma_{g1} > 0$ and $n_g > 5$, then the steering coefficients print is printed after the note "TERMINATION OF STAGE k" and before the note "MAXIMUM VALUES".

If $\sigma_{g1} > 0$ and $n_g < 5$, the note "STEERING COEFFICIENTS NOT CALCULATED" is printed after the note "TERMINATION OF STAGE k" and before the note "MAXIMUM VALUES".

OUTPUT PRINT FORMAT I (Continued)

Hunt Print

| | n_i | title |
|------------|---------------|---------------|
| HUNT PRINT | XXX | HHHHHHHHH |
| | X | a |
| Y | OX.XXXXXXXXXX | OX.XXXXXXXXXX |
| | x_1 | x_2 |
| YA | OX.XXXXXXXXXX | OX.XXXXXXXXXX |
| | x_3 | x_4 |
| | x_5 | x_6 |
| YB | OX.XXXXXXXXXX | OX.XXXXXXXXXX |
| | x_7 | |
| | Z | z_1 |
| YC | OX.XXXXXXXXXX | OX.XXXXXXXXXX |
| | z_2 | z_3 |
| | z_4 | z_5 |
| YD | OX.XXXXXXXXXX | OX.XXXXXXXXXX |
| | z_6 | z_7 |
| | | |

Auxiliary Print

| | t | σ_{P1} | σ_{P2} | σ_{P3} | σ_{P4} |
|----|---------------|----------------|----------------|---------------|---------------|
| Z | XXXX.XXXX | OX.XXXXXXXXXX | OX.XXXXXXXXXX | OX.XXXXXXXXXX | OX.XXXXXXXXXX |
| | σ_{P5} | σ_{P6} | σ_{P7} | σ_{P8} | |
| ZA | OX.XXXXXXXXXX | OX.XXXXXXXXXX | OX.XXXXXXXXXX | OX.XXXXXXXXXX | |
| | σ_{P9} | σ_{P10} | σ_{P11} | | |
| ZB | OX.XXXXXXXXXX | OX.XXXXXXXXXX | OX.XXXXXXXXXX | | |

Steering Coefficient Print

STEERING COEFFICIENTS

| | a_0 | a_1 |
|----|---------------|---------------|
| X | OX.XXXXXXXXXX | OX.XXXXXXXXXX |
| | b_1 | b_2 |
| XA | OX.XXXXXXXXXX | OX.XXXXXXXXXX |
| | b_3 | n_g |
| | OX.XXXXXXXXXX | XXXX. |

Maximum Print

MAXIMUM VALUES

| | t | σ_{mj} (value) | σ_{mj} (code) | T_{mi} |
|---|-----------|-----------------------|----------------------|----------|
| V | XXXX.XXXX | OX.XXXXXXXXXX | XXXX | OX |

(6) Maximum Print

If $\sigma_{mj} \neq T_{mj} = k_k$, or $T_{mj} = 1$ with $k_k = 4$, the maximum print (printline V) including the note "MAXIMUM VALUE" is printed after the steering coefficients print of the k-th stage.

(7) Optional Titled Output

If K_{TPF} the titled print flag input in L683 is non-zero the following format is printed at the top of each page of the output print format I.

BD XXX. RR XX. RUN XXX.

T CARD TITLE MESSAGE IS PRINTED ON THIS LINE

| | | | | | | | |
|---|-------------------|---------------------|-----------------------|-------------------------|----------------------------|-----------------|---------------------------|
| A | TIME | GROUND RANGE | GEOMETRIC ALTITUDE | EARTH VELOCITY | INERTIAL VELOCITY | AXIAL ACCEL | MODE TYPE |
| B | ATTITUDE ANGLE | ATTITUDE RATE | ATTACK ANGLE | FLIGHT PATH ANGLE | INERTIAL FLIGHT PATH | TRANS ACCEL | EARTH VELOCITY RATE |
| C | WEIGHT | WEIGHT FLOW | TOTAL THRUST | VACUUM THRUST | SPECIFIC IMPULSE | AXIAL THRUST | VEHICLE LOAD FACTOR |
| D | MACH NUMBER | DYNAMIC PRESSURE | AIR VELOCITY | AXIAL FORCE | NORMAL FORCE | Q ALPHA | AMBIENT PRESSURE |

b.

Format II Output Print

Format II output print is given following the entire Format I output print defined in section N1. The printline block in the duty cycle print is sequenced to present general duty cycle parameters first, then the time dependent duty cycle parameters. The duty cycle print arrangement is pictured in this section.

(1)

Duty Cycle Print

If K_{DC} is non-zero, the duty cycle print for the " K_{DC} "-th stage shall be given following the flexible body print.

OUTPUT PRINT FORMAT II

DUTY CYCLE PRINT

| | | | | | |
|----|-------------------|----------------------|-----------------|-----------------|------------------|
| | \bar{I} | \bar{I}_v | x_e | x_{nf} | δ_{me} |
| | I-DEL | I-VAC | X-E | X-NF | D-DESIGN |
| WA | OX.XXXXXXXXXXEOXX | OX XXXXXXXXEOXX | OXOXO.XXOX | OXOXO.XXOX | OXO.XXOX |
| | I_{spm} | $h_{q\alpha}$ | $p_{q\alpha}$ | ω_c | $\bar{\delta}_s$ |
| | ISP-VACM | H-Q ALPHA | P-Q ALPHA | CONT FREQ | SLEW |
| WB | OXOXO.XXOX | OXOXOXOX | OXOXO.XXOX | OXOXO.XXOX | OXO.XXOX |
| | \bar{I}_p | $\bar{I}_{\delta p}$ | $t_{\eta p}$ | \bar{p} | δ_{pmax} |
| | I-P | I-DDOTP | T-NP | ETA-P | DDOT-PMAX |
| WC | OX.XOXOXOXOXEOXX | OXOXOX.XX | OXOXO.XXOX | OX.XXOXOX | OXOXO.XXOX |
| | \bar{I}_y | $\bar{I}_{\delta y}$ | t_{-y} | η_y | δ_{ymax} |
| | I-Y | I-DDOTP | T-NY | ETA-Y | DDOT-YMAX |
| WD | OX.XOXOXOXOXEOXX | OXOXOX.XX | OXOXO.XXOX | OX.XXOXOX | OXOXO.XXOX |
| | $q'_{\alpha max}$ | $q'_{q\alpha}$ | $t_{q\alpha}$ | C_{noq} | $M'_{q\alpha}$ |
| | Q-ALPHA | Q-Q ALPHA | T-Q ALPHA | NORM COEF | MACH Q A |
| WE | OXOXOXOX.XX | OXOXOX.XX | OXOXO.XXOX | OX.XXOXOX | OXO.XXOX |
| | K_{dc} | D_B | A_{FW1} | t_{Ba} | F_{vave} |
| | STG | CASE DIA | VZH VTHR/WT | STG TIME | STG VAC THRUST |
| WF | X OXOXO.XXOX | OXOXO.XXOX | OXOXO.XXOX | OX.XXOXOXOXEOXX | OX.XXOXOXOXEOXX |
| | R_{PFV} | \bar{z}_d | \bar{A}_t | α'_d | P_{ce} |
| | PC/FMV | EXP RAT | AT | GAMMA | PCA |
| WG | OX.XXOXOXOXEOXX | OXOXO.XXOX | OXOXO.XXOX | OX.XXOXOX | OXOXO.XXOX |
| | W_{TVG} | W_{exi} | I_{spavg} | P_{cmax} | |
| | WTVC | W-EXI | ISP-AVG | PC-MAX | |
| WH | OX.XXOXOXOXEOXX | OX.XXOXOXOXEOXX | OX.XXOXOXOXEOXX | OX.XXOXOXOXEOXX | |
| | n_m | n_c | n_{dc} | M_{fzmax} | M_{hymax} |
| | H-D | N-C | N-DC | M-HINGE-F | M-HINGE-Y |
| WI | XXX | XXX | XXX | OX.XXOXOXOXEOXX | OX.XXOXOXOXEOXX |
| | I_{YN} | W_{MO} | K_{CH} | | |
| | INT-MAIN | WGT-MAIN | XT-MAIN | | |
| WJ | OX.XXOXOXOXEOXX | OX.XXOXOXOXEOXX | OX.XXOXOXOXEOXX | | |

| | | | | | | |
|----|------------------|----------------|------------------|--------------|------------|------------------|
| | \dot{A}_{tmax} | I_{at} | A_{xmax} | | | |
| | ADTMAX | IAT | AXMAX | | | |
| WK | +0.XXXXXXXEDXX | +0.XXXXXXXEDXX | +XXXXX.XXXX | | | |
| | F_{max} | P_{cmax} | ϵ_{max} | A_{tmin} | C_{fmax} | |
| | FMAX | PCMAX | EPSMAX | ATMIN | CFMAX | |
| WL | +XXXXXXXXXX.XX | +XXXXXX.XXXX | +XXXXX.XXXX | +XXXXXX.XXXX | +X.XXXXXXX | |
| | F_{min} | P_{cmin} | ϵ_{min} | A_{tmax} | C_{fmin} | |
| | FMIN | PCMIN | EPSMIN | ATMAX | CFMIN | |
| WM | +XXXXXXXXXX.XX | +XXXXXX.XXXX | +XXXXX.XXXX | +XXXXXX.XXXX | +X.XXXXXXX | |
| | t_{Bq} | δ_{pq} | δyq | F_q | X_{cgq} | \bar{p}_{vacq} |
| | TIME | D-PITCH | D-YAW | F-JEL | X-CG | F-VAC |
| WO | XXXX.XXX | OX.XXXXX | OX.XXXXX | XXXXXXXX.X | XXXX.XXXXX | XXXXXXXX.X |
| | . | . | . | . | . | . |
| | . | . | . | . | . | . |
| WO | XXXX.XXX | OX.XXXXX | OX.XXXXX | XXXXXXXX.X | XXXX.XXXXX | XXXXXXXX.X |
| | . | . | . | . | . | . |
| | . | . | . | . | . | . |

(2)

Error Code

Certain computations and parameter values result in program logic terminating the run. The error which causes the abort is identified by printout. The printout occurs after the main print is given for the trajectory computation up to the time of error.

(a)

Common Error

Verbal descriptions of common errors are as follows:

1. *Undefined type of flight - check input L310, L317, etc.
2. *Undefined mode - check input L600, L603, etc.
3. Undefined type of hunt - check input L84
4. Invalid sigma Z or Y - check input L85, L94, L103, etc
5. Invalid sigma Y - check input L77
6. Input card error
7. Dependent parameter not varying - Hunt Procedure one
8. Impossible region exist - Hunt Procedure one
9. Singularity in quadratic fit - Hunt Procedure one
10. Delta X input zero - check L81
11. Internal tolerance input zero - check L83
12. Invalid sigma A - check input L78
13. *The missile weight has gone to zero - dump follows

*These messages are followed by a formatted dump

(b) Integration Routine Errors

In the event of an integration routine error, the following information is provided:

INTEGRATION ERROR TYPE X

Type 1 indicates the initial integration interval is too small; this error should seldom occur.

Type 2 indicates the CNTRL or MAXPRT routine has cut the interval too far in attempting to meet accuracy criteria.

Type 3 indicates the integration routine has cut the interval too far.

The minimum allowable interval is $2(t+1) \times 10^{-8}$.

AT TIME = XXXX - the time of the failure

DELT = XXXX - the integration interval

CONTROL COUNTER. XXXX- the number of passes through the CNTRL routine; i.e., the number of time intervals integrated. Zero here indicates the trajectory cannot get started for some reason.

BREAKUP COUNTER. XXXX- The number of passes through the CNTRL routine in attempting the most recent breakup. An integer here and error type 2 indicates trouble with one or more of the following:

1. Attitude control Table
2. Gains Table
3. Special Print Table
4. Weight Jettison Table
5. Wind Profile Table
6. Mode Control Table
7. Staging
8. Target Dynamical Conditions Table
9. Lift off
10. Thrust Modulation Control Table

MAXPRT COUNTER XXXX- The number of passes through the MAXPRT routine; a positive integer here and error type 2 indicates trouble finding a maximum print value. A value of -1 indicates no maximum prints have been requested.

INTEGRATION COUNTER XXXX- The number of times the integration interval has been cut. A positive integer here and error type 3 indicates trouble in maintaining integration accuracy.

TIME (START) - Time at call to integration routine

DELT (START)-Initial integration interval.

EMAX-- Maximum value of E_i

JMAX - Index i of E_i

Following the above there is a table of 5 columns of 50 items each, labeled Y (start), HK1, HK3, HK4, .nc. Y (start) is just that, and HK1, HK3, and HK4 are the h_1 , h_3 , and h_4 of the Range-Kutser-Menson integration method (k_2 is not saved and k_5 can be found as D_y in locations 751-800 of the P-region). INC is a logical variable indicating whether the particular equation is included in the integration vector. This information is of use only with type 3 errors.

(c)

Formatted Dump

Certain error conditions cause the trajectory to terminate with a formatted dump consisting of the following sections:

P REGION (1000 locations) - this is the section described in switching code; i.e., the output variables identified by L5000-L5999.

GN REGION (100 locations) - this area contains real variables and constants.

JN REGION (100 locations) - this area contains integer variables, constants, counters and flags.

LG REGION (100 locations) - this area contains logical flags

WGT TABLES (150 locations) - this is the WGTBLS common region. It contains supplemental main and complementary thrust-weight tables, each of which are 3×25 arrays. The table entries are the derivative of thrust, second derivative of weight, and weight.

STAGE TABLES (75 locations) - this is a 15×5 array, containing 15 values each of XOLD, XTEMP, XTARG, DET, and BRKTM. These values are used by the routines CNTRL and BKKPS to perform breakups. $XOLD_i$ is the past value of variable i , $XTEMP_i$ is the most recent value and $XTARG_i$ is the target value. DET_i is either the estimated time to achieve $XTARG_i$, or -10^8 if $XTARG_i$ has been achieved. $BRKTM_i$ is the time a previous breakup occurred and is used whenever MAXPRT requires repeated passes over the same interval to locate and extremal. The i index relates the type of breakup involved, as follows:

- $i =$ 1. Attitude (flight) Control Table
 - 2. Gains (TVC) Table
 - 3. Weight Jettison Table
 - 4. Special Print Table
 - 5. Wind Profile Table
 - 6. Mode Control Table
 - 7. Staging
 - 8. Target Dynamical Conditions Table
 - 9. Liftoff
 - 10. Thrust Modulation Control Table
- The remaining locations ($i = 9-15$) are not used.

STAGE FLAGS (30 locations) - this is a 15×2 array of integers; 15 values each of LMP and KDP. These are used with the values above. LMP_i is the L-number, less 5000, of the variable X_i ; for example, $LMP = 0$ means a breakup on the variable t , or $LMP = 270$ means a breakup on α . KDP_i is the L-number that identifies the breakup; for example, $KDP = 31$ means that the

breakup of the second line of the attitude control table was in progress. $KDP = 0$ means that breakup point has not yet been found. The index i is as above. A negative value for LMP_i indicates the corresponding table is not involved in the breakup process.

TVC REGION (800 locations) - this is an array of 100×8 , consisting of 100 each of the values printed on line W0, followed by the values printed on lines WA through WJ of the Duty Cycle Print.

(d) Simultaneous Hunt Errors

The following message is output if the hunting procedure 2 fails:

ERROR HAS OCCURRED IN OPTM2 ROUTINE - DUMP FOLLOWS

c.

Trajectory Shaper Output Print

The following output format is used in presenting the trajectory Shaper parameters

(OUTPUT FORMAT)

TRAJECTORY SHAPER SUBROUTINE

INPUT

CONTROL FLAG

L598 X^{sh} DIM HH

TARGET CONDITION

L599 OXXXXXX.XX NM Message 2 Delete if K_{sh} = 1
 HHHHHHHHHHHHHHHHHH

OUTPUT

| NO STG. | INITIAL VEL. | INITIAL ALT. | EARTH. ROTATION |
|----------------|--------------|--------------|-----------------|
| , DIM | , FT/SEC | , FT | , DIM |
| N_k | V_{so} | h_o | \tilde{u}/u |
| X ^k | 0XXXXX.XXX | 0XXXXXX.XXX | 0X.XXXXXXXX |

| | STAGE I | STAGE II | STAGE III | STAGE IV |
|--------------|-------------------|-------------------|-------------------|-------------------|
| ACTION TIME | t_{B1} | t_{B2} | t_{B3} | t_{B4} |
| , SEC | I_{VT1} | I_{VT2} | I_{VT3} | I_{VT4} |
| VAC. IMPULSE | I_{speff1} | I_{speff2} | I_{speff3} | I_{speff4} |
| , LB-SEC | Δ_{W1} | Δ_{W2} | Δ_{W3} | Δ_{W4} |
| EXP. WEIGHT | W_{B1} | W_{B2} | W_{B3} | W_{B4} |
| , LB | $\Delta_{WL/WB1}$ | $\Delta_{W2/WB2}$ | $\Delta_{W3/WB3}$ | $\Delta_{W4/WB3}$ |
| STG. WEIGHT | $W_{B1/WB1}$ | $W_{B2/WBL}$ | $W_{B3/WB1}$ | $W_{B4/WB1}$ |
| , LB | W_{PLO1} | W_{PLO2} | W_{PLO3} | W_{PLO4} |
| STG. MASS | | | | |
| FRACT.. DIM | | | | |
| STG. RATIO | | | | |
| . DIM | | | | |
| PROPULSION | | | | |
| WEIGHT, LB | | | | |

IDEAL VELOCITY
, FT/SEC

ΔV
 OXXXXXX,XXX
 PITCH OVER
 ANGLE, DEG
 012
 OXXX.XXXXXX

CIRCULAR ORBITAL
VELOCITY FT SEC
VICO
OXXXXXX.XXX

PAYLOAD WEIGHT
LB

WPL
OXXXXXXXXX.XXXX
PITCH OVER ANGULAR
RATE, DEG/SEC
Qu2
OXXXXX XXXXXX

TERMINAL STAGE IGNITION
FLIGHT PATH ANGLE, DEG
γ IT
0XX.XXXXXX

VEHICLE LIFTOFF
WEIGHT, LB

WT
OXXXXXXX.XXXX
VEHICLE VELOCITY AT
PITCH OVER, FT SEC
Veo
OXXXX.XXXXXX

CIRCULAR ORBITAL
ALTITUDE, FT
hco
OXXXXVXXX.XXX

Delete
if
Kshl # 3

Message 1

MAXIMIZE RANGE WITH GIVEN PAYLOAD

If $K_{sh} = 1$

MAXIMIZE PAYLOAD TO A GIVEN RANGE

If $K_{sh} = 2$

DETERMINE PAYLOAD TO A CIRCULAR ORBIT

If $K_{sh} = 3$

Message 2

TARGET RANGE

If $K_{sh} = 2$

ORBITAL ALTITUDE

If $K_{sh} = 3$

SECTION IV

ROLL CONTROL REQUIREMENTS

The roll control requirements are determined from estimates of the roll disturbing moments: the offset roll torque, the vortex roll torque, and the aerodynamic roll torque. The offset roll torque is caused by the transverse thrust vector and the distance between the TVC vector point and the offset center-of-gravity centerline. The vortex roll torque is caused by the spiralling exhaust gases leaving the nozzle. The aerodynamic roll torque is caused by the coupled aerodynamic normal force and the distance between the aerodynamic center of pressure and missile center-of-gravity centerline offsets.

A. LINKAGE WITH TRAJECTORY ROUTINE

The roll control requirement routine can operate with data from the trajectory output duty cycle or can operate independently of the trajectory program by inputting mandatory data. Options are available to input variables and constants or have them calculated internally.

The logic to use data from the TVC duty cycle is as follows.

1. If the mandatory data are not input, i.e., K_k , D_B , F_{vac} , W_0 , or F_{vac}/W_0 , then data on print-line WF of the TVC duty cycle are used.
2. If the control flag K_{tr} is nonzero, the parameters C_{Nq} , $q\alpha'_m$, and δ'_{mx} are obtained from the TVC duty cycle parameter C_{Nq} , $q\alpha'_{max}$, and $\bar{\delta}_{pmax}$, respectively.

B. PROGRAM INSTRUCTIONS

1. ROLL TORQUE

$$M_{rtk} = \begin{cases} M'_{rtk} & \text{if } M'_{rtk} \text{ is input} \\ (M_{osk}^2 + M_{vrk}^2 + M_{ark}^2)^{\frac{1}{2}} & \text{otherwise} \end{cases} \quad (\text{in-lbf})$$

Where M'_{rtk} is the input roll torque (in-lbf), M_{osk} is the offset roll torque (in-lbf), M_{vrk} is the vortex roll torque (in-lbf) and M_{ark} is the aerodynamic roll torque (in-lbf).

a. Offset Roll Torque

$$M_{osk} = \begin{cases} 0 & \text{if } M'_{rtk} \text{ is input} \\ M'_{osk} & \text{if } M'_{osk} \text{ is input} \\ K_{osk} (\pi/180) F_{vack} \delta_{mxk} \epsilon_{osk} & \text{otherwise} \end{cases} \quad (\text{in-lbf})$$

Where M'_{osk} is the input offset roll torque (in-lbf), K_{osk} is the offset roll torque multiplier, F_{vack} is the input average webtime vacuum thrust (lbf), δ_{mxk} is the maximum thrust vector deflection angle (deg) and ϵ_{osk} is the effective offset distance (in).

(1) Offset Roll Torque Multiplier

$$K_{osk} = \begin{cases} K'_{osk} & \text{if } K'_{osk} \text{ is the input} \\ 1.0 & \text{otherwise} \end{cases} \quad (\text{dim})$$

Where K'_{osk} is the input offset torque multiplier (dim)

b. Vortex Roll Torque

$$M_{vrk} = \begin{cases} 0 & \text{if } M'_{rtk} \text{ is input} \\ M'_{vrk} & \text{if } M'_{vrk} \text{ is input} \\ K_{vrk} \eta_{vrk} F_{vack} & \text{otherwise} \end{cases} \quad (\text{in-lbf})$$

Where K_{vrk} is the vortex roll torque multiplier (dim), η_{vrk} is the vortex roll torque per pound of thrust factor (in).

(1) Vortex Roll Torque Multiplier

$$K_{vrk} = \begin{cases} K'_{vrk} & \text{if } K'_{vrk} \text{ is input} \\ 1.0 & \text{otherwise} \end{cases} \quad (\text{dim.})$$

Where K'_{vrk} is the input vortex roll torque multiplier (dim.)

(2) Vortex Roll Torque Per Pound of Thrust Factor

$$\eta_{vrk} = \begin{cases} \eta'_{vrk} & \text{if } \eta'_{vrk} \text{ is input} \\ 0.00363 & \text{otherwise} \end{cases} \quad (\text{in})$$

Where η'_{vrk} is the input vortex roll torque per pound of thrust factor (in)

(3) Maximum Deflection Angle

$$\delta_{mxk} = \begin{cases} \delta'_{mxk} & \text{if } \delta'_{mxk} \text{ is input} \\ K_{\delta mk} [B_{\delta 0k} + B_{\delta 1k} (\ln W_{ok}) + B_{\delta 2k} (\ln W_{ok})^2] & \text{otherwise} \end{cases} \quad (\text{deg})$$

Where

Stage I

$$B_{\delta 01} = 15.729698$$

$$B_{\delta 11} = -1.5695603$$

$$B_{\delta 21} = 0.046411178$$

$$K_{\delta m1} = 1.0$$

Stage II

$$B_{\delta 02} = 10.480564$$

$$B_{\delta 12} = -1.072774$$

$$B_{\delta 22} = 0.032548762$$

$$K_{\delta m2} = 1.0$$

Stage III

$$B_{\delta 03} = 5.7204757$$

$$B_{\delta 13} = -0.58573616$$

$$B_{\delta 23} = 0.018170142$$

$$K_{\delta m3} = 1.0$$

Stage IV

$$B_{04} = 5.7204757$$

$$B_{014} = -0.58573616$$

$$B_{024} = 0.018170142$$

$$K_{0m4} = 1.0$$

Unless

B_{0jk} is input, then set

$$B_{0jk} = B_{0ik}$$

$$j = 0, 1, \text{ or } 2 \quad k = 1, 2, 3, \text{ or } 4$$

or

K_{0mk} is input, then set

$$K_{0mk} = K_{0mk}$$

$$k = 1, 2, 3, \text{ or } 4$$

Where W_{ok} is the input k -th stage liftoff weight (lb), B_{0jk} are coefficients and K_{0mk} is the maximum deflection angle multiplier. The maximum deflection angle versus stage liftoff weight is shown in Figure 30.

(4) Effective Offset Distance

$$\epsilon_{osk} = \begin{cases} \epsilon_{osk} & \text{if } \epsilon_{osk} \text{ is input} \\ K_{0ok} (B_{\epsilon 1} + B_{\epsilon 1} D_{Bk} + B_{\epsilon 2} D_{Bk}^2 + B_{\epsilon 3} D_{Bk}^3) & \end{cases} \quad (\text{in.})$$

$$B_{\epsilon 0} = 0.51640019 \times 10^{-1}$$

$$B_{\epsilon 1} = 0.34855505 \times 10^{-2}$$

$$B_{\epsilon 2} = -0.21364594 \times 10^{-4}$$

$$B_{\epsilon 3} = 0.28005590 \times 10^{-6}$$

Unless $B_{\epsilon j}$ is input, then set

$$B_{\epsilon j} = B_{\epsilon j}$$

$$j = 0, 1, 2, \text{ or } 3$$

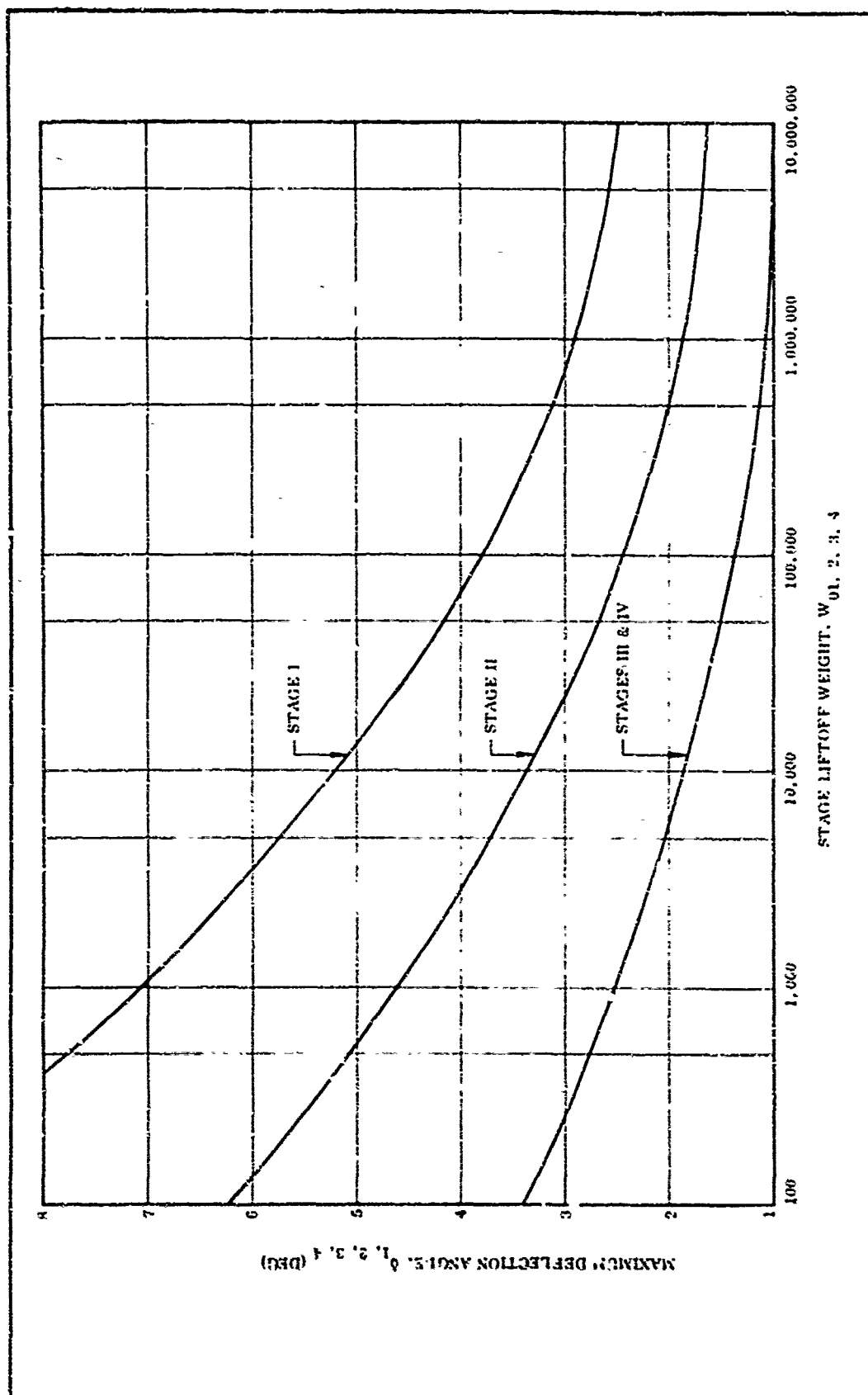


Figure 30. Maximum TVC Deflection Angle vs Stage Lift-off Weight

$$K_{odk} = \begin{cases} K'_{odk} & \text{if } K'_{odk} \text{ is input} \\ 1.0 & \text{otherwise} \end{cases} \quad (\text{dim})$$

Where D_{Bk} is the input k-th stage case diameter (in.), B_k are coefficients and K_{odk} is the effective offset distance multiplier (dim).

c. Aerodynamic Roll Torque

$$M_{ark} = \begin{cases} 0 & \text{if } M'_{rt} \text{ is input} \\ M'_{ark} & \text{if } M'_{ark} \text{ is input} \\ K_{ark} (\pi/576) C_{N\alpha k} D_{Bk}^2 q\alpha'_{mxk} \epsilon_{Gsk} & \text{otherwise} \end{cases}$$

Where M'_{ark} is the input aerodynamic roll torque (in-lbf), K_{ark} is the aerodynamic roll torque multiplier (dim), $C_{N\alpha k}$ is the normal force coefficient (1/deg), D_B is the input case base diameter (in), $q\alpha'_{mxk}$ is the maximum dynamic pressure-angle of attack product (lbf-deg/ft²). The offset distance versus case diameter is given in Figure 31.

(1) Aerodynamic Roll Torque Multiplier

$$K_{ark} = \begin{cases} K'_{ark} & \text{if } K'_{ark} \text{ is input} \\ 1.0 & \text{otherwise} \end{cases} \quad (\text{dim})$$

Where K'_{ark} is the input aerodynamic roll torque multiplier (dim).

(2) Normal Force Coefficient

$$C_{N\alpha k} = \begin{cases} C'_{N\alpha k} & \text{if } C'_{N\alpha k} \text{ is input} \\ 0.05 & \text{otherwise} \end{cases} \quad (1/\text{deg})$$

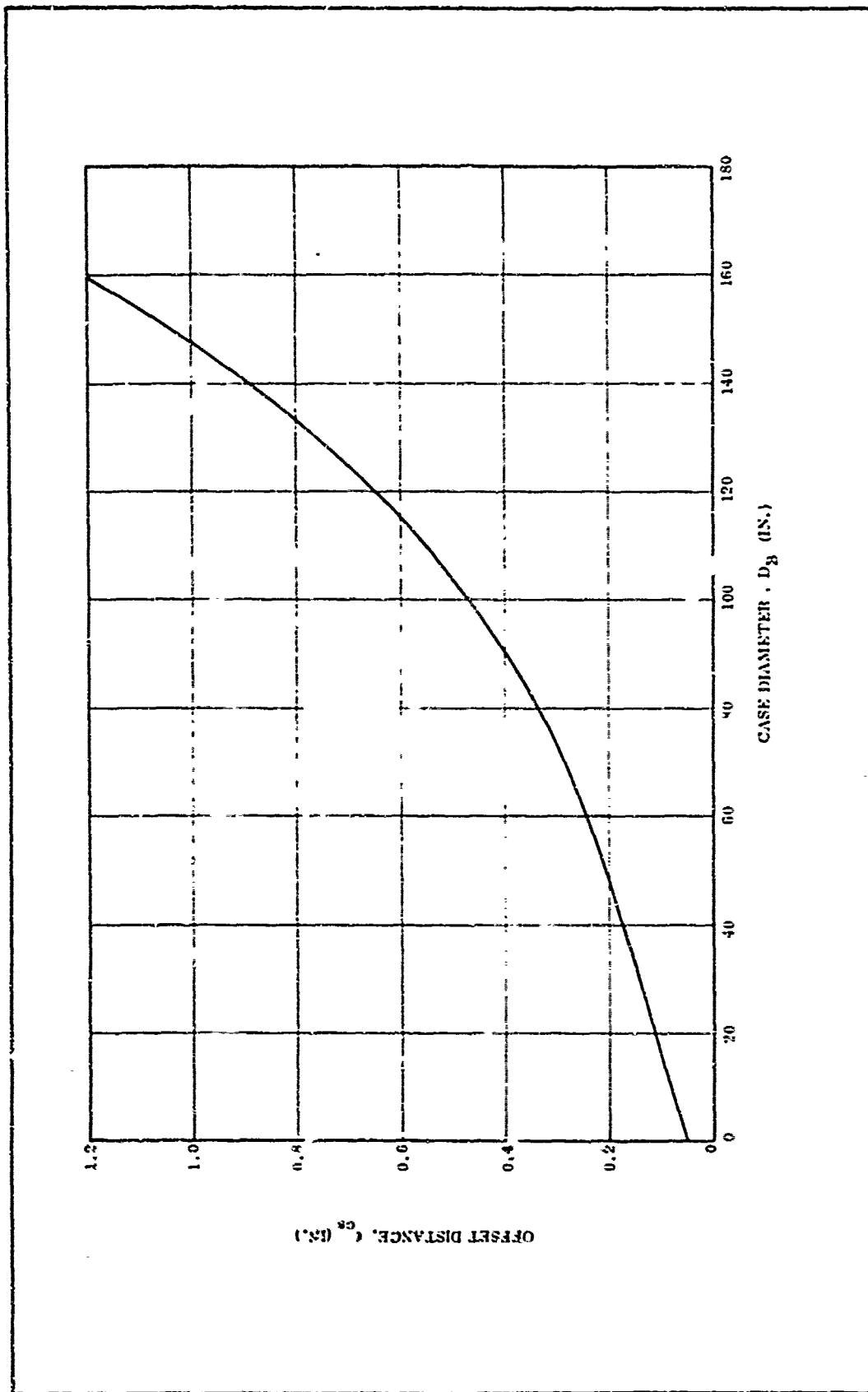


Figure 31. Offset Distance vs Case Diameter

(3) Maximum Dynamic Pressure-Angle of Attack

STAGE I

$$q\alpha'_{mx1} = \begin{cases} q\alpha'_{mx1} & \text{if } q\alpha'_{mx1} \text{ is input} \\ K_{q\alpha1} [B_{q01} + B_{q11} (F_{vac1}/W_{01}) + B_{q21} (F_{vac1}/W_{01})^2 + B_{q31} (F_{vac1}/W_{01})^3] & \text{otherwise} \end{cases} \quad (\text{lb-ft-deg/ft}^2)$$

Where

$$\begin{aligned} B_{q01} &= -1167.3282 \\ B_{q11} &= 5817.9004 \\ B_{q21} &= 868.14226 \\ B_{q31} &= -209.07636 \end{aligned}$$

unless B'_{qj1} is input, then set

$$B_{qj1} = B'_{qj1}$$

$j = 0, 1, 2, \text{ or } 3$

$$K_{q\alpha1} = \begin{cases} K'_{q\alpha1} & \text{if } K'_{q\alpha1} \text{ is input} \\ 1.0 & \text{otherwise} \end{cases} \quad (\text{dim.})$$

STAGE II

$$q\alpha'_{mx2} = \begin{cases} q\alpha'_{mx2} & \text{if } q\alpha'_{mx2} \text{ is input} \\ K_{q\alpha2} [B_{q02} + B_{q12} (F_{vac1}/W_{01}) + B_{q22} (F_{vac1}/W_{01})^2 + B_{q32} (F_{vac1}/W_{01})^3] & \text{otherwise} \end{cases} \quad (\text{lb-ft-deg/ft}^2)$$

Where

$$\begin{aligned} B_{q02} &= 2564.6454 \\ B_{q12} &= -3653.9365 \\ B_{q22} &= 1477.6228 \\ B_{q32} &= -60.327994 \end{aligned}$$

unless B'_{qj2} is input, then set

$$B_{qj2} = B'_{qj2}$$

$i = 0, 1, 2, \text{ or } 3$

$$K_{q\alpha 2} = \begin{cases} K'_{q\alpha 2} & \text{if } K'_{q\alpha 2} \text{ is input} \\ 1.0 & \text{otherwise} \end{cases} \quad (\text{dim})$$

STAGE III

$$q\alpha_{mx3} = \begin{cases} q'_{\alpha_{mx3}} & \text{if } q'_{\alpha_{mx3}} \text{ is input} \\ 0 & \text{otherwise} \end{cases} \quad (\text{lb deg/ft}^2)$$

STAGE IV

$$q_{mx4} = \begin{cases} q'_{mx4} & \text{if } q'_{mx4} \text{ is input} \\ 0 & \text{otherwise} \end{cases} \quad (\text{lb deg/ft}^2)$$

Where B_{qjk} are coefficients (dim), $K_{q\alpha k}$ are the maximum dynamic pressure-angle of attack multipliers (dim), F_{vac1} is the Stage I input average webtime vacuum thrust (lb) and W_{01} Stage I liftoff weight (lbm). The maximum $q\alpha$ versus vacuum thrust to weight is given in Figure 32.

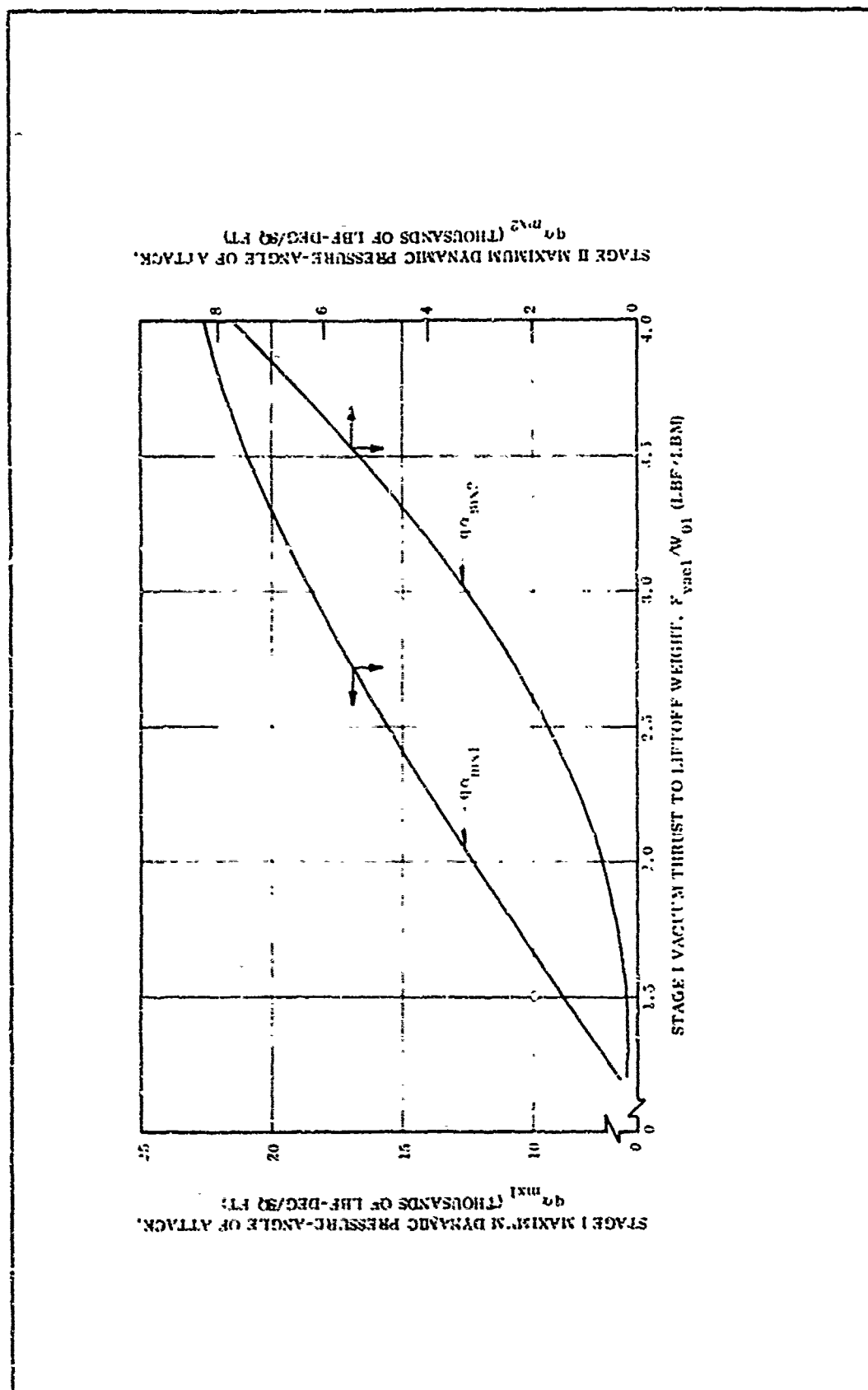


Figure 32. Maximum $q\alpha$ vs Vacuum Thrust to Weight

2. ROLL CONTROL SUBROUTINE NOMENCLATURE

| SYMBOL | DEFINITION | UNITS |
|--------------|--|---------------|
| H DELTA IK | FACTOR OF MAX THRUST VECT DEFLECTN ANGLE OF KTH STAGE | -- |
| R FOST K | CONSTANTS USED TO COMPUTE EFFECTIVE OFFSET DISTANCE | -- |
| RJ JK | COEFFICIENTS FOR COMPUTING MAX DYN PRESS-ANGLE OF ATTK | -- |
| CN ALPHA | INPUT NORMAL FORCE COEFFICIENT | (1/DEG) |
| CN ALPHA Q | AERODYNAMIC NORMAL FORCE COEFFICIENT AT MAX QALPHA | (1/DEG) |
| DR | OUTPUT TVC DUTY CYCLE STAGE CASE DIAMETER | IN |
| DELTA MXK | MAX THRUST VECTOR DEFLECTION ANGLE | DEG |
| DELTA PMXK | INPUT MAX THRUST VECTOR DEFLECTION ANGLE | DEG |
| DELTA BAROMX | MAX MAGNITUDE PITCH VECTOR DEFLECTION ANGLE | DEG |
| FOSTEN TSK | EFFECTIVE OFFSET DISTANCE | IN |
| ETA VRK | VORTEX ROLL TORQUE PER POUND OF THRUST FACTOR | IN |
| ETA VRK | INPUT VORTEX ROLL TORQUE PER POUND OF THRUST FACTOR | IN |
| FVAC | NOMINAL INPUT VACUUM THRUST-TIME CURVE | LB |
| FVACK | INPUT AVERAGE WFTIME VACUUM THRUST | LB F |
| KAPK | AERODYNAMIC ROLL TORQUE MULTIPLIER | -- |
| K DELTA MK | FACTOR OF MAX THRUST VECTOR DEFLECTION ANGLE | -- |
| KK | STAGE NUMBER | -- |
| KJDK | EFFECTIVE OFFSET DISTANCE MULTIPLIER | -- |
| KJCK | OFFSET ROLL TORQUE MULTIPLIER | -- |
| KQ ALPHA K | FACTOR OF MAX DYNAMIC PRESSURE-ANGLE OF ATTACK PRODUCT | -- |
| KVRK | VORTEX ROLL TORQUE MULTIPLIER | -- |
| KJISK | INPUT OFFSET TORQUE MULTIPLIER | -- |
| MARX | AERODYNAMIC ROLL TORQUE | IN-LBF |
| MJCK | OFFSET ROLL TORQUE | IN-LBF |
| MRTK | ROLL TORQUE | IN-LBF |
| MVRK | VORTEX ROLL TORQUE | IN-LBF |
| MJISK | INPUT OFFSET ROLL TORQUE | IN-LBF |
| MRTX | INPUT ROLL TORQUE | IN-LBF |
| MVRX | INPUT VORTEX ROLL TORQUE | IN-LBF |
| QALPHA M | DYNAMIC PRESSURE | LB-FT**2 |
| QALPHA MXK | MAXIMUM DYNAMIC PRESSURE-ANGLE OF ATTACK PRODUCT | LBF-DEG/FT**2 |
| WJ | STAGE LIFTOFF WEIGHT | LB |